

# Exam

# FINAL

**P201 Fall 2006,  
Instructor: Prof. Abanov**

**12/13/06**

Name\_\_\_\_\_

Section\_\_\_\_\_

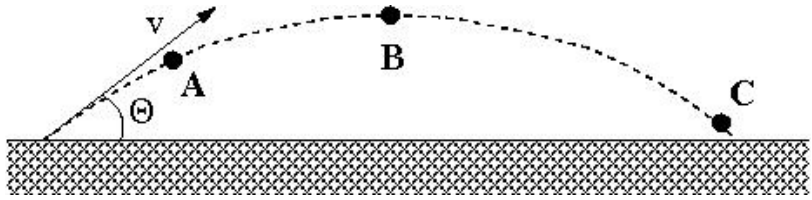
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# Your grade:

## Problem 1.

A ball has been thrown from the ground level with initial velocity  $v = 20\text{m/s}$  at the initial angle

$\theta = 30^\circ$ . Point B is the top of the trajectory, point C is right before the ball hits the ground.



What is the ball's acceleration at points A, B, and C? A \_\_\_\_\_, B \_\_\_\_\_, C \_\_\_\_\_

What is horizontal component of the velocity at points B and C? B \_\_\_\_\_, C \_\_\_\_\_

What is vertical component of the velocity at points B and C? B \_\_\_\_\_, C \_\_\_\_\_

What time does it take for the ball to reach the points B and C? B \_\_\_\_\_, C \_\_\_\_\_

What is the height of the trajectory at the point B? \_\_\_\_\_

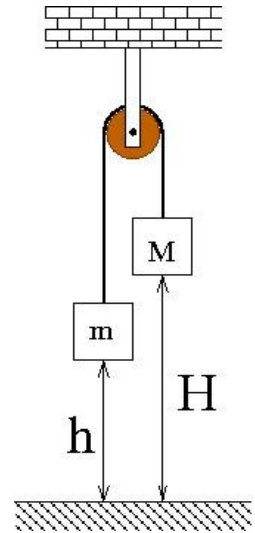
What is the distance from the initial point to the point C? \_\_\_\_\_

What would the height of the trajectory at the point B be if you doubled the initial velocity? \_\_\_\_\_

What would the distance from the initial point to the point C be if you doubled the initial velocity? \_\_\_\_\_

### Problem 2.

Two bricks with masses  $M=20\text{kg}$  and  $m=16\text{kg}$  are hanging at the height  $h=2\text{m}$  and  $H=5\text{m}$  on a frictionless pulley as shown on the figure. At the initial moment everything is at rest



What is the acceleration of the bricks  $m$  and  $M$ ?  $M$ \_\_\_\_\_,  $m$ \_\_\_\_\_

What is the tension  $T$  of the rope? \_\_\_\_\_

What is the initial energy of the system? \_\_\_\_\_

What is the potential energy of the system when the brick  $M$  hits the floor? \_\_\_\_\_

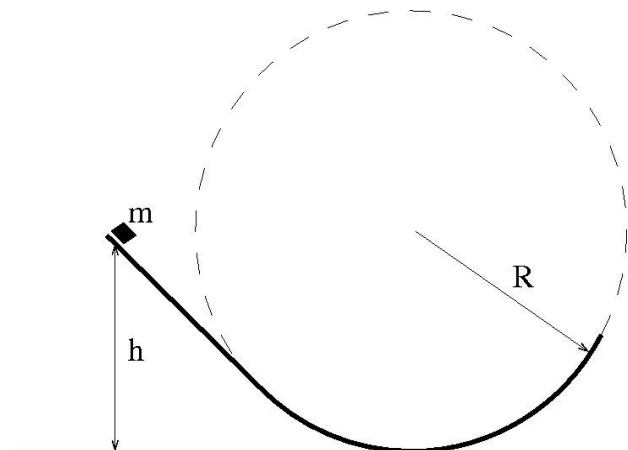
What is the velocity of the brick  $M$  right before it hits the floor? \_\_\_\_\_

What would be the velocity of the brick  $M$  right before it hits the floor, if 20 Joules of heat were produced in the block due to friction? \_\_\_\_\_

### Problem 3.

A brick of mass  $m=5\text{kg}$  slides down a frictionless ramp from a height  $h=2\text{m}$ . The ramp at the end bends with radius  $R=2\text{m}$  as shown in the figure.

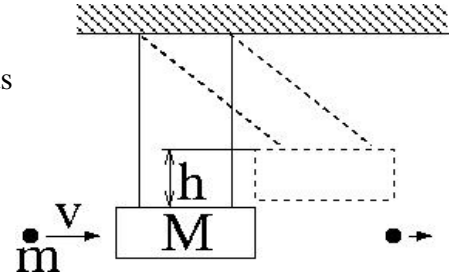
What is the velocity of the brick at the bottom of the ramp? \_\_\_\_\_



What is the magnitude of upright force which acts on the brick at the bottom of the ramp? \_\_\_\_\_

**Problem 4.**

A bullet of mass  $m=10\text{g}$  has an initial velocity  $v=300\text{m/s}$ . It goes through a wooden brick of mass  $M=5\text{kg}$  which is hanging as shown in the figure. The speed of the bullet on the other side of the brick is half of its initial speed.



What is the initial momentum of the system? \_\_\_\_\_

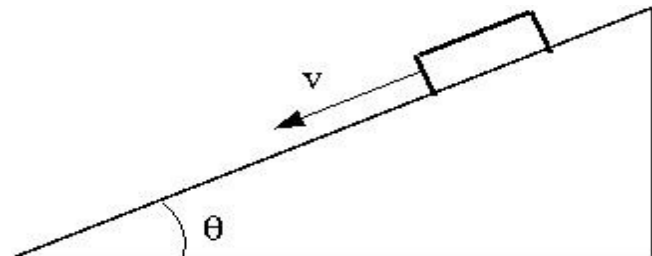
What is the maximum height  $h$  the brick  $M$  will get to? \_\_\_\_\_

How much of the initial energy of the bullet were converted to heat? \_\_\_\_\_

**Problem 5.**

A brick of mass  $M=4\text{kg}$  on a slope of the angle  $\theta=20^\circ$  initially has a velocity  $v=2\text{m/s}$

The friction coefficient between the brick and the slope is  $\mu=0.4$



What is the friction force which acts on the brick?  $F=$  \_\_\_\_\_ (show the direction on the figure)

What is the acceleration of the brick? \_\_\_\_\_

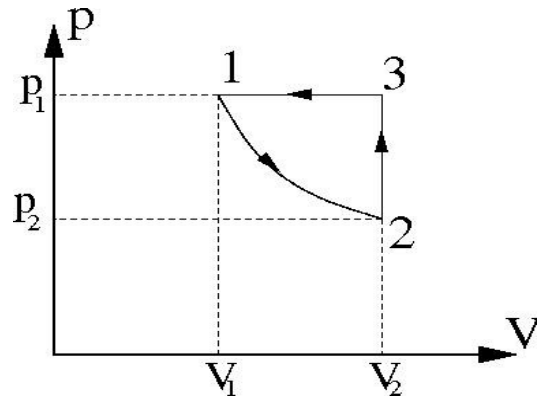
How much time will it take the brick to stop? \_\_\_\_\_

What distance will the brick move until it stops? \_\_\_\_\_

How much heat will be produced by the friction? \_\_\_\_\_

**Problem 6.**

One mole of an ideal gas has initial temperature 500K and initial volume  $1\text{m}^3$  (1). During an isothermal process its volume doubled (2). Then by a process at constant volume it was brought to the initial pressure (3). Finally, decreasing volume at constant pressure the gas was brought to the initial state.



What is the initial pressure  $p_1$  ? \_\_\_\_\_

What are the volume  $V_2$  , the pressure  $p_2$  and the temperature  $T_2$  at the state (2)? \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_

What are the volume  $V_3$  , the pressure  $p_3$  and the temperature  $T_3$  at the state (3)? \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_

How much work had to be done on the gas during the process 2-3? \_\_\_\_\_

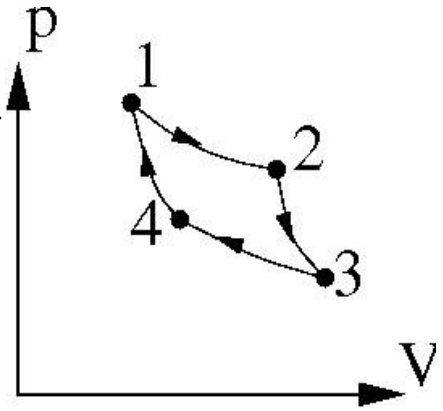
How much internal energy of the gas has changed during the process 2-3? \_\_\_\_\_

How much heat had to be supplied to the gas during the process 2-3? \_\_\_\_\_

How much heat had to be supplied to the gas during the process 3-1? \_\_\_\_\_

**Problem 7.**

One mole of an ideal gas goes around the Carnot cycle. The temperature of the hot heat bath is  $T_H=400\text{K}$  , the temperature of the cold bath is  $T_C=350\text{K}$  . During the process 1-2 the gas received  $4\text{J}$  of heat.



**What work is done by the gas during the process 2-3?\_\_\_\_\_**

**What work is done by the gas during the process 4-1?\_\_\_\_\_**

**How much work has been done by the gas during the process 1-2?\_\_\_\_\_**

**How much heat the gas transferred to the cold bath during the process 3-4?\_\_\_\_\_**

**How much work the gas has done during the process 3-4?\_\_\_\_\_**

**What is the thermal efficiency of this heat engine?\_\_\_\_\_**

**What is the change of entropy during the processes 1-2, 2-3, 3-4, 4-1? \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_**

**What is the net change of entropy during the cycle? Why?\_\_\_\_\_**

**Problem 8.**

A wire with mass  $50\text{g}$  is stretched so that its ends are tied down at points  $70\text{cm}$  apart. The wire vibrates in its fundamental mode with frequency  $170\text{Hz}$  and with an amplitude of  $0.8\text{cm}$  at the antinodes.

What is the wavelength of the fundamental mode? \_\_\_\_\_

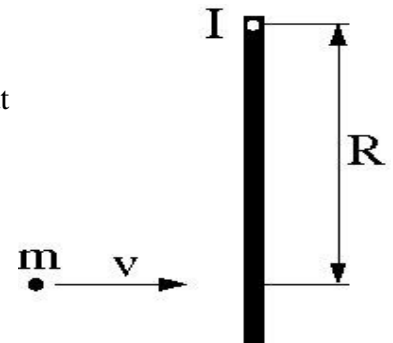
What is the speed of the wave? \_\_\_\_\_

What is the tension of the wire? \_\_\_\_\_

What are the frequency of the second harmonic? \_\_\_\_\_

**Problem 9.**

A bullet of mass  $m=10\text{g}$  and velocity  $v=300\text{m/s}$  hits a door at the distance  $R=1\text{m}$  (see figure) and gets stuck in it. The door is initially at rest. The door's moment of inertia is  $I=10\text{kg}\cdot\text{m}^2$ .



What is the initial angular momentum of the system? \_\_\_\_\_

What is initial energy of the system? \_\_\_\_\_

What is the final angular velocity of the door? \_\_\_\_\_

How much heat was produced during the collision? \_\_\_\_\_

**Problem 10.**

A piece of metal (  $\rho_m = 10000\text{kg}/\text{m}^3$  ) of mass  $m = 10\text{g}$  is attached by a rope to a chunk of ice (  $\rho_i = 900\text{kg}/\text{m}^3$  ) of mass  $M = 100\text{g}$  (see figure). The density of water is  $\rho_w = 1000\text{kg}/\text{m}^3$  .

**What is the tension of the rope?**\_\_\_\_\_

**What volume of the ice sticks out of the water?**\_\_\_\_\_

