

```

[> # FOURIER SINE SERIES OF A SQUARE WAVE

[> # f(x) = 1 on (0,Pi); f(x) = -1 on (-Pi,0); f has period 2*Pi.

[> # First we need to calculate the Fourier coefficients.
> bn := (2/Pi)*Int(sin(n*x), x=0..Pi);

$$bn := \frac{2 \left( \int_0^{\pi} \sin(nx) dx \right)}{\pi} \quad (1)$$


[> value(%);

$$-\frac{2 (-1 + \cos(\pi n))}{\pi n} \quad (2)$$


[> # This is 0 unless n is odd.

[> # Note that, unlike the coefficients of the triangle wave, these
   decrease like 1/n, not 1/n^2.

[> bodd := k -> (4/Pi)*(1/(2*k+1));

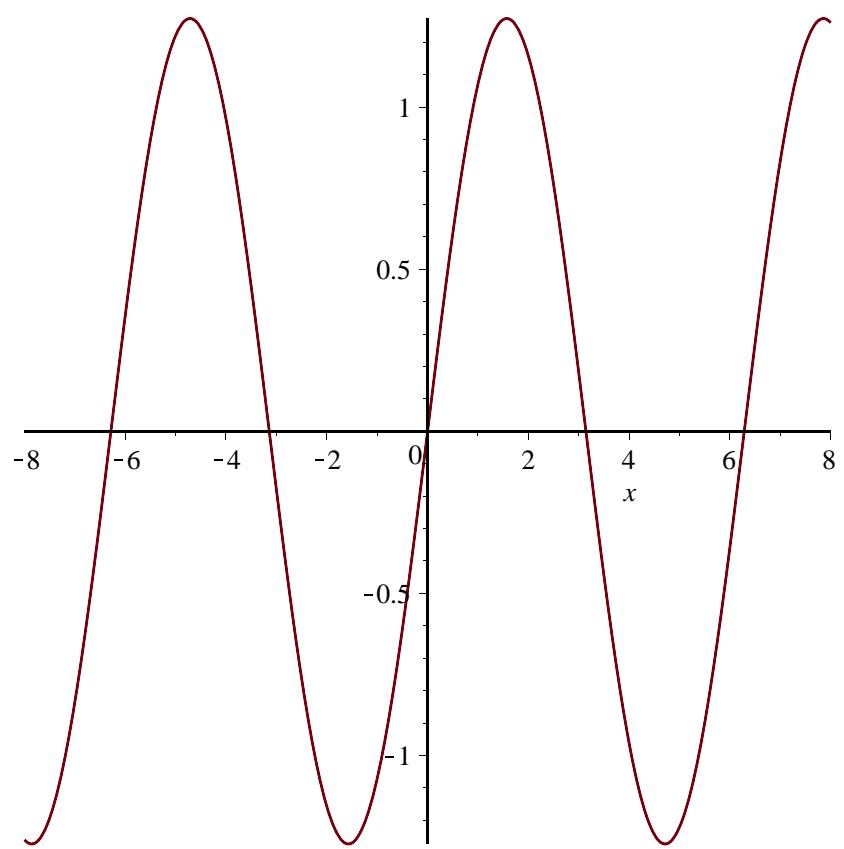
$$bodd := k \rightarrow \frac{4}{\pi (2k+1)} \quad (3)$$


[> partialsum := K -> sum(bodd(k)*sin((2*k+1)*x), k=0..K);

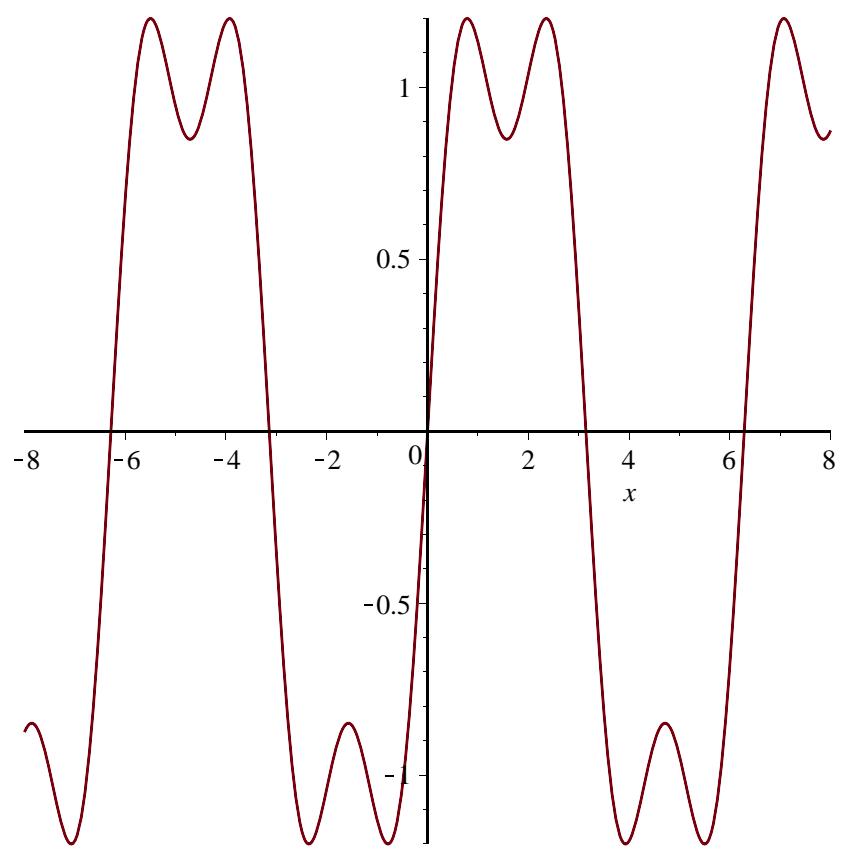
$$partialsum := K \rightarrow \sum_{k=0}^K bodd(k) \sin((2k+1)x) \quad (4)$$


[> plot(partialsum(0), x=-8..8);

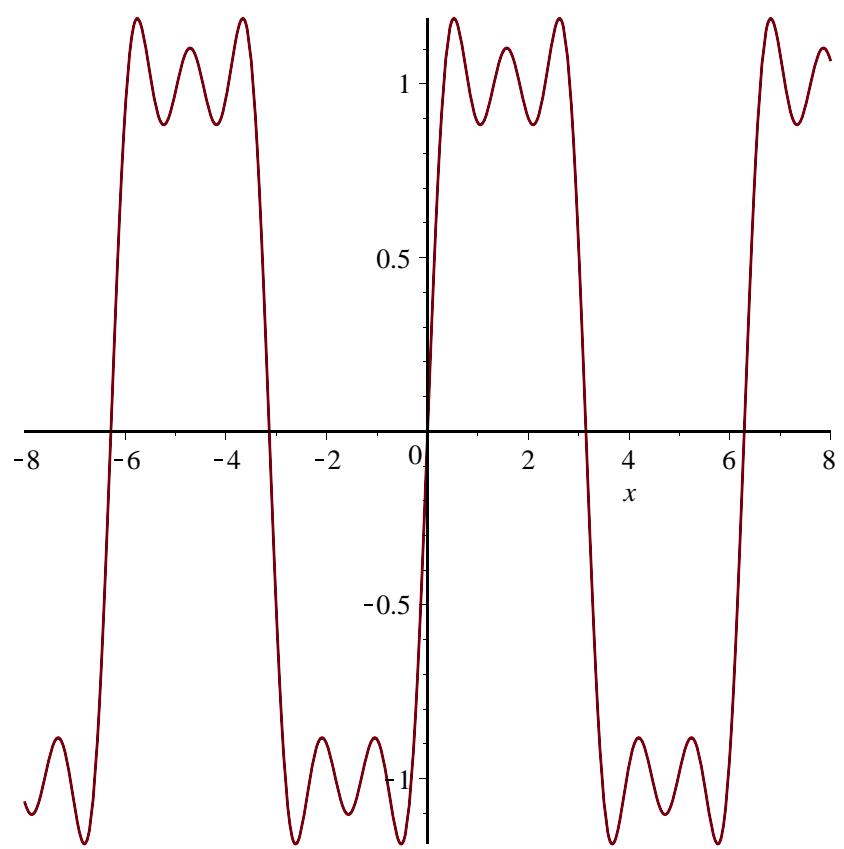
```



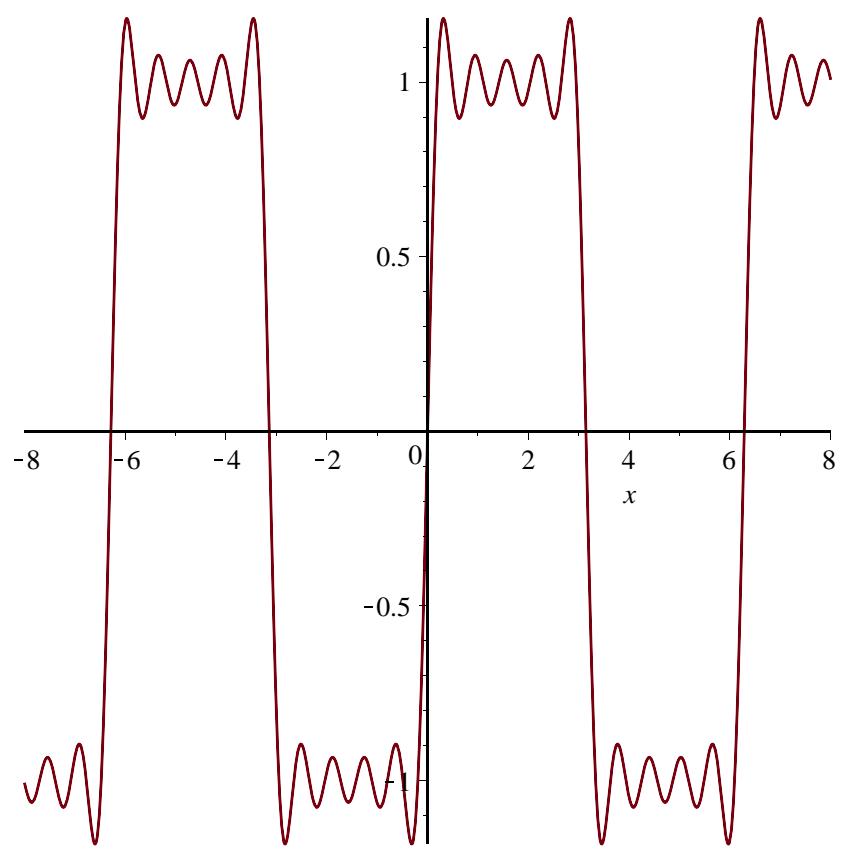
```
> plot(partialsum(1), x=-8..8);
```



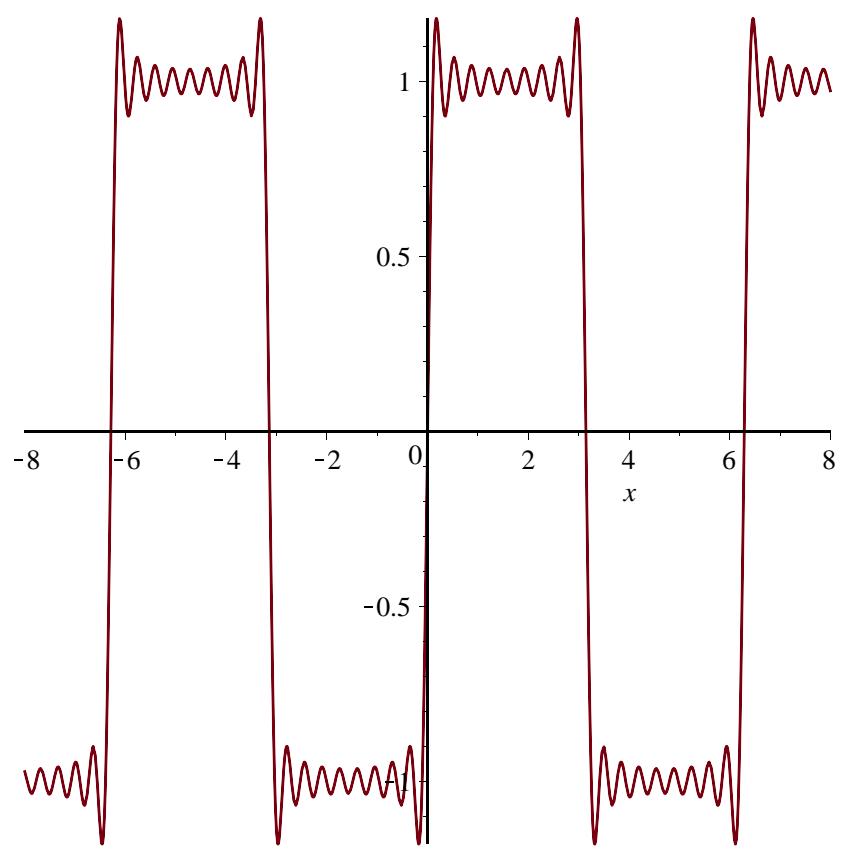
```
> plot(partialsum(2), x=-8..8);
```



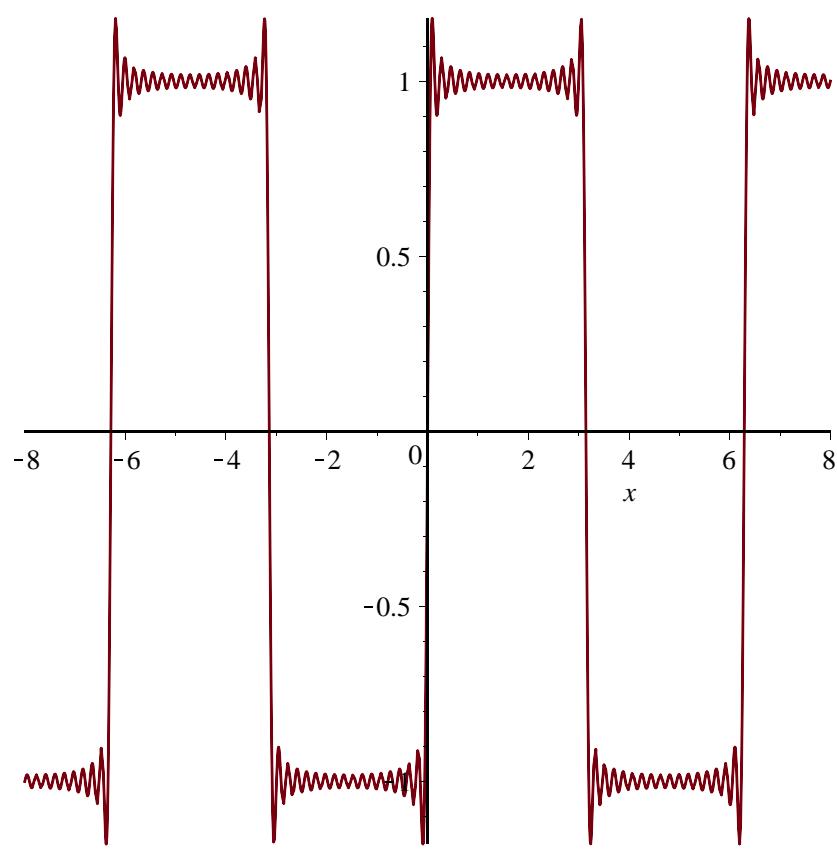
```
> plot(partialsum(4), x=-8..8);
```



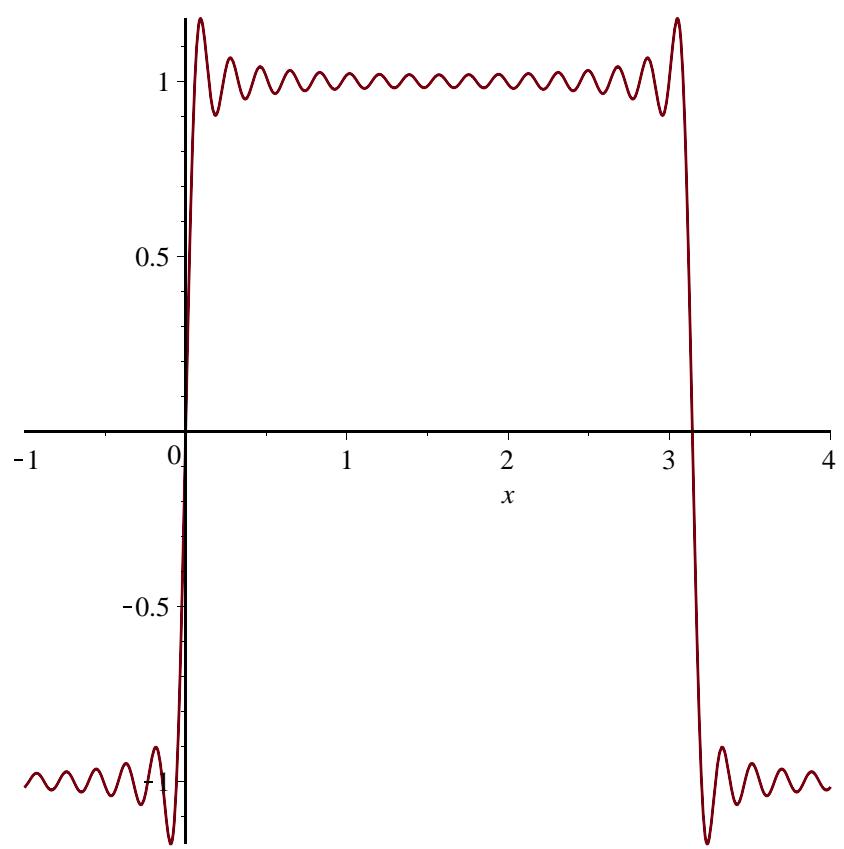
```
> plot(partialsum(8), x=-8..8);
```



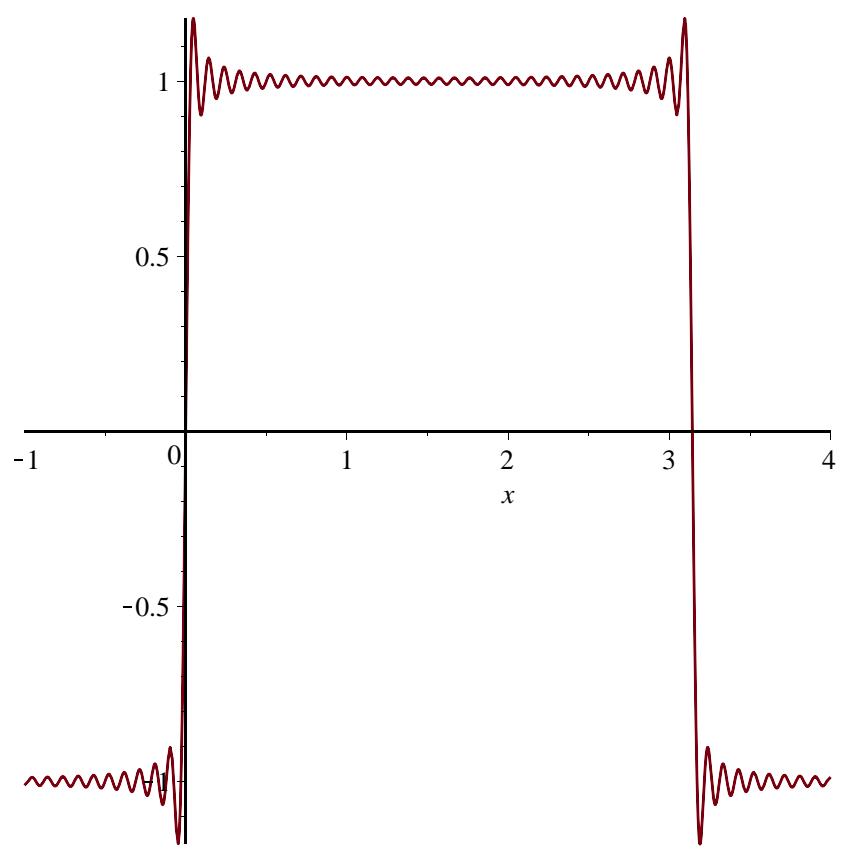
```
> plot(partialsum(16), x=-8..8);
```



```
> # Let's look up close.  
> plot(partialsum(16), x=-1..4);
```



```
> plot(partialsum(32), x=-1..4);
```



```
> plot(partialsum(64), x=-1..4);
```

