

# Strong-Field Imaging of Molecular Dynamics

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# Explosion Energies

$$E_{\text{ex}} = \frac{Z_1 Z_2}{R}$$

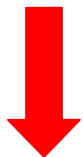
Light Atoms

Heavy Atoms

TABLE IV. Total kinetic-energy releases in the fragmentation channels following the multielectron dissociative ionization of N<sub>2</sub>, CO, and O<sub>2</sub> in intense laser field with 100-fs pulse duration, 615-nm wavelength in the 10<sup>15</sup> W/cm<sup>2</sup> range.

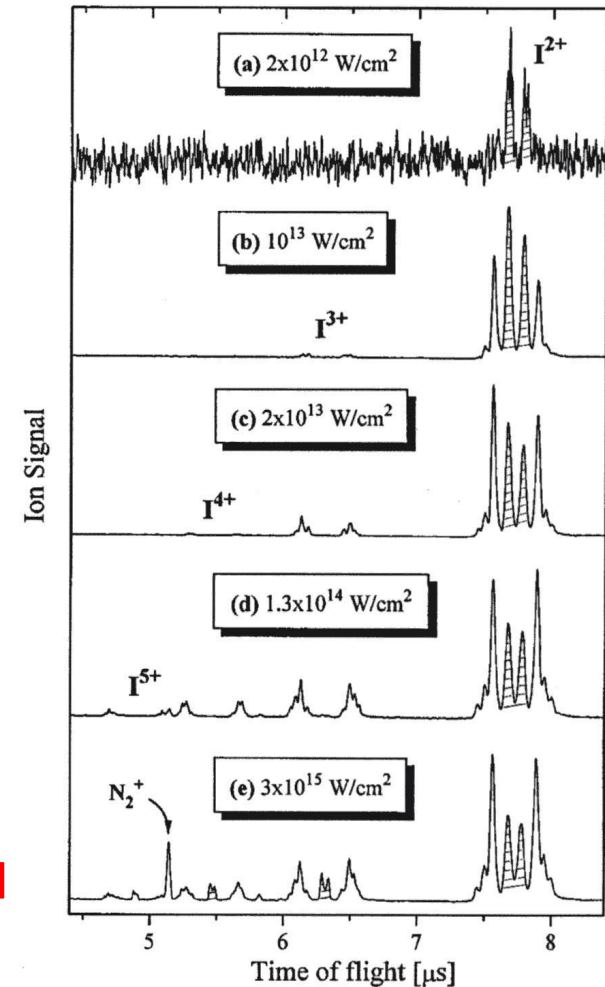
Fragment channel	Molecule AB		
	N <sub>2</sub>	CO	O <sub>2</sub>
A <sup>+</sup> + B <sup>+</sup>	6.8	6.6	5.5
A <sup>+</sup> + B <sup>2+</sup>		11.7	
A <sup>2+</sup> + B <sup>+</sup>	13.1	11.7	11.9
A <sup>2+</sup> + B <sup>2+</sup>	22	19.9	20
A <sup>2+</sup> + B <sup>3+</sup>		32.7	
A <sup>3+</sup> + B <sup>2+</sup>	32	29.8	32

Cornaggia, *et al.*, PRA **44**, 4499 (1991)



$R_c \approx 0.28$  nm  
~40% of  $E_{\text{eq}}$

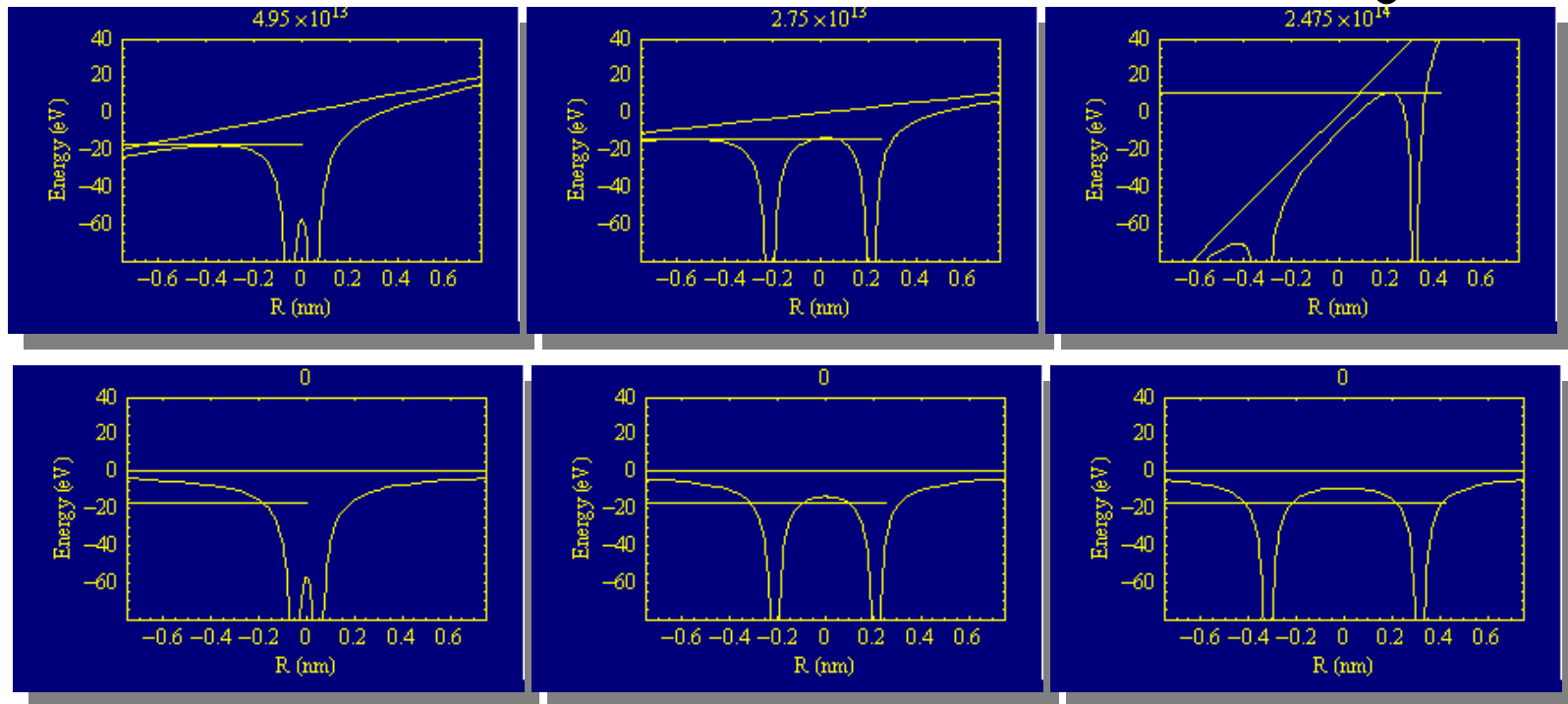
$R_c \approx 0.38$  nm  
~70% of  $E_{\text{eq}}$



Normand, *et al.*, PRA **53**, R1958 (1996)

# Enhanced Ionization at $R_c$

I ↑

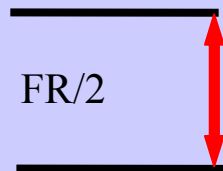


$R = R_{eq}$

$R = R_{eq}$

$R > R_{eq}$

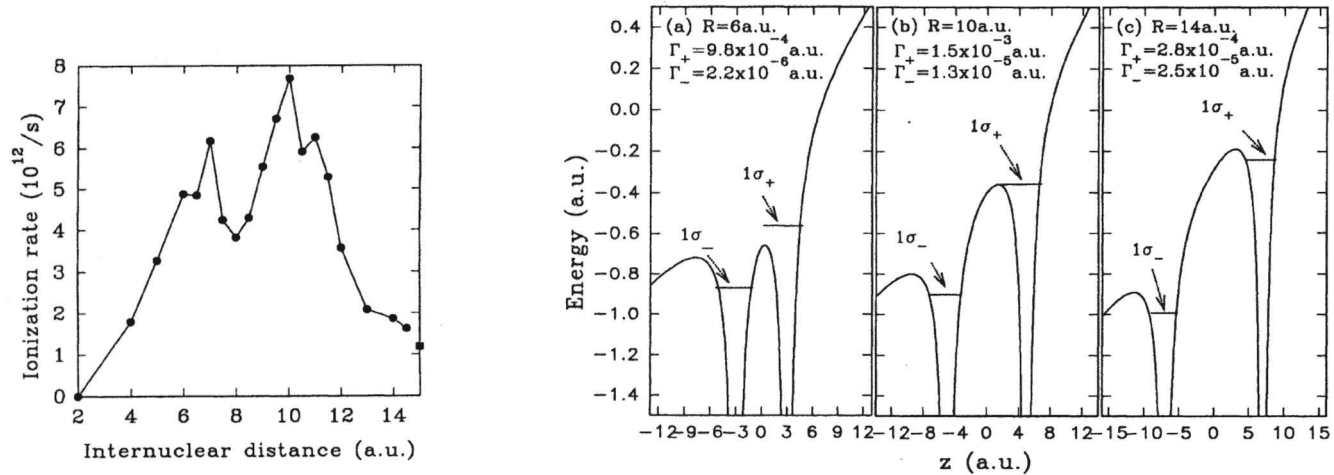
Posthumus, *et al.* J.Phys.**28**; Zuo & Bandrauk, PRA **52**; Seideman, *et al.* PRL **75**



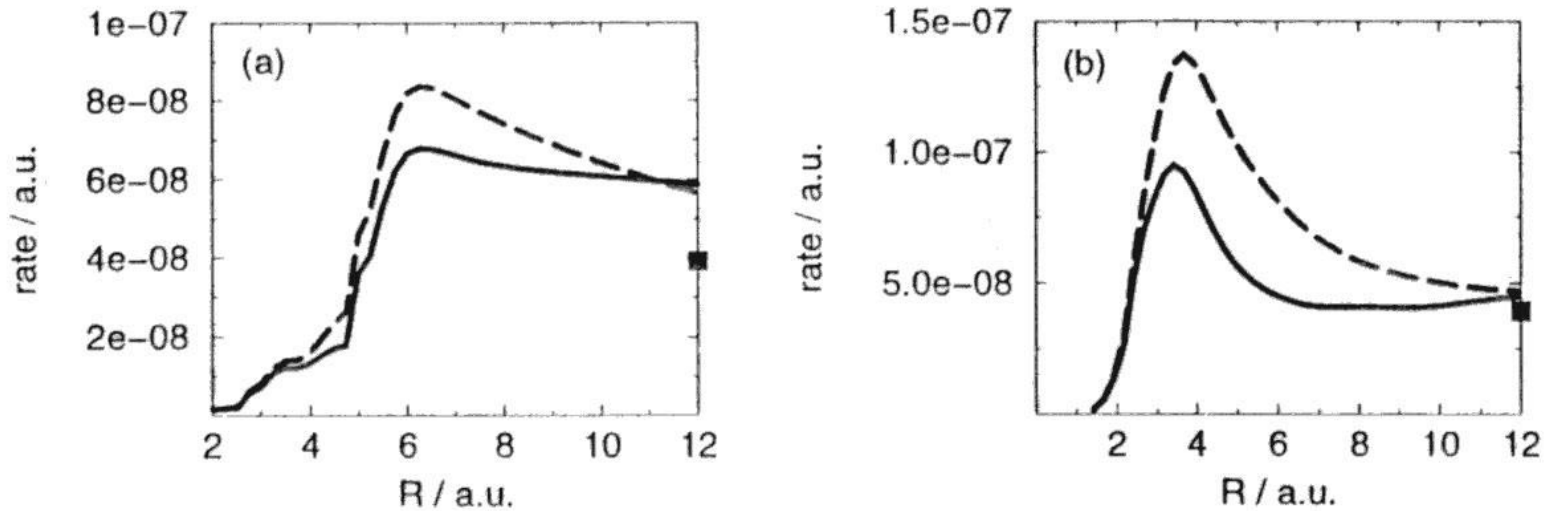
$$1\sigma_g \rightarrow (1s_1 + 1s_2)/\sqrt{2}$$

$$1\sigma_u \rightarrow (1s_1 - 1s_2)/\sqrt{2}$$

# Enhanced Ionization: Theory



Numerical Integration of SE in 3D; Zuo and Bandrauk, PRA 52, R2511 (1995)



Manybody S-Matrix; J. Muth-Böhm, A. Becker and F. H. M. Faisal, ICOMP VIII (99)

# H<sub>2</sub> Explosion Energy: Experiment

Theory  $\longrightarrow$   $R_c = 4/I_p$  (au)

Zuo and Bandrauk, PRA **52**, R2511 (1995)

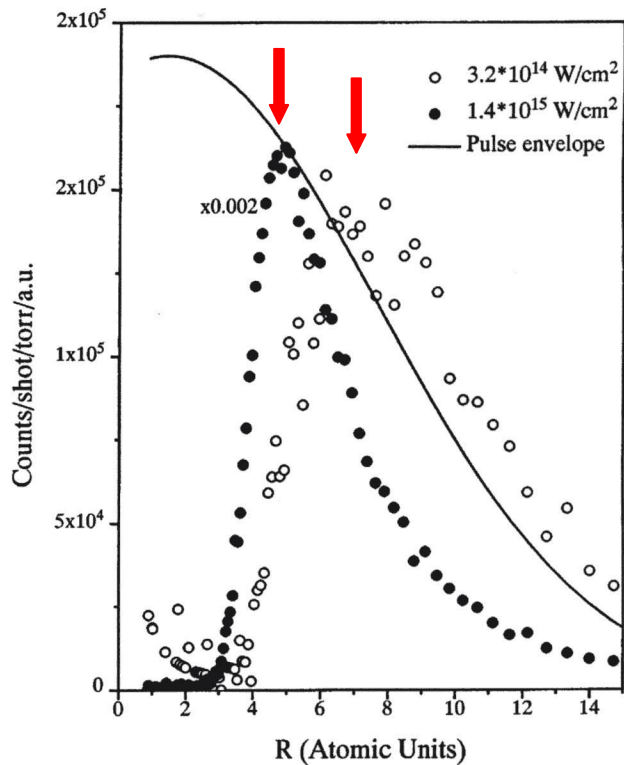
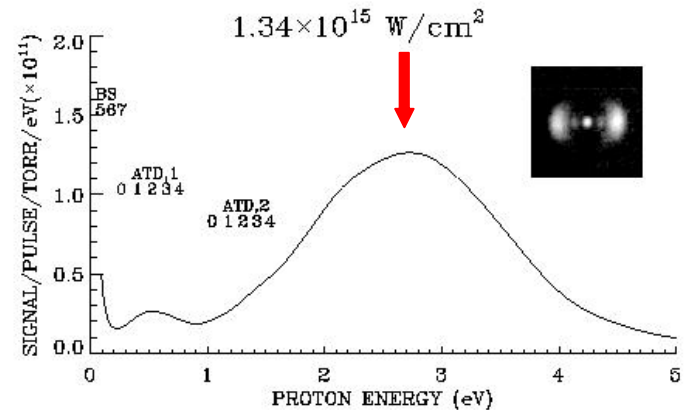
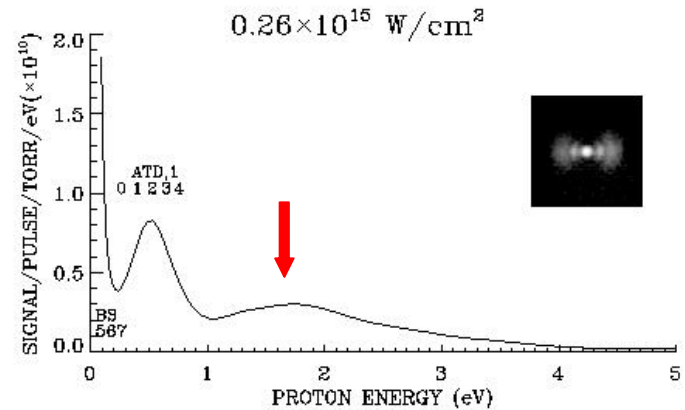


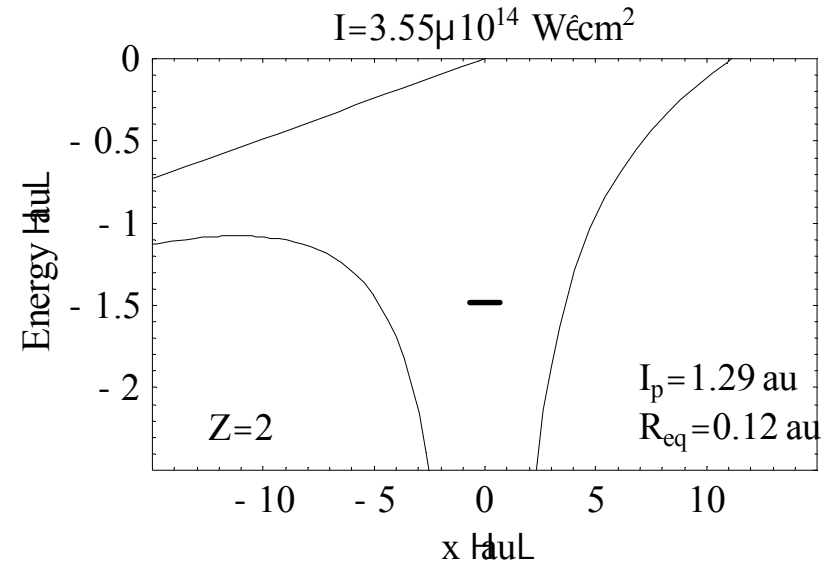
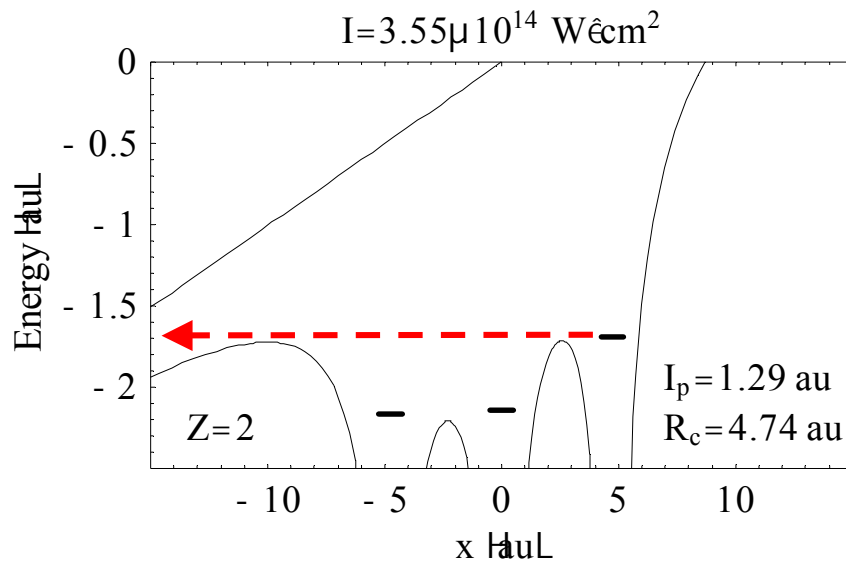
FIG. 4. Ionization signal as a function of internuclear separation and the laser intensity envelope.

Gibson, *et al.*, PRL **79**, 2022 (1997)



Zhang and Hill, unpublished

# 3-Atom Enhanced Ionization at $R_c$



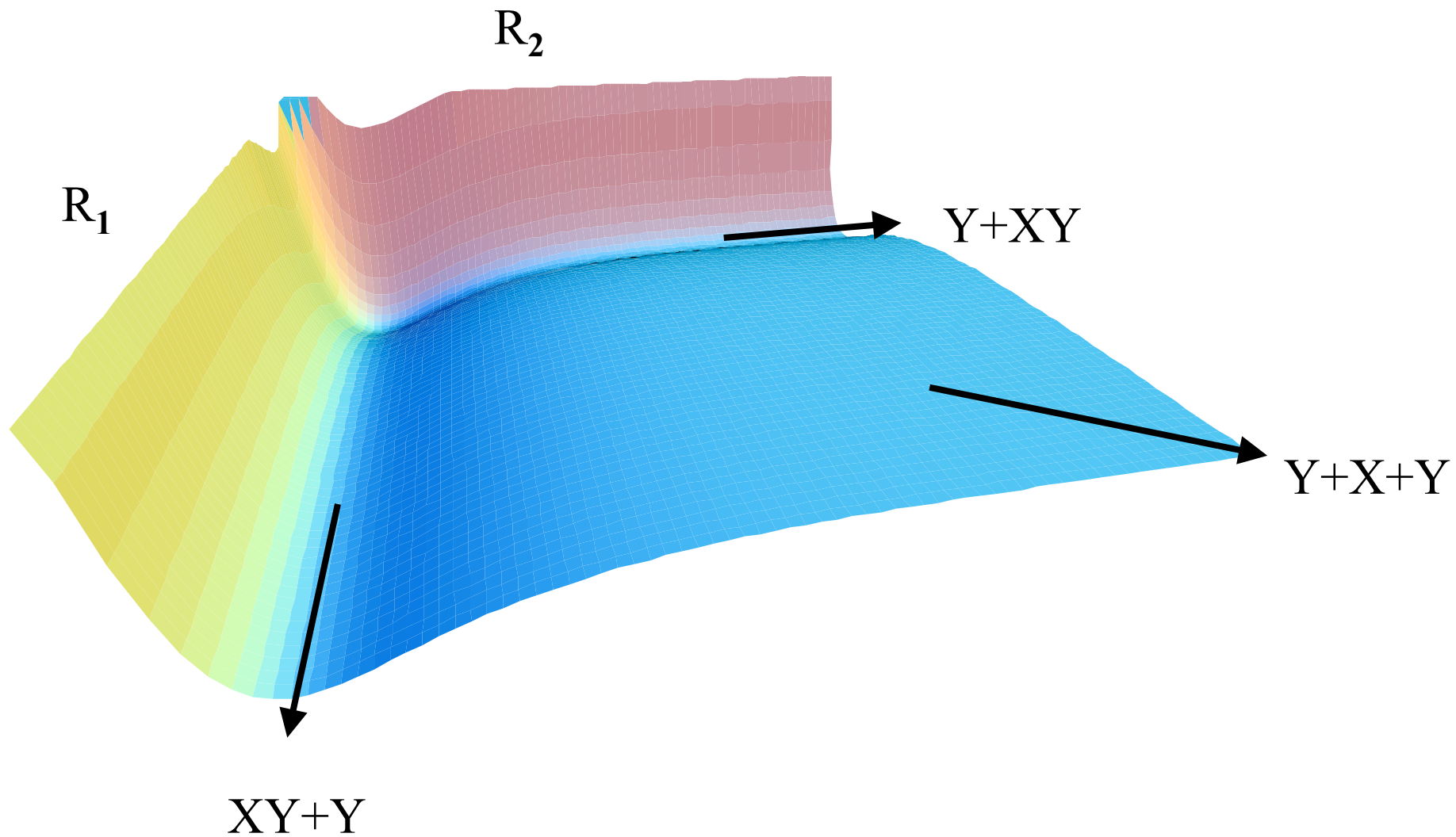
$$E_{\text{mea}} \approx 66 \text{ eV} \quad \rightarrow \quad V(r_{CO} = R_c) = \sum_{i < j} \frac{Z_i Z_j}{r_{ij}} \quad \rightarrow \quad R_c \approx 0.22 \text{ nm (4 au)}$$



$$p, q, r = 1, 2, 3$$

**No intermediate molecular states observed!**

# GENERIC $XY_2$ LINEAR POTENTIAL SURFACE



What about the electrons?



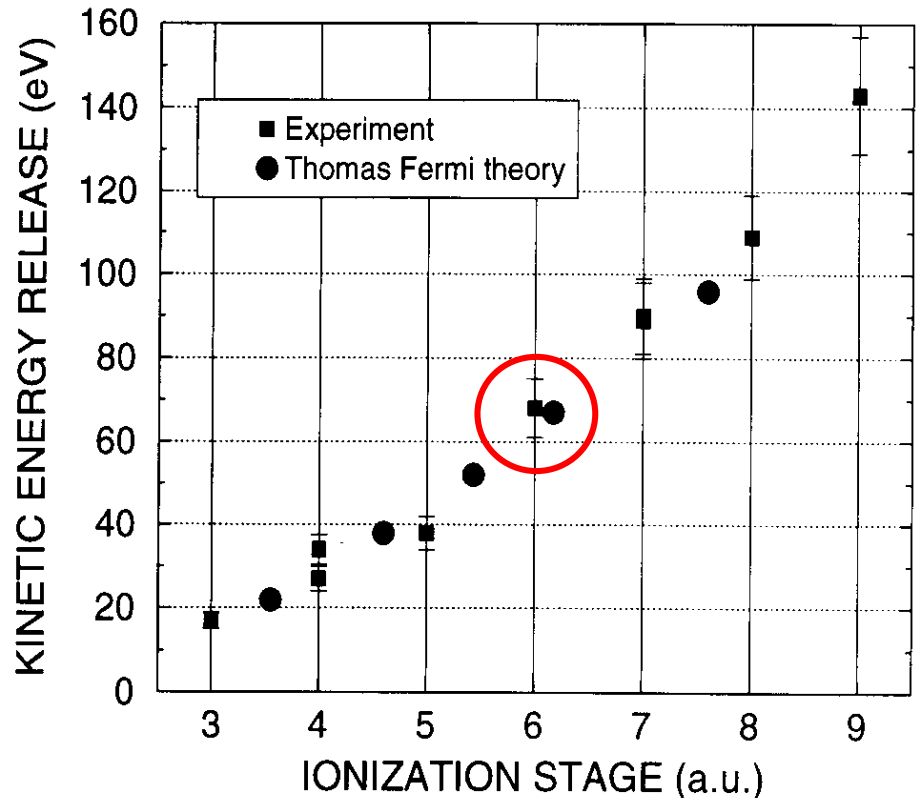
# Dynamic Screening Explosion Model

Brewczyk, Rzażewski and Clark PRL **78**, 191 (1997)

Ionization and  
Dissociation *Interlaced*  
**Electrons do not leave  
region immediately!**



Dissociation begins @  $R_{eq}$   
but slowed by electron cloud  
producing energies consistent  
with dissociation from  $R_c$ .



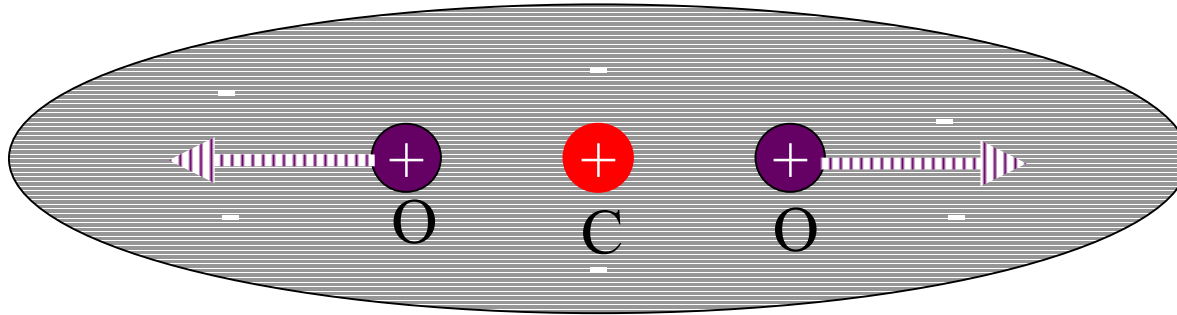
Hering, Brewczyk and Cornaggia, PRL **85**, 2288 (2000)

# Thomas-Fermi Hydrodynamic Model

$$\Phi(x, y) = \frac{Ze}{[b^2 + (x - R)^2 + y^2]^{1/2}} + \frac{Z_0 e}{[b^2 + x^2 + y^2]^{1/2}} + \frac{Ze}{[b^2 + (x + R)^2 + y^2]^{1/2}} - \frac{e^2}{2Am^2} \iint_{-\infty}^{\infty} \frac{\Phi(x', y') dx' dy'}{[c^2 + (x - x')^2 + (y - y')^2]^{1/2}},$$

$$U(R) = -\frac{Ze^2}{2m} \iint_{-\infty}^{\infty} \frac{\rho_{\text{at}}^{Z_0}(x, y) + \rho_{\text{at}}^Z(x - R, y)}{[b^2 + (x + R)^2 + y^2]^{1/2}} dx dy - \frac{Ze^2}{2m} \iint_{-\infty}^{\infty} \frac{\rho_{\text{at}}^{Z_0}(x, y) + \rho_{\text{at}}^Z(x + R, y)}{[b^2 + (x - R)^2 + y^2]^{1/2}} dx dy - \frac{Z_0 e^2}{2m} \iint_{-\infty}^{\infty} \frac{\rho_{\text{at}}^Z(x + R, y) + \rho_{\text{at}}^Z(x - R, y)}{(b^2 + x^2 + y^2)^{1/2}} dx dy + 2 \frac{ZZ_0 e^2}{R} + \frac{ZZe^2}{2R},$$

# Static Screening Model

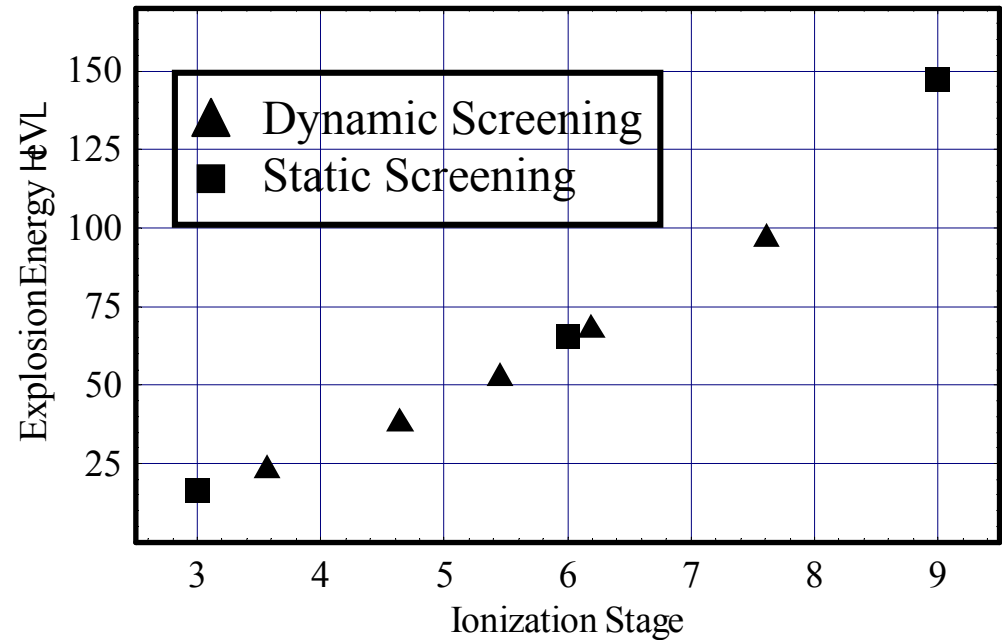


$$Z^{eff} = Z - \sigma$$

$$\sum_{i < j} \frac{Z_i^{eff} Z_j^{eff}}{r_{ij}^{eq}} \approx 66 \text{ eV}$$

$$\sum_{i < j} \frac{Z_i Z_j}{r_{ij}} \Big|_{r_{CO}=R_C} = \sum_{i < j} \frac{Z_i^{eff} Z_j^{eff}}{r_{ij}} \Big|_{r_{CO}=R_{eq}}$$

$$\sigma \equiv Z \left( 1 - \sqrt{R_{eq}/R_C} \right)$$



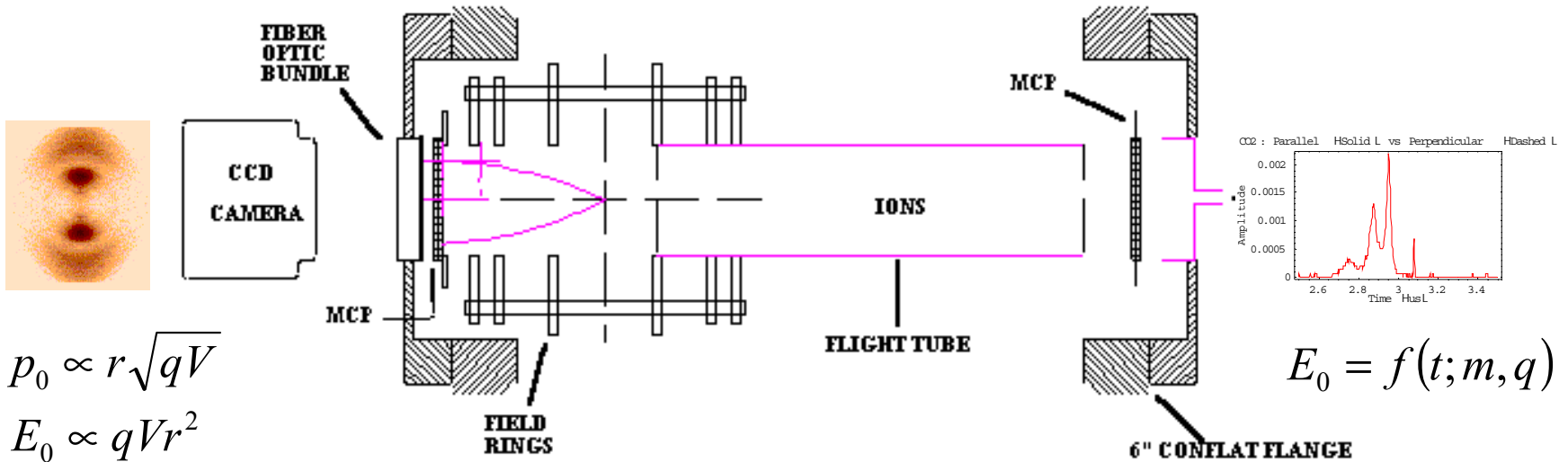
Zhao, Zhang and Hill, PRA (submitted)

# Angular Dependence of $E_C$

$$\varepsilon = \frac{2Z^2}{R_C(\theta_b)} + \frac{Z^2}{2R_C(\theta_b)\sin(\theta_b/2)}$$

$$\varepsilon = \frac{2[Z - \sigma(\theta_b)]^2}{R_{eq}} + \frac{[Z - \sigma(\theta_b)]^2}{2R_{eq}\sin(\theta_b)}$$

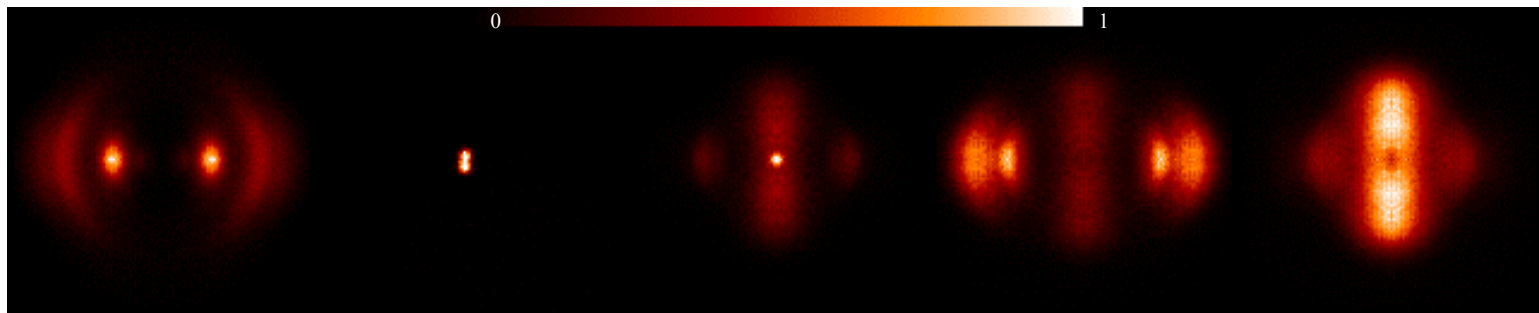
# Momentum & Time-of-Flight Spectra



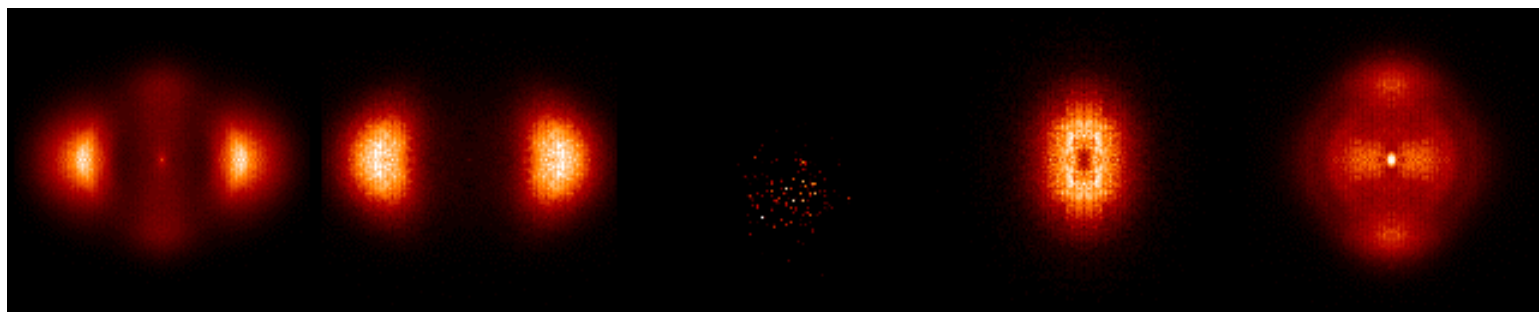
**Time-Resolved Images**  
 128 x 128 Pixels  
 730 Hz Digital Acquisition  
 500,000 – 1,000,000 Frames  
*Mass-Resolved*

*Energies & Angular Distributions*

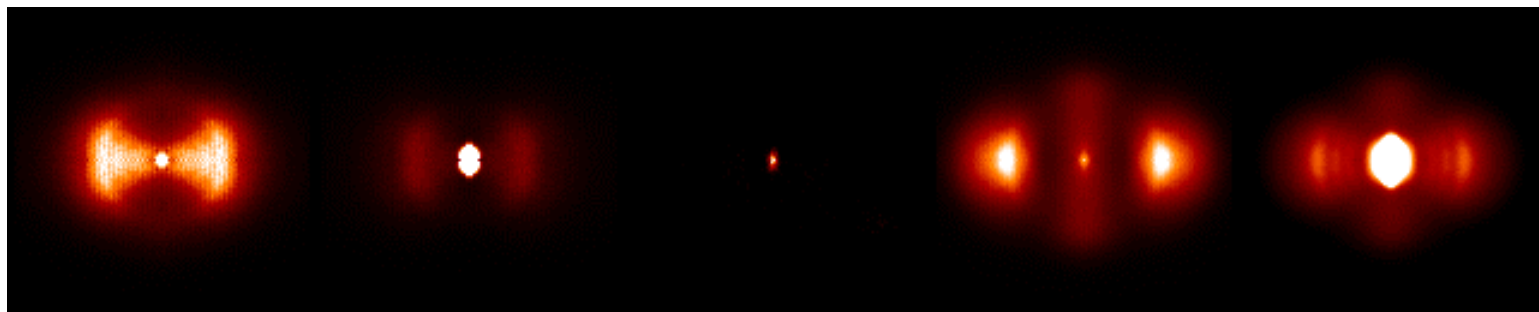
**Time-Resolved Waveforms**  
 Digital Scope Acquisition  
*Mass-Resolved*  
*Energies Distributions*



(a)  $\text{H}^+$  110 – 210 ns      (b)  $\text{H}_2^+$  210 – 310 ns      (c)  $\text{N}^{3+}$  320 – 420 ns      (d)  $\text{N}^{3+}, \text{O}^{3+}$  370 – 470 ns      (e)  $\text{N}^{2+}$  420 – 520 ns

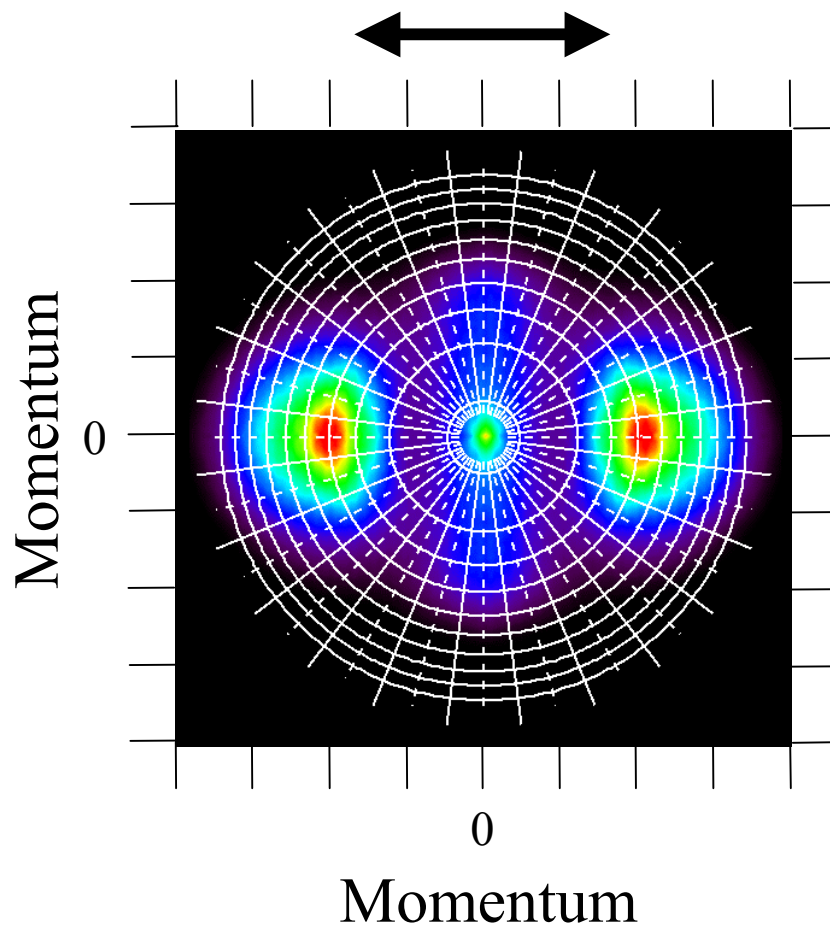
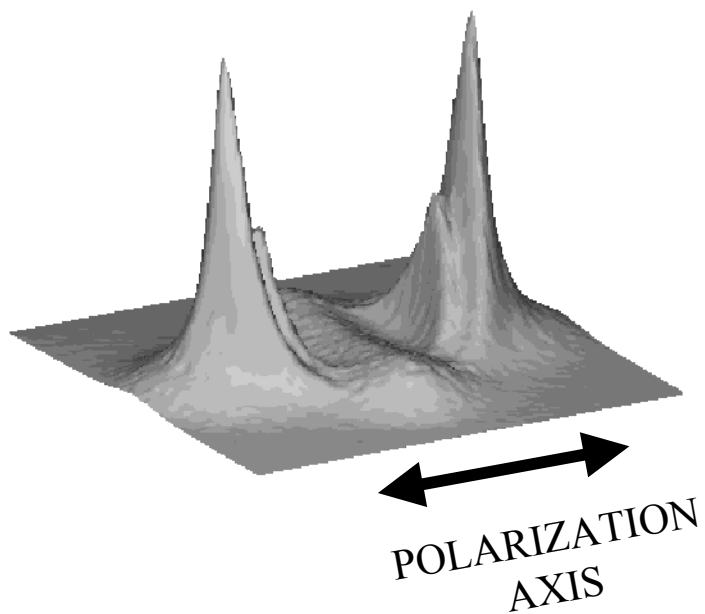


(f)  $\text{N}^{2+}, \text{O}^{2+}$  470 – 570 ns      (g)  $\text{O}^{2+}$  520 – 620 ns      (h) 570 – 670 ns      (i)  $\text{N}^+$  620 – 720 ns      (j)  $\text{N}^+$  670 – 770 ns



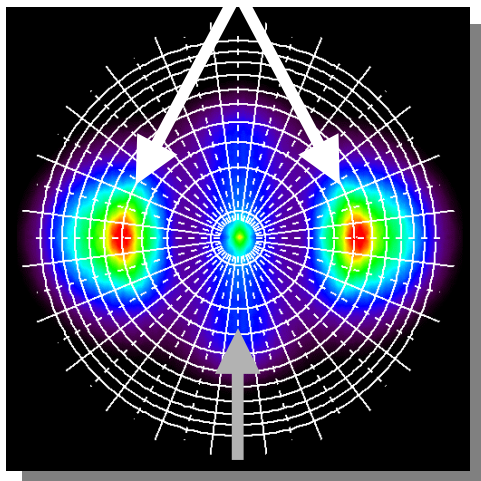
(k)  $\text{O}^+$  720 – 820 ns      (l)  $\text{O}^+$  770 – 870 ns      (m)  $\text{OH}^+$  820 – 920 ns      (n)  $\text{N}^{2+,3+}, \text{O}^{2+,3+}$  320 – 620 ns      (o) All Ions All Time

# Momentum Image

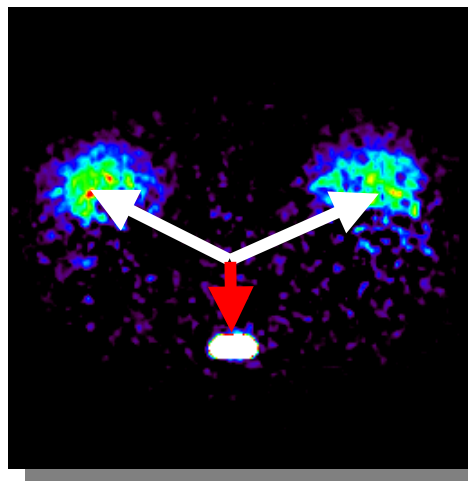


Scale: 5 – 8 amu/div

# Correlation Imaging



AVERAGE IMAGE



SELECTIVE AVERAGE

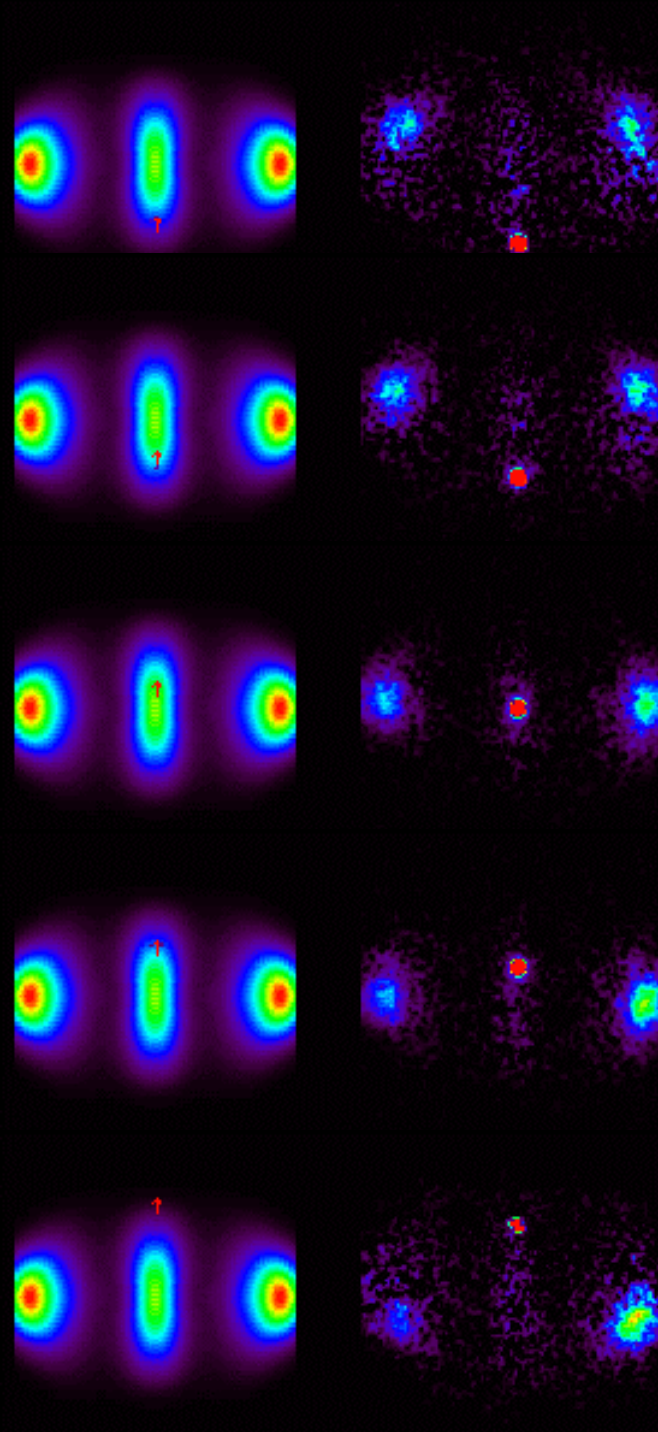


POLARIZATION  
AXIS



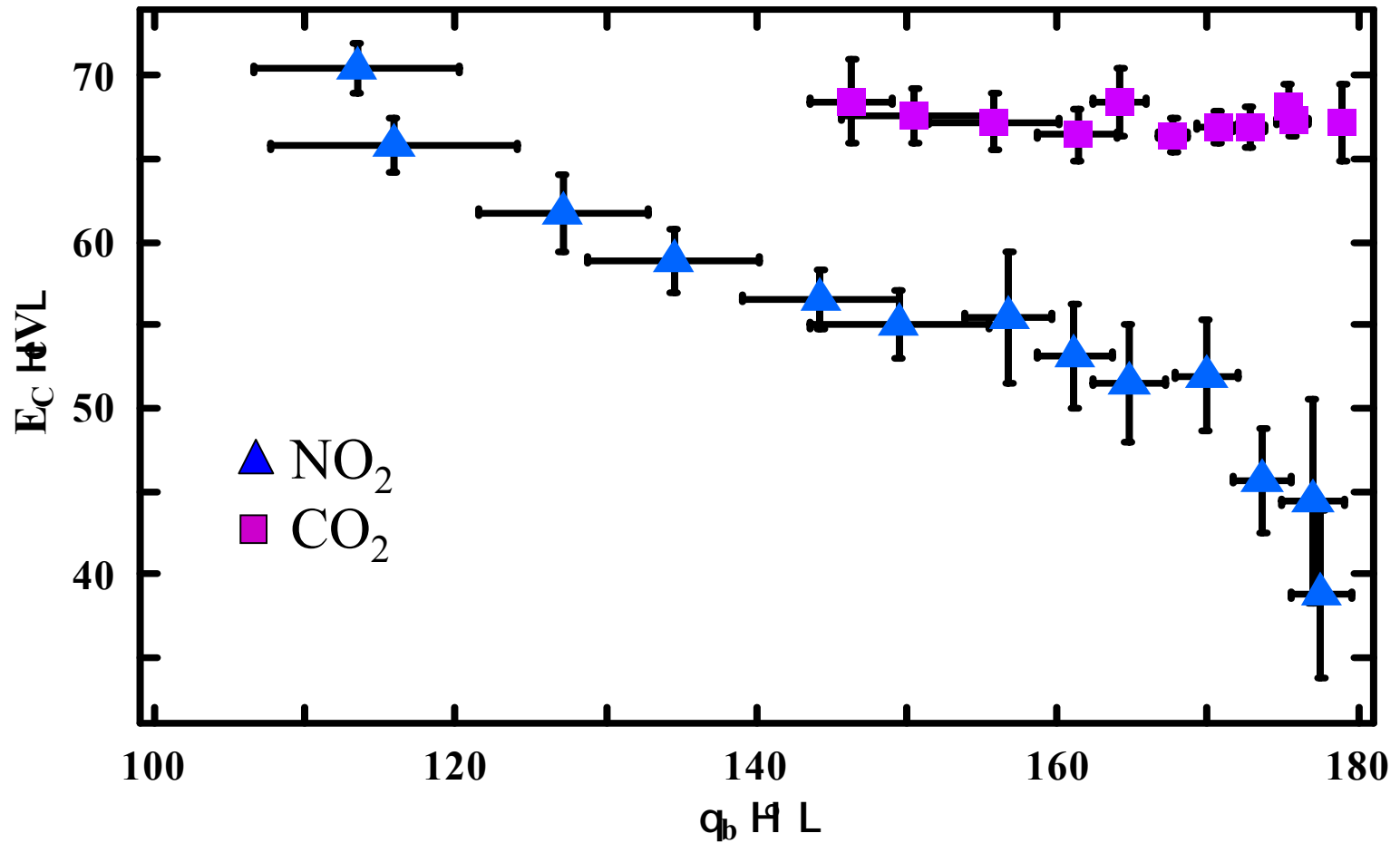
Image labeling: a graphical interface to  
correlation in multiparticle ejection  
dynamics

K. Zhao,<sup>1,2</sup> G. Zhang,<sup>3</sup> and W. T. Hill, III<sup>1,2</sup>

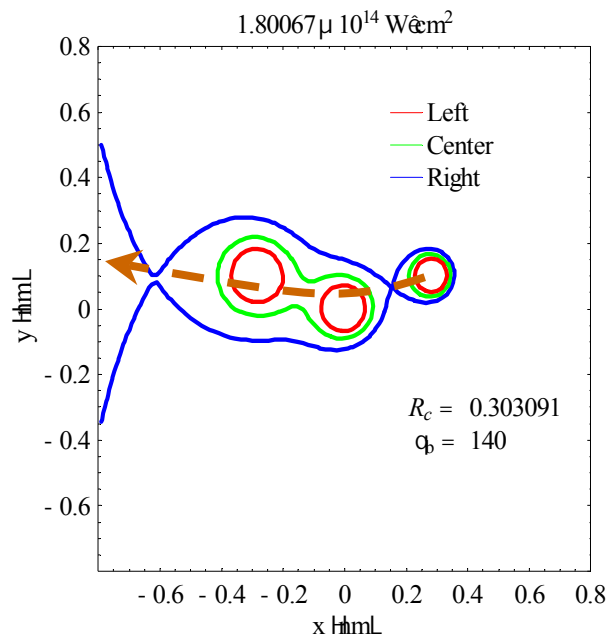




# Symmetric Coulomb Explosion

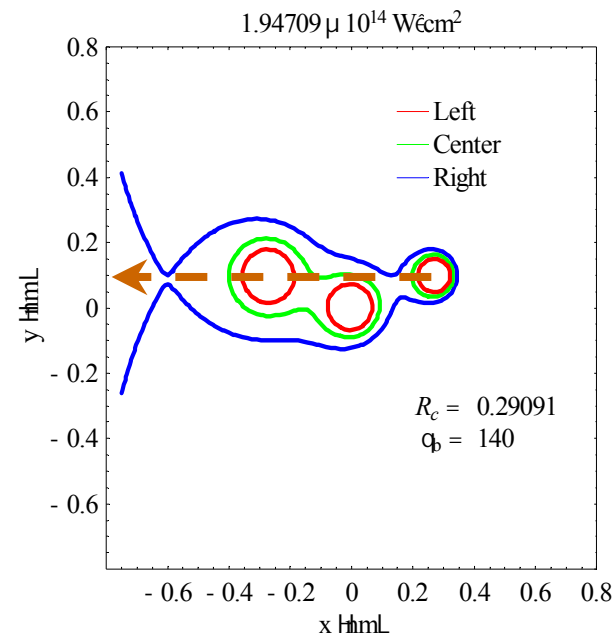


# Through Minimum



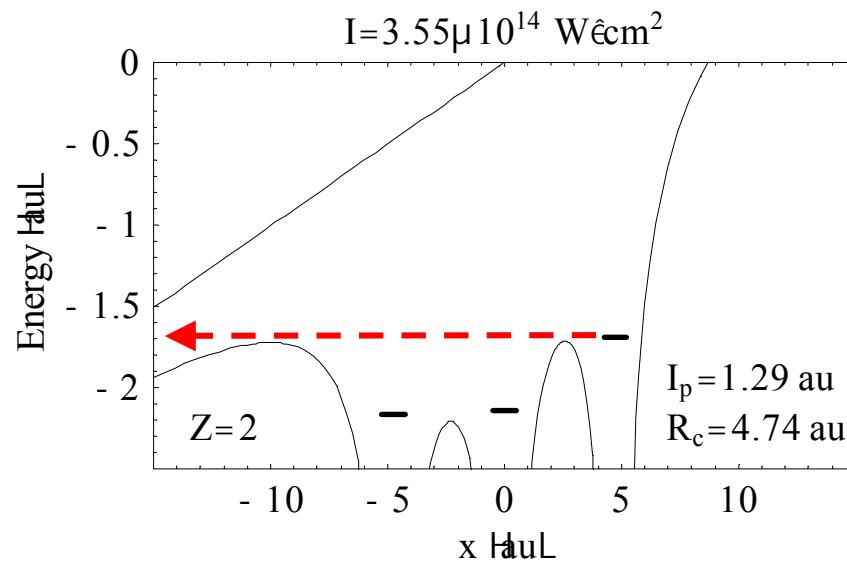
Over-the-Barrier  
Ionization

# Across O-O

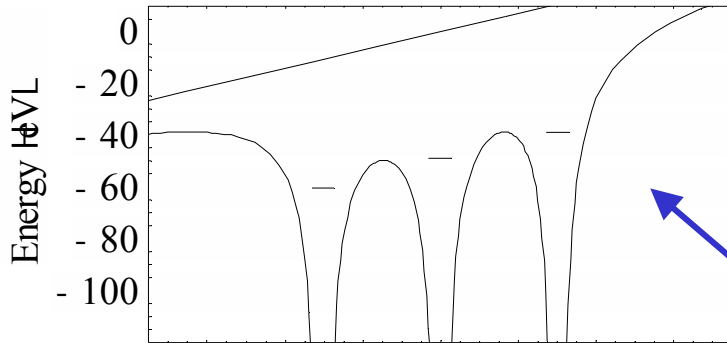


$$E_C = \frac{2Z^2}{R_C(\theta_b)} + \frac{Z^2}{2R_C(\theta_b)\sin(\theta_b/2)}$$

$$V = -\sum_{i=1}^3 \frac{Z_i}{\sqrt{(x-x_i)^2 + (y-y_i)^2 + S^2}} + Fx$$

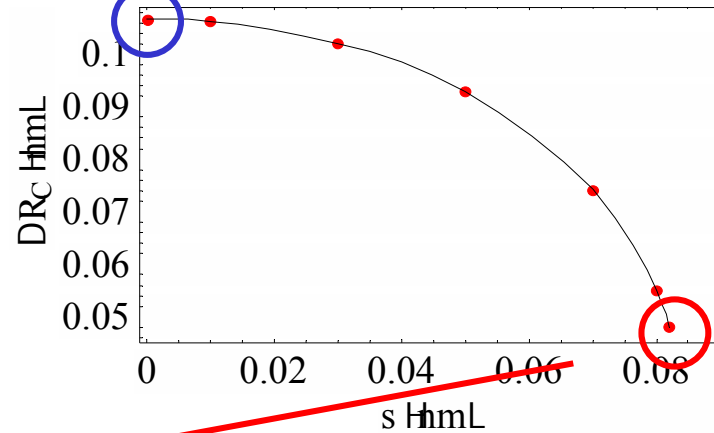
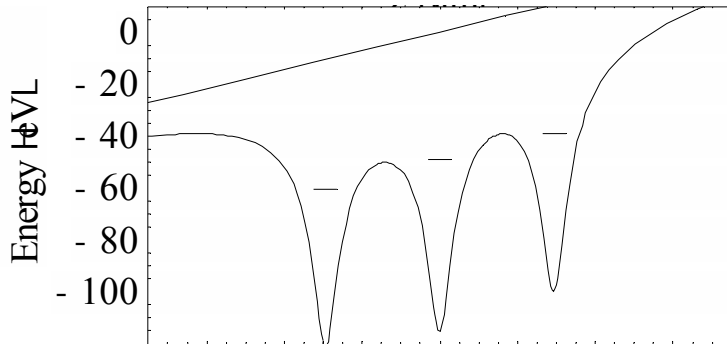


$I = 1.66 \times 10^{14}$ ,  $R = 0.302$  nm,  $s = 0.0001$

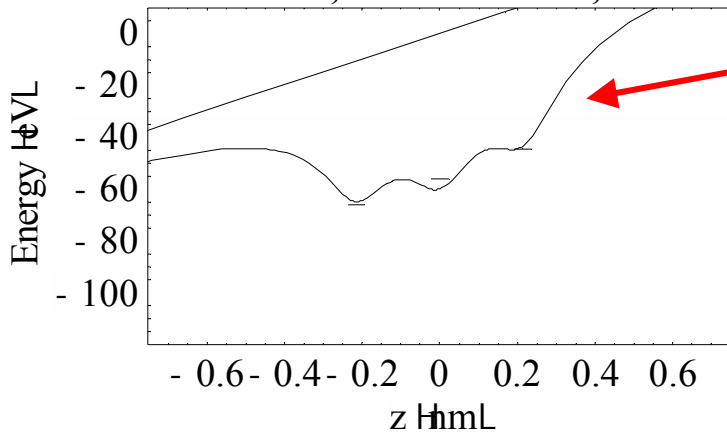


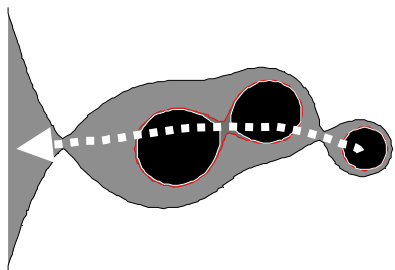
## Limits on Smoothing Factor

$I = 1.75 \times 10^{14}$  W/cm<sup>2</sup>,  $R = 0.294$  nm,  $s = 0.03$

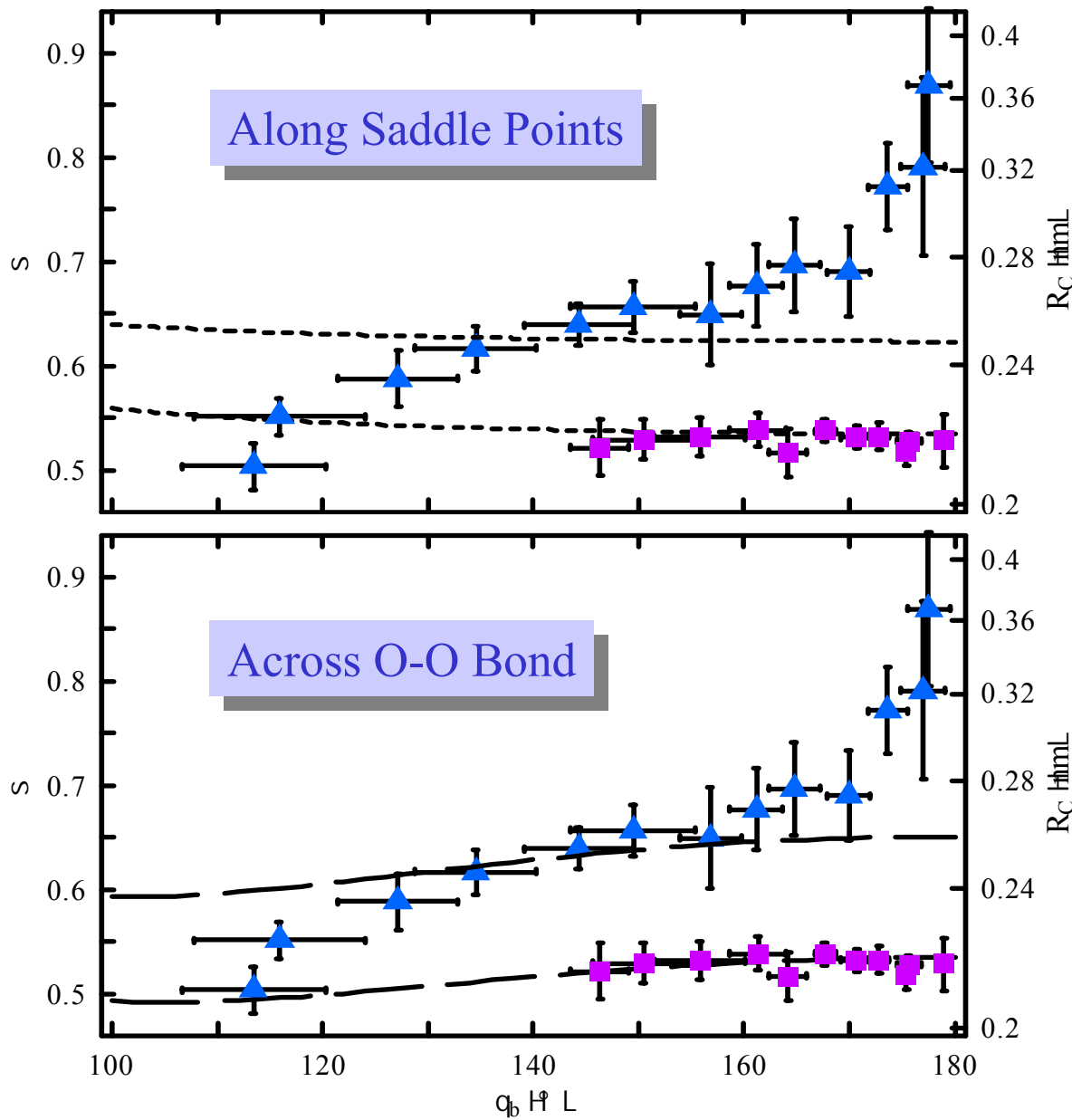
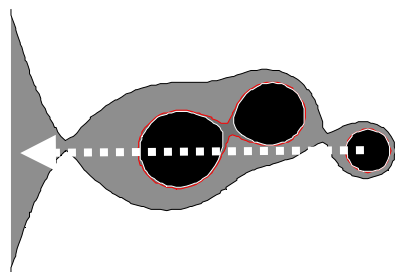


$I = 3.29 \times 10^{14}$  W/cm<sup>2</sup>,  $R = 0.216$  nm,  $s = 0.082$

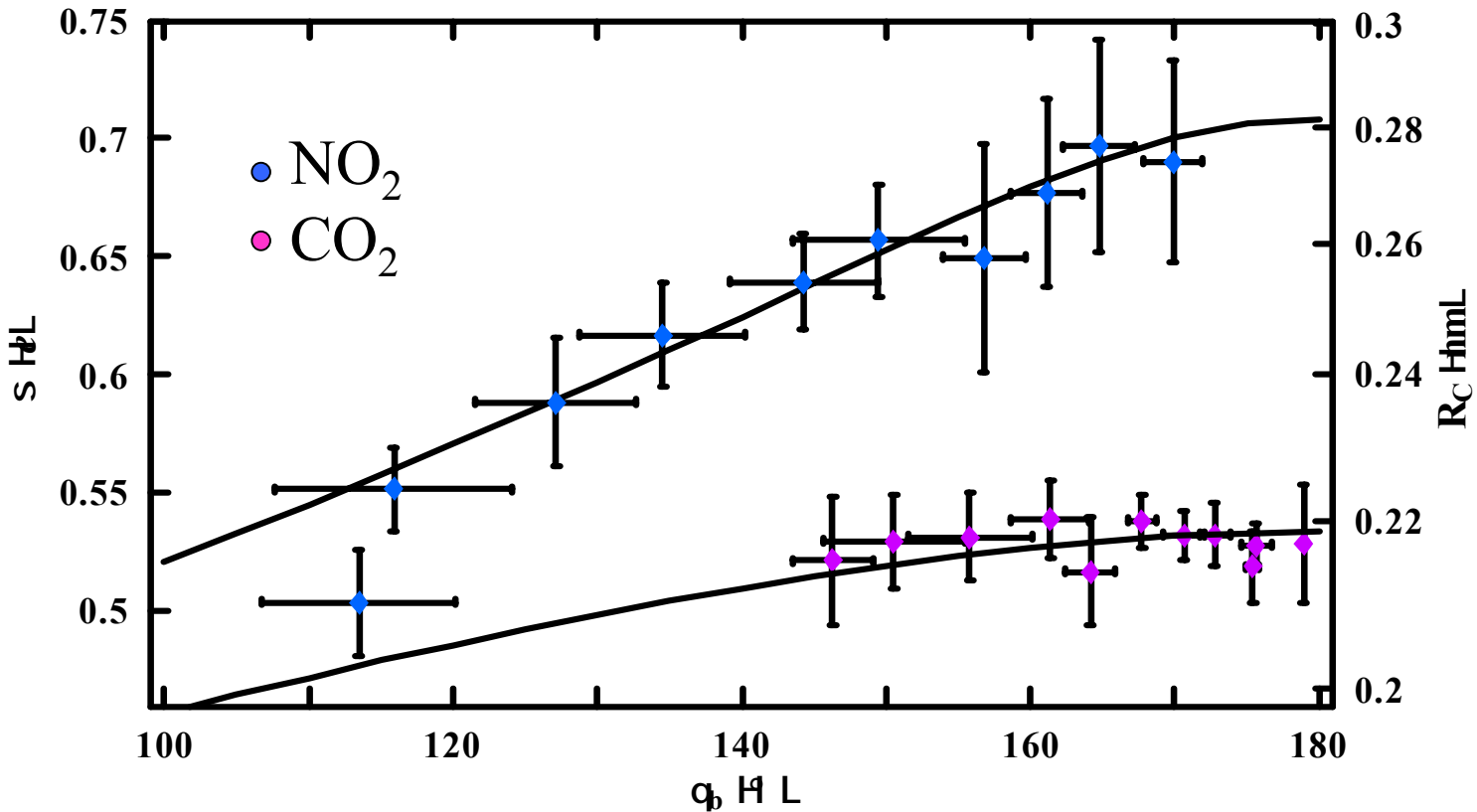




Enhanced  
Ionization  
at  $R_c$



# Symmetric Explosion vs. Bond Angle

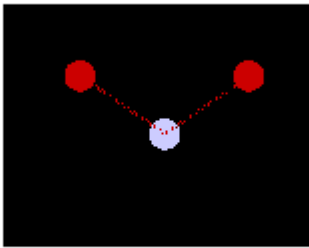


$$V = Z_{eff}^2(\theta_b) \left[ \frac{2}{R_{eq}} + \frac{1}{2R_{eq} \sin(\theta_b/2)} \right] = e^{-\frac{x^2}{x_0^2} - \frac{y^2}{y_0^2}}$$

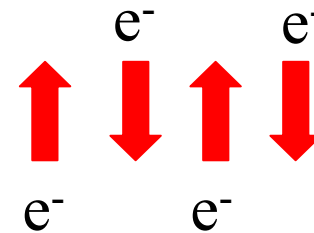
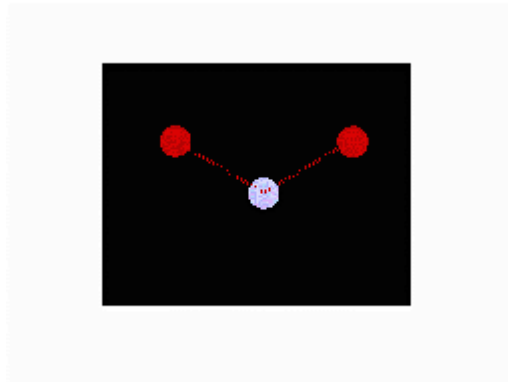
$$= Z^2 \left[ \frac{2}{R_{eq}} + \frac{1}{2R_{eq} \sin(\theta_b/2)} \right] - \sum_{i=1}^3 \frac{Z_i q_{el}}{\pi} \int_{Area} \frac{\rho(x, y) dx dy}{\sqrt{(x-x_i)^2 + (y-y_i)^2 + s^2}}$$

# Charge Density Parameters

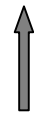
NO<sub>2</sub>



CO<sub>2</sub>



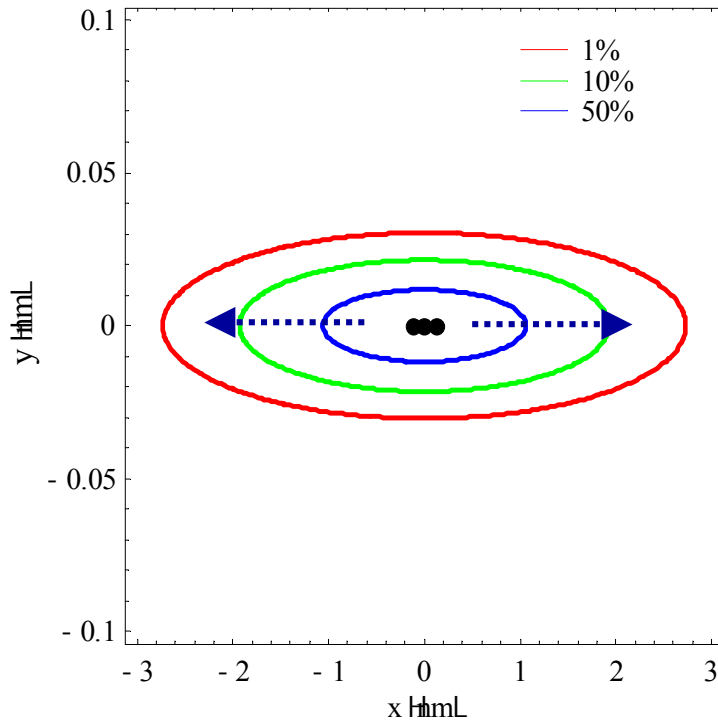
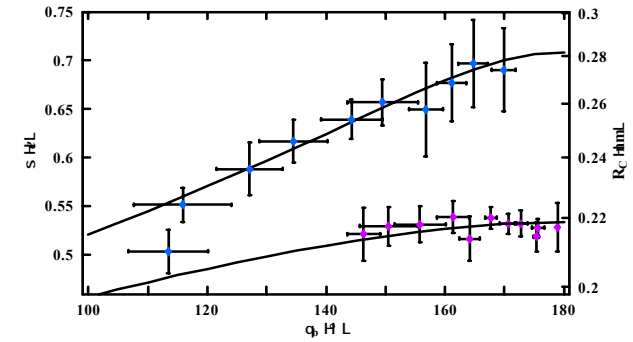
Resulting  
Charge  
Distribution



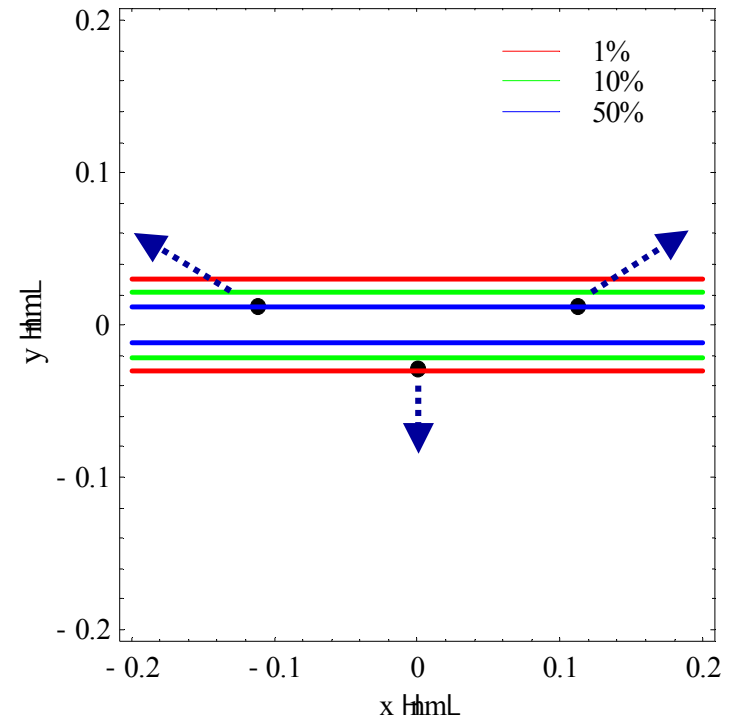
Wider Distribution

Larger  $y_0$

# Linear vs. Bent Explosions



CO<sub>2</sub> explosion range  
 $\theta_b = 145 - 180^\circ$



NO<sub>2</sub> explosion range  
 $\theta_b = 125 - 170^\circ$

# Conclusion

- The first example of where the  $R_c$  and screening models give different results!
- Screening explains the electron dynamics and the differences between linear and bent explosions.
- We have now recovered the ability to use ultrafast pulses to examine molecular structure.



# Acknowledgements

- Graduate Students
  - Harry Zhao
  - Vishal Chintawar
  - J. Zhu
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  - T. Colvin, Jr.
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  - F. Adameitz (France)
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