

Lecture Notes¹

ECON 323

Microeconomic Theory

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¹These lecture notes are prepared for my teaching and the convenience of my students in class. Please do not distribute them.

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Part I

Preliminaries and the Basics of Demand and Supply

Part 1 surveys the scope of economics and microeconomics, introduces basic concepts and methodologies, and discusses the market model of demand and supply.

Chapter 1

Economics Review and Math Review

1.1 Economics Review

Learn and teaching economics can be challenging because students are often come to class with a keen interest in learning about the economy, while instructors need to focus on teaching the theories and models that underpin the field. This inherent tension arises from the fact that there is no single, tangible “economy” to study; rather, economics is based on a set of theories and models that should be judged by their usefulness, much like tools, rather than a single fact. This can make it difficult to teach and learn effectively.

Moreover, what is commonly thought of as “facts” in economics are actually predictive statements integrated into theoretical models, particularly in microeconomic theory. Understanding these technical concepts and logical reasoning is crucial for mastering the subject, further adding to the challenge of learning and teaching economics.

1.1.1 The Themes of Economics

Economics studies economic phenomena and the economic behavior of individual agents—consumers, workers, firms, government, and other economic units—as well as how they make *trade-off choices* so that limited resources are allocated among competing uses.

Due to the *fundamental inconsistency and conflict* between **limited resources** and individuals' **unlimited desires** (i.e., wants), economics is created to study trade-off choices in resource allocation to make the best use of limited resources and maximize the satisfaction of individuals' needs.

Typical Resources

The three typical resources are:

- **Labor:** includes the mental and physical skills provided by workers, e.g., teachers, managers, dancers, and steel workers.
- **Capital:** includes man-made aids to production, e.g., machinery, buildings, and tools.
- **Land:** includes all natural resources, e.g., soil, forests, minerals, and water.

Two Most Objective Realities

Economic issues are difficult to solve due to the following two most objective realities:

1. **Self-interest behavior:** individuals (at whatever level: national, firm, household, or personal level) usually pursue their own interests under normal circumstances.
2. **Asymmetric information:** information among individuals is often asymmetric, and it is easy to pretend or lie.

Dealing with these two most basic objective realities and determining what kind of economic system, institution, incentive mechanism, and policy to use have become the core issues and themes in all areas of economics.

At the same time, economics often involves subjective value judgments, which makes economic issues even more difficult to solve since it is hard to reach a consensus.

Strong Externality in Application

Economics has strong externalities, either positive or negative, in practical applications. Poor applications of economic theories can have negative impacts on individuals and even an entire economy. Therefore, it is crucial to learn and understand economics correctly, especially the fundamental concepts of microeconomic theory.

Four Fundamental Questions that Economic Institutions Must Answer

Every economic institution must address the following four fundamental questions:

- i) What goods and services should be produced, and in what quantity? (Chapters 1-5)
- ii) How should these goods and services be produced? (Chapters 6-14)
- iii) For whom should they be produced, and how should they be distributed? (Welfare analysis: Chapters 9 and 11)
- iv) Who will make decisions, and by what process? (Economic system: Chapter 1)

Different economic institutional arrangements provide different answers to these questions. The effectiveness of an institutional arrangement in resolving these problems depends on how well it deals with *four* key words: **self-interests**, **information**, **incentives**, and **efficiency**.

Two Basic Economic Institutions in Practice:

There are two basic economic institutions used in practice:

(1) **Centrally planned (command) economic institution** (a *centralized* decision system):

- The government answers all four questions and monopolizes decision-making processes and all sectors.
- There is no unemployment, inflation, or free enterprise.

(2) **Market economy institution** (a *decentralized* decision system):

- Consumption and production decisions are made through market mechanisms.
- Consumers and producers are motivated by pursuing self-interests.

While a real-world economic system may fall somewhere in between these two extremes, the dominant position of one institution is critical. The centrally planned economic system's fundamental flaw is its inability to effectively resolve problems induced by information and incentives, leading to inefficiency in resource allocation.

In contrast, the market economic system has proven to be the only institution capable of achieving sustainable development and growth. It is the most effective way to reach cooperation and solve conflicts among individuals. Modern economics studies various economic phenomena and behaviors under the market economic environment by using analytical approaches, such as the demand and supply model. Therefore, this course focuses on the market system and how it works.

Methodology of Scientific Economic Analysis

Scientific economic analysis is essential for studying and solving complex economic and social problems. However, relying solely on theory or practice is insufficient. The "**three dimensions**" of *theoretical logic, practical*

knowledge, and historical perspective, and the "six natures" of scientificity, rigor, practicality, pertinency, foresight, and intellectual depth are crucial for conducting comprehensive analysis and producing sound conclusions.

The use of empirical quantitative analysis is necessary to confirm theoretical reasoning and logical deduction. Historical experience and lessons is also crucial for understanding fundamental laws, principles, human behavior patterns, and values. However, relying solely on historical experience may lead to outdated ideas and hinder economic and social development. Therefore, a balance between deductive reasoning and empirical verification is necessary.

By applying the "three dimensions and six natures" in reasoning, testing, and verification, decision-making can be both scientific and artistic, ensuring that conclusions or reform measures and plans meet the necessary criteria. This comprehensive approach is crucial for studying and solving major economic and social issues. Indeed, *all knowledge is presented as history, all science is exhibited as logic, and all judgment is understood in the sense of statistics.*

All in all, to become a good economist, you need to have an original, creative, and academic way of critical thinking.

1.1.2 The Themes of Microeconomics

Microeconomics is the core of economics and the theoretical foundation of all branches of economics and business science. It enables us to employ simplified assumptions for in-depth analyses of various aspects of the complex world in order to get some useful insights.

Microeconomics is the study of economic behaviors of individuals such as consumers, firms, workers and investors, as well as how markets are operated.

Macroeconomics, on the other hand, is the study of a national economy as a whole.

The core of microeconomics is **pricing**. It focuses on such questions

as: how pricing is determined? which factors affect pricing? Does a firm have market (pricing) power? How can an enterprise get the power of pricing? To answer these questions, it is necessary to study the demand, supply, characteristics and functions of the market, and pricing in all kinds of markets and economic environments. As a result, microeconomics is also known as the **price theory**.

Theories and Models

Like any science, *economics is concerned with the **explanations** of observed phenomena and **predictions** based on theories.*

Economic theory is a set of principles and ideas aimed at explaining how economies function and how they can be improved. It relies on a set of assumptions and analytical frameworks and in order to derive logical conclusions. Through the application of economic theory to real-world issues, economists can develop policies and solutions that promote economic growth, efficiency, and equity.

Economic model: A simplified, often *mathematical*, framework, which is based on economic theory and is designed to illustrate complex processes and make predictions.

When evaluating a theory, it is important to keep in mind that it is invariably imperfect and has limited success in making predictions. Why?

The two tenets of pragmatism/instrumentalism:

- 1) there are no complete facts, only theories (models);
- 2) theories are to be judged by their usefulness (just like tools).

How to model an economic phenomenon or issue is not only science but also art. Statistics and econometrics enable us to measure the *accuracy* of our predictions while historical experiences can be used to validate the accuracy of a theory's explanations and predictions.

Two Categories of Economic Theory

Economic theory can be further divided into two categories:

- **Benchmark theories:** These provide various benchmarks and reference systems to establish criteria for determining what is better and whether it represents the right direction.

When tackling a problem, it is necessary to first determine the direction and goals of improvement towards ideal situations such as **perfect competition**. By learning from the best and comparing with the best, we can continuously improve.

The first three parts (Chapters 2-9) of this course provide benchmark theories.

- **More realistic theories:** These aim to solve practical issues, so their assumptions are closer to reality and are usually modifications of the benchmark theory.

Major Economic Agents

- **Consumers:** They generate demand for goods and services via **utility maximization**.
- **Producers (firms):** They supply quantities of goods and services via **profit maximization** or **loss minimization**.

Three Basic Assumptions

1. **Self-interest behavior:** individuals are self-interested and pursue their personal goals.
2. **Rationality assumption:** market participants make rational (i.e., optimal) decisions.
3. **Scarcity of resources:** market participants confront scarce resources.

1.1.3 Positive versus Normative Analysis

*Positive questions deal with **explanation and prediction**, while normative questions deal with what **ought** to be:*

- **Positive statements:** Describing relationships of cause and effect. Tell us what is, was, or will be. Any disputes can be settled by looking at facts, e.g., “the sun will rise in the east tomorrow”.
- **Normative statements:** Opinions or value judgments; those tell us what should or ought to be. Disputes can **not** be settled by looking at facts, e.g., “It would be better to have low unemployment than to have low inflation.”

Positive analysis is central to microeconomics. Normative analysis is often supplemented by value judgments. When value judgments are involved, microeconomics cannot tell us what the best policy is. However, it can clarify the trade-offs and thereby help to illuminate the issues and sharpen the debate.

1.1.4 What is a Market?

Market: The market constitutes a modality of trade in which buyers and sellers conduct voluntary exchanges. It refers not only to the location where buyers and sellers conduct exchanges, but also to all forms of trading activity, such as auction and bargaining mechanisms.

It is crucial to keep in mind that any transaction in *the market has both buyers and sellers*. In other words, for a buyer of any good, there is a corresponding seller. The final outcome of the market process is determined by the rivalry of relative forces of sellers and buyers in the market.

An **industry** includes only sellers but not buyers.

Competitive versus Noncompetitive Markets

Perfectly competitive market: market with many buyers and sellers, so that no single buyer or seller has an impact on price. That is, *everyone takes the price as given*.

Although perfect competition is an ideal situation, many other markets are competitive enough to be treated as if they were perfectly competitive.

Other markets containing a small number of producers may still be treated as competitive for purposes of analysis. Some markets contain many producers but are **noncompetitive**; that is, *individual firms can jointly affect the price*.

In markets that are not perfectly competitive, different firms might charge different prices for the same product. The market prices of most goods will fluctuate over time, and for many goods the fluctuations can be rapid. This is particularly true for goods sold in competitive markets.

1.1.5 Real versus Nominal Prices

Inflation is an increase in the level of prices of the goods and services that households buy, which is measured as the *rate of change of those prices*.

These are two kinds of prices:

- **Nominal price**, also known as the **absolute price**: the price unadjusted for inflation.

For example, the nominal prices of a pound of butter was about \$0.87 in 1970, \$1.88 in 1980, \$1.99 in 1990, \$3.48 in 2015.

- **Real price**, also known as the **relative price**: the price adjusted for inflation.

For example, the price of the first-class ticket for Titanic in 1912 was \$7,500 which is the equivalent of roughly \$128,000 in 2016 dollars.

Moreover, we have:

- **Consumer Price Index (CPI):** measure of the aggregate price level.
 - Records the prices of a large market basket of goods purchased by a “typical” consumer over time. When the CPI is higher this year than last, it means there has been inflation since last year.
 - *Percent changes in CPI measure the rate of inflation.*
- **Producer Price Index (PPI):** measure of the aggregate price level for intermediate products and wholesale goods.

The Formula for Computing the Real Prices of a Good

The real prices of a good in year t in term of the base year dollars is calculated as follows:

$$\text{Real price in year } t = \frac{CPI_{\text{base year}}}{CPI_{\text{year } t}} \times \text{the nominal price in year } t.$$

Example 1.1 (Real price of butter) The nominal prices of a pound of butter was about \$0.87 in 1970, \$1.88 in 1980, \$1.99 in 1990, \$3.48 in 2015. The CPI was 38.8 in 1970 and rose to about 237 in 2015.

After correcting for inflation, was the price of butter more expensive in 2015 than in 1970?

To find out, let’s calculate the 2015 price \$3.48 of butter in terms of 1970 dollars.

$$\text{Real price in 2015} = \frac{CPI_{1970}}{CPI_{2015}} \times \text{the nominal price in 2015} = \frac{38.8}{237} \$3.48 = \$0.57.$$

The nominal price of butter went up by about 300 percent, while the CPI went up 511 percent. Relative to the aggregate price level, butter prices fell.

Example 1.2 (The price of eggs and the price of a college education) Table 1.1 in shows the nominal price of eggs, the normal cost of a college education, and the CPI.

	1970	1980	1990	2000	2016
CPI	38.8	82.4	130.7	172.2	241.7
Nominal Prices					
Eggs	\$.61	\$.84	\$1.01	\$.91	\$2.47
Education	\$1,784	\$3,499	\$7,602	\$12,922	\$25,694
Real Prices (\$1970)					
Eggs	\$.61	\$.40	\$.30	\$.21	\$.40
Education	\$1,784	\$1,624	\$2,239	\$2,912	\$4,125

Table 1.1: The real prices of eggs and a college education in 1970 dollars

Using the formula for computing the real price of a good, the real price of eggs for the year 1980 and a college education for the year 1990 in 1970 dollars can be found as follows:

$$\begin{aligned} \text{Real price of eggs in 1980} &= \frac{CPI_{1970}}{CPI_{1980}} \times \text{the nominal price in 1980} \\ &= \frac{38.8}{82.4} \$.84 = \$.4, \end{aligned}$$

$$\begin{aligned} \text{Real price of eggs in 1990} &= \frac{CPI_{1970}}{CPI_{1990}} \times \text{the nominal price in 1990} \\ &= \frac{38.8}{130.7} \$1.01 = \$.3, \end{aligned}$$

$$\begin{aligned} \text{Real price of education in 1980} &= \frac{CPI_{1970}}{CPI_{1980}} \times \text{the nominal price in 1980} \\ &= \frac{38.8}{82.4} \$3,499 = \$1,624, \end{aligned}$$

$$\begin{aligned} \text{Real price of education in 1990} &= \frac{CPI_{1970}}{CPI_{1990}} \times \text{the nominal price in 1990} \\ &= \frac{38.8}{130.7} \$77,603 = \$2,239, \end{aligned}$$

and so forth.

If we want to convert the CPI in 2000 into 100 and determine the real prices of eggs and a college education in 2000 dollars, we need to divide the CPI for each year by the CPI for 2000 and multiply that result by 100, and then use the new CPI numbers in Table 2.3 to find the real price of butter in 2000 dollars.

	1970	1980	1990	2000	2016
CPI	22.5	47.9	75.9	100	140.3

Table 1.2: Conversion of the CPI in 2000 dollars

Other examples on real prices are:

- In nominal terms, the minimum wage (currently \$7.25 per hour, Texas adopts the federal minimum wage rate) has increased steadily over the past 80 years. However, in real terms its 2020 level is around 33 percent lower than the minimum wage in 1970.
- The prices of both health care and college textbooks have been rising much faster than overall inflation. This is especially true of college textbook prices, which have increased about three times as fast as the CPI.

1.1.6 Why study microeconomics?

Microeconomic concepts are used by everyone to assist them in making choices as consumers and producers. The following examples show the numerous levels of microeconomic questions necessary in many decisions.

Example 1.3 (Corporate Decision Making) For instance, the Toyota Prius. In 1997, Toyota Motor Corporation introduced the Prius in Japan, and started selling it worldwide in 2001. The design and production of the Prius involved not only some impressive engineering (using hybrid power system), but a lot of economics as well. Many of the challenging questions can be answered by microeconomic theory:

- How strong in demand and how quickly will it grow? One must understand consumer preferences and trade-offs (Chapters 3-5).
- What are the production and costs of manufacturing? (Chapters 6-7)
- Given all costs of production, how many should be produced each year? (Chapters 8-9)
- Toyota had to develop pricing strategy and determine competitors reactions? (Chapters 10-11)
- Risk analysis. Uncertainty of future prices: gas, wages. (Chapter 5)
- Organizational decisions — integration of all divisions of production. (Chapters 12-13)
- Government regulation: Emissions standards (Chapters 2 and 9)

Example 1.4 (Public Policy Design) For instance, 1970 Clean Air Act imposed emissions standards and have become increasingly stringent. A number of important decisions have to be made when imposing emissions standards:

- What are the impacts on consumers?
- What are the impacts on producers?
- How should the standards be enforced?
- What are the benefits and costs?

1.2 Math Review

In this course, we focus on functions where independent and dependent variables are **real numbers**. The set of all real numbers is denoted by \mathcal{R} . A function of one variable, f , is a **mapping** from the **domain** X (a subset of \mathcal{R}) to the **range** \mathcal{R} , such that to every element in the domain, f assigns a unique element from the range. In short we write: $f : X \rightarrow \mathcal{R}$. Sometimes, we also write $y = f(x)$. In this case, we say x is the **independent variable** and y is the **dependent variable**.

A function of one variable can be visualized:

- The horizontal axis (often called x -axis) represents the domain.
- The vertical axis (or y -axis) represents the range.
- A generic point on the curve has a coordinate $(x, f(x))$.

1.2.1 Equations for straight lines

Equation for a straight line (or a linear function of one variable) takes the following form:

$$y = ax + b$$

where the constant a is the slope, which describes the rate at which function value changes with respect to the change of the independent variable x , and the constants b and $-\frac{b}{a}$ are respectively the y -axis and x -axis intercepts, which describe where the line intersects with the y -axis and x -axis, respectively.

Moreover, linear functions could exhibit the following geometrical features:

- positive slope ($a > 0$) - upward sloping;
- negative slope ($a < 0$) - downward sloping;
- larger absolute value in slope - steeper;

- smaller absolute value in slope - flatter;
- positive y -intercept - intersect with y -axis above x -axis;
- negative y -intercept - intersect with y -axis below x -axis;
- increase b - upward shift of the line;
- decrease b - downward shift of the line.

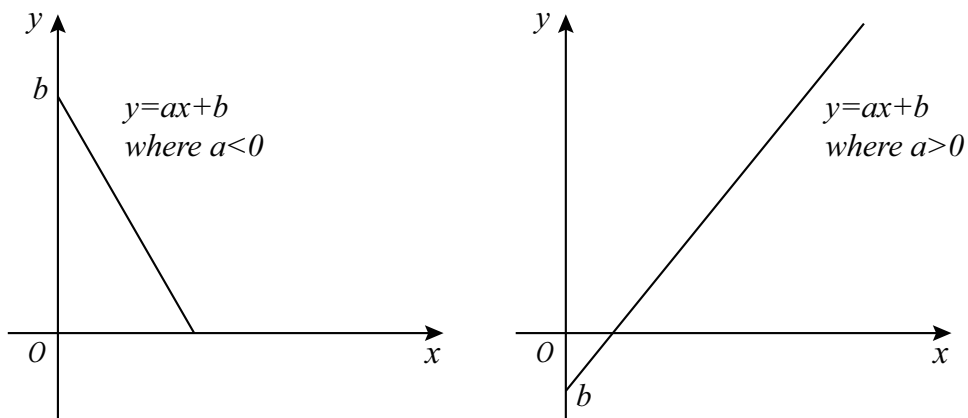


Figure 1.1 Linear functions with negative or positive slopes

1.2.2 Solve two equations with two unknowns

Example 1.5 $y = 60 - 3x$.

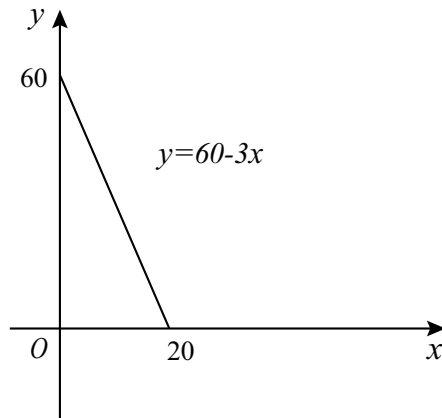


Figure 1.2 A numerical example of downward-sloping linear functions

The slope = -3 .

$x = 0 \Rightarrow y$ -axis intercept = 60.

$y = 0 \Rightarrow x$ -axis intercept $x = 20$.

Example 1.6 $y = 5 + 2x$

The slope = 2.

$x = 0 \Rightarrow y$ -axis intercept 5.

$y = 0 \Rightarrow x$ -axis intercept $x = -\frac{5}{2}$.

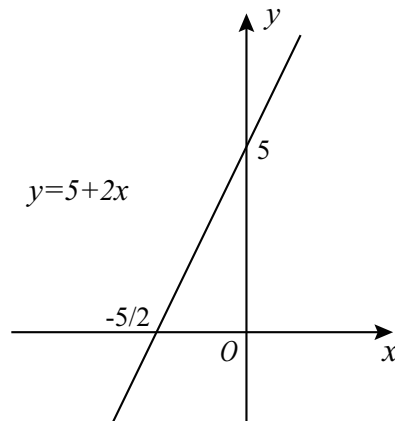


Figure 1.3 A numerical example of upward-sloping linear functions

Example 1.7 To find the intersection of these two lines, we have the following two approaches:

Graphically:

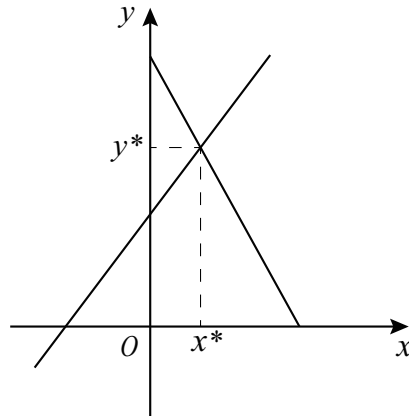


Figure 1.4 Interaction of two straight lines

Algebraically:

Equalizing $y = 60 - 3x$ and $y = 5 + 2x$, we have

$$60 - 3x = 5 + 2x$$

or

$$55 = 5x.$$

Thus, we get the solution for x :

$$x^* = 11.$$

Substituting $x^* = 11$ into either the equation, we have

$$y^* = 60 - 3x^* = 60 - 33 = 27$$

or

$$y^* = 5 + 2x^* = 5 + 22 = 27.$$

1.2.3 Derivatives

The **derivative** of a function f at x , written as $f'(x)$ or $\frac{df}{dx}(x)$, is defined as the **limit** of the difference quotient (if it exists):

$$f'(x) = \lim_{\Delta x \rightarrow 0} \frac{f(x + \Delta x) - f(x)}{\Delta x},$$

and called it is **differentiable** at x .

Thus, *the derivative of a function at x measures the rate at which the function value changes with respect to a change in the independent variable*, i.e., it is the slope of the tangent to the graph of f at point $(x, f(x))$.

Common rules of derivatives

- sum and difference rule:

$$(f \pm g)'(x) = f'(x) \pm g'(x).$$

- product rule:

$$(fg)'(x) = f'(x)g(x) + f(x)g'(x).$$

- quotient rule:

$$\left(\frac{f}{g}\right)'(x) = \frac{f'(x)g(x) - f(x)g'(x)}{g(x)^2}.$$

- power rule $f(x) = x^k$ (k is real number):

$$f'(x) = kx^{k-1}.$$

- natural logarithmic rule $f(x) = \ln x$:

$$f'(x) = \frac{1}{x}.$$

- exponential rule $f(x) = e^x$ ($e \cong 2.71828 \dots$ is the base of natural logarithm):

$$f'(x) = e^x.$$

- linearity rule (k is real number):

$$(kf)'(x) = kf'(x).$$

- chain rule:

$$(g(f))'(x) = g'(f(x))f'(x).$$

1.2.4 Functions of multiple variables

A function of k variables is a **mapping** $f : X_1 \times X_2 \cdots X_k \rightarrow \mathcal{R}$, where X_i for $i = 1, 2, \dots, k$ are subsets of \mathcal{R} .

The partial derivative of z with respect to x_i , denoted by $\frac{\partial z}{\partial x_i}$, is defined as:

$$\frac{\partial z}{\partial x_i} = \lim_{\Delta x_i \rightarrow 0} \frac{\Delta z}{\Delta x_i} = \frac{f(x_1, x_2, \dots, x_{i-1}, x_i + \Delta x_i, x_i, \dots, x_n) - f(x_1, x_2, \dots, x_n)}{\Delta x_i}.$$

Computation is similar to compute a derivative. When computing $\frac{\partial z}{\partial x_i}$, we should view all other variables as constant and view x_i as a variable, compute the derivative (with respect to x_i).

We mostly focus on **functions of two variables**. In a function of two variables $z = f(x, y)$, x and y are independent variables and z is a dependent variable.

Chapter 2

Market Analysis

Demand-supply analysis is a fundamental and powerful tool that can be applied to a wide variety of interesting and important problems. To name just a few:

- Understanding and predicting how changing world economic conditions affect market price and production;
- Evaluating the impact of government price controls, minimum wages, price supports, and production incentives;
- Determining how taxes, subsidies, tariffs, and import quotas affect consumers and producers.

2.1 Demand

Demand [$D(p)$]: A schedule which shows the relationship between the quantity of a good that consumers are **willing** and **able** to buy and the price of the good, **ceteris paribus**.

Here,

- *willingness* to purchase reflects tastes (preferences) of consumers;
- *ability* to purchase depends upon income;

- *ceteris paribus*: all other things remaining constant (preferences, income, prices of other goods, environmental conditions, expectations, size of markets).

Thus, the demand curve, labeled D , reveals how the quantity of a good demanded by consumers depends on its price.

Market demand: The sum of single individual demands.

price of calculators (p)	quantity demanded (millions) of calculators per year
\$20	2
\$15	5
\$10	10
\$5	15
\$1	25

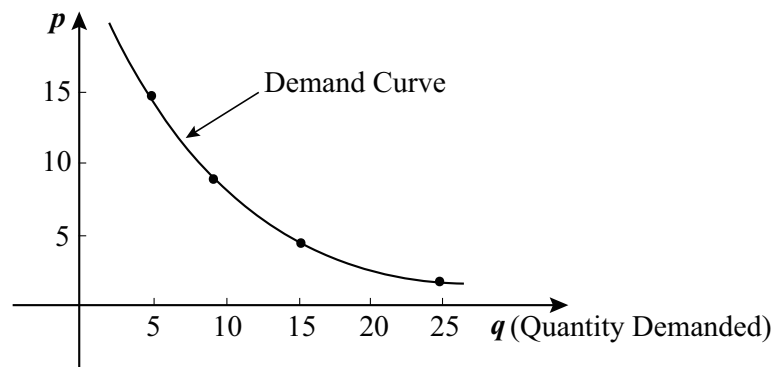


Figure 2.1 The downward-sloping demand curve

Law of Demand: An *inverse* relationship between price and quantity demanded. That is, the lower the price, the larger will be the quantity demanded, and vice versa.

A linear demand function can be denoted as $D(p) = ap + b$. An inverse relationship between quantity and price implies $a < 0$.

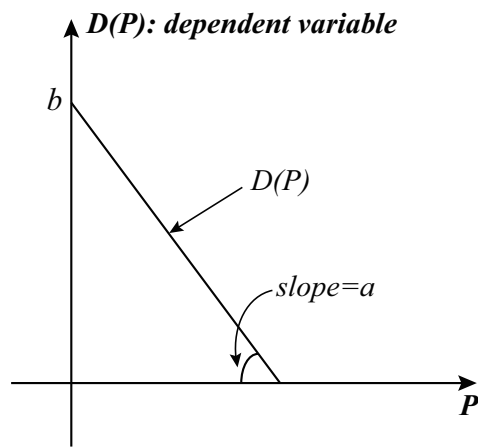


Figure 2.2 A linear demand function

However, *traditionally, economists reverse the axes when graphing:*

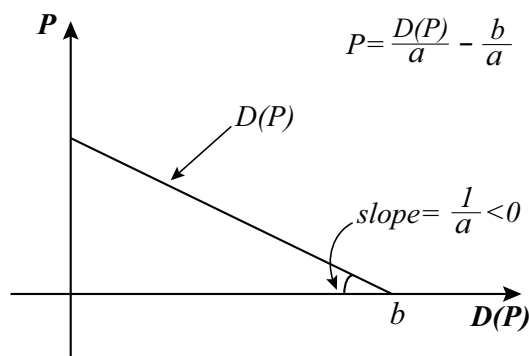


Figure 2.3 A linear demand function with y -axis representing price

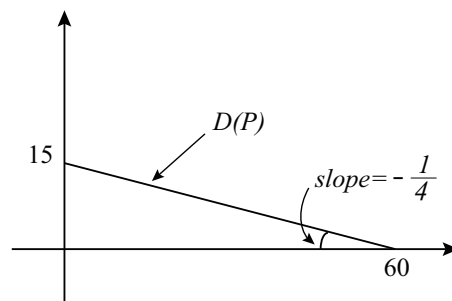


Figure 2.4 A numerical example of linear demand function

Example 2.1 $D(p) = 60 - 4p$. Then $p = -1/4D(p) + 15$ with slope $= -\frac{1}{4}$.

Above, we have imposed the assumption that all other influences on demand are held constant as the price changes. Price change is the only cause of a change in quantity demanded (movement along demand curve).

Changes in Quantity Demanded versus Changes in Demand

(1) Change in quantity demanded:

- i) caused by a change in price;
- ii) represented by a movement along the demand curve.

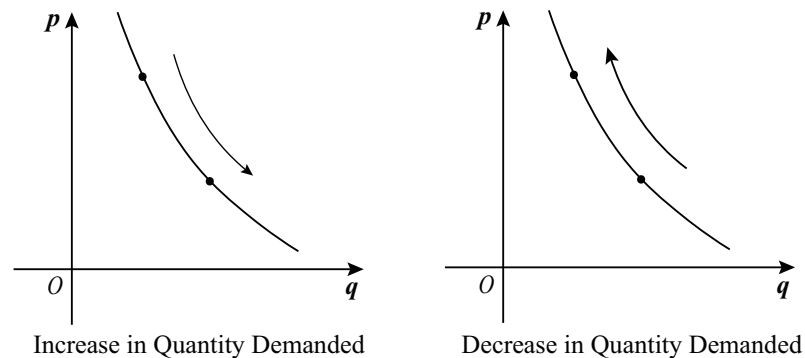


Figure 2.5 Change in quantity demanded: movement along the demand curve

(2) Change in demand:

- i) caused by a change in something other than price;
- ii) represented by a shift of the demand curve.

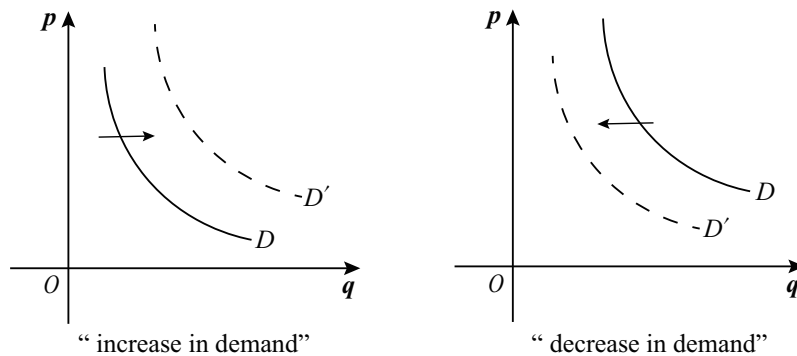


Figure 2.6 Change in demand: the shift of demand curves

Factors causing a change in demand (i.e., factors which shift the demand curve):

- a) Size of market as city grows. E.g., Better marketing \Rightarrow increase in the number of consumers \Rightarrow increase in demand as depicted in Figure 2.7.

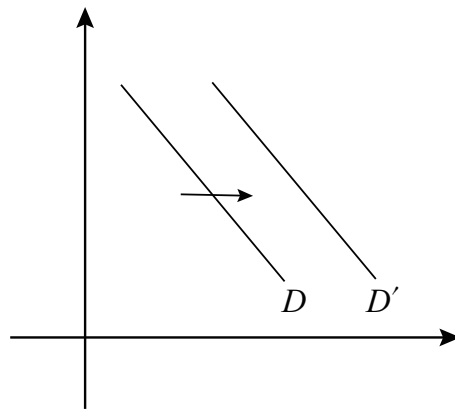


Figure 2.7 Demand curve shifts to the right as size of market grows

- b) Income.

- **Normal goods:** As income rises, demand rises; most goods are “normal” goods as also depicted in Figure 2.7.

- **Inferior goods:** As income rises, demand falls; e.g., potatoes, bread (poverty goods) as depicted in Figure 2.8.

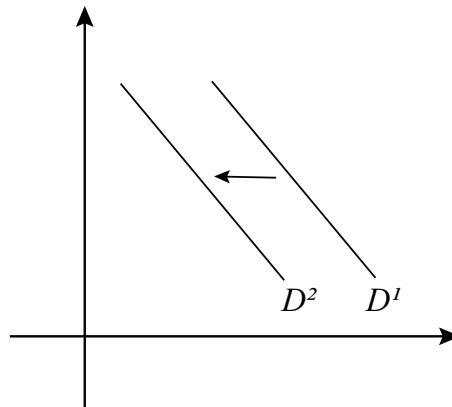


Figure 2.8 Demand curve for inferior goods shifts towards the left as income rises

c) Prices of related goods.

- **substitute goods** (also known as the “**competing goods**”): Two goods for which an increase in the price of one leads to an increase in the demand of the other, e.g., beef and pork as depicted in Figure 2.9.

— Price of beef rises \Rightarrow the substitution of pork for beef \Rightarrow demand for pork rises. Consequently, the *demand curve for pork shifts to the right*.

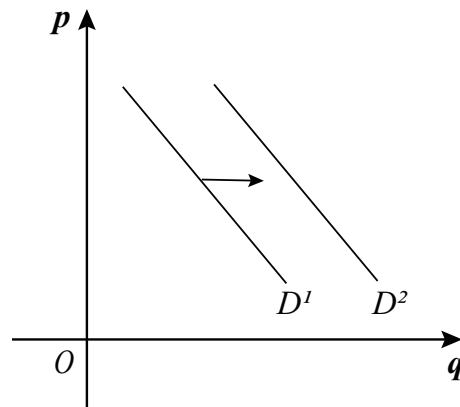


Figure 2.9 Demand curve for pork shifts towards the right as the price of beef increases

- **complementary goods:** Two goods for which an increase in the price of one leads to a decrease in the demand of the other, e.g., hamburger and buns as depicted in Figure 2.10.
—The price of hamburgers falls \Rightarrow quantity demanded rises \Rightarrow demand for buns rises.

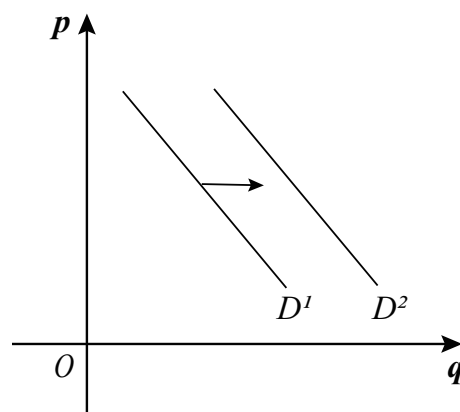


Figure 2.10 Demand curve for buns shifts towards the right as the price of hamburgers increases

d) Tastes (preferences)

e.g., cigarette causes cancer \Rightarrow demand for cigarette falls as depicted in Figure 2.11.

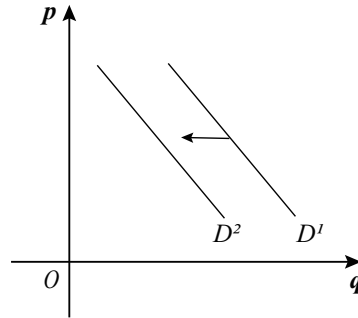


Figure 2.11 Demand curve for cigarette shifts towards the left as people know cigarette causes cancer

e) Expectations

e.g., paper towels go on sale next week \Rightarrow people will buy them next week \Rightarrow demand of this week falls as depicted in Figure 2.12.

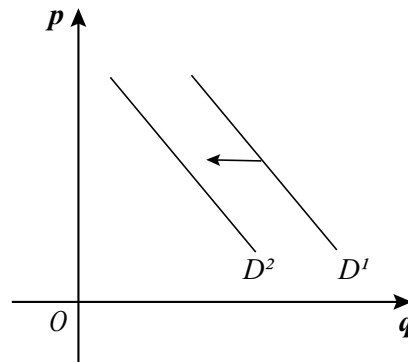


Figure 2.12 Demand curve for paper towels in this week shifts towards the left

f) Environmental conditions

e.g., weather conditions affect demand for air conditioners, ice cream, and winter coats.

2.2 Supply

Supply [$S(p)$]: a schedule which shows the relationship between the quantity of a good that producers are **willing** and **able** to sell and the price of the good, **ceteris paribus**.

The supply curve, labeled S , shows how the quantity of a good offered for sale changes as the price of the good changes. The supply curve is upward sloping: The higher the price, the more firms are able and willing to produce and sell.

Market supply: The sum of the supplies of individual firms.

price of calculators	quantity supplied (millions) of calculators per year
\$20	600
\$10	300
\$2	100

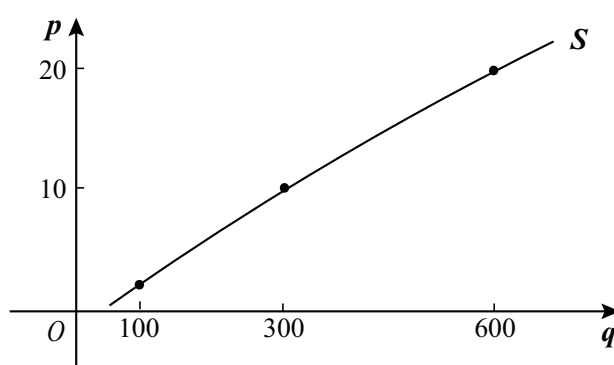


Figure 2.13 A supply curve

Law of Supply: There is a **direct** (i.e., positive) relationship between the price of a good and the quantity supplied. That is, all else being equal, the higher the price, the larger the quantity supplied, and vice versa.

The linear supply function is:

$$S(p) = ap + b,$$

where a and b are constants. Since there is a direct relationship between price and quantity supplied, $a > 0$.

Example 2.2 $S(p) = -10 + 6p$. Then, $p = \frac{1}{6}S(p) + \frac{5}{3}$ with slope $= \frac{1}{6}$.

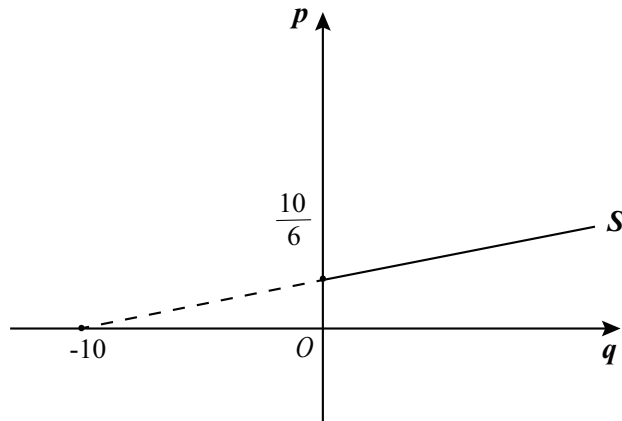


Figure 2.14 A numerical example of supply curve

Why is there a direct relationship between price and quantity supplied?

This can be explained by the concept of *Substitution or Expansion in Production*. As the price of a good rises, producers will find it more profitable to allocate more resources into the production of this relatively high priced good, and may even shift away from the production of relatively low priced goods. Alternatively, the producers have incentives to hire extra resources.

Changes in Quantity Supplied versus Changes in Supply

(1) **Change in quantity supplied:**

- i) caused by a change in price;
- ii) represented by a movement along the supply curve.

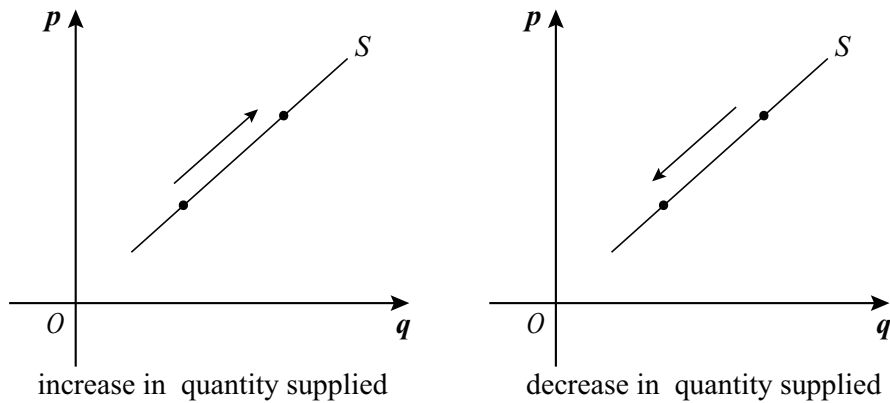


Figure 2.15 Change in quantity supplied: movement along supply curve

(2) **Change in supply:**

- i) caused by a change in something other than price;
- ii) represented by a shift of the supply curve.

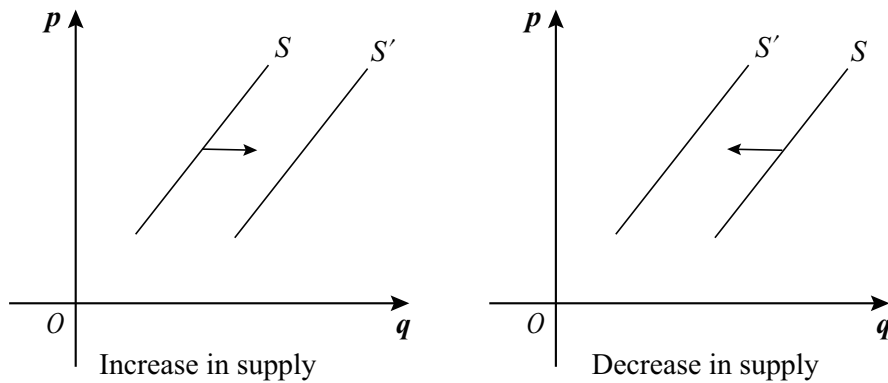


Figure 2.16 Change in supply: shifts in supply curve

Factors Causing a Change in Supply (factors which shift the supply curve):

- a) number of firms
- b) prices of related goods

- c) technology
- d) expectations
- e) environmental conditions

Examples of change in supply:

- i) prices of resources: increase in wage \Rightarrow increase in costs of production \Rightarrow decrease in supply.
- ii) advancement in technology \Rightarrow decrease in costs of production \Rightarrow increase in supply.

2.3 Determination of Equilibrium Price and Quantity

Notations:

- q^d is the quantity demanded of a commodity;
- q^s is the quantity supplied of a commodity;
- p is the price of the commodity;

Equilibrium price (also known as the **market-clearing price**), denoted by p^e , is established at the price where quantity demanded equals quantity supplied of the commodity.

Three relevant concepts:

- **Market mechanism:** The tendency in a free market for the price to change until the market clears.
- **Surplus:** A situation in which the quantity supplied exceeds the quantity demanded at a given price.
- **Shortage:** A situation in which the quantity demanded exceeds the quantity supplied at a given price.

When can we use the supply-demand model?

- The assumption in this model is that at any given price, a given quantity will be produced and sold.
- This assumption makes sense only if a market is at least **roughly competitive**, which means that both sellers and buyers should have **little market power** — i.e., little ability **individually** to affect the market price.
- Suppose instead that supply were controlled by a single producer — a monopolist. If the demand curve shifts in a particular way, it may be in the monopolist's interest to keep the quantity fixed but change the price, or to keep the price fixed and change the quantity.

Example 2.3 (Example on Calculator (continued)) From Table 2.1, we can know the equilibrium price is $p^e = \$10$. We say that " p^e clears the market".

The equilibrium quantity: $q^e = 3000$ ($q^e = q^s = q^d$).

p	q^d (millions)	q^s (millions)	surplus (+) or shortage (-)
\$20	700	6000	+5300
\$10	3000	3000	0
\$2	6500	1000	-5500

Table 2.1: Market equilibrium of calculators.

The market equilibrium can be also visualized as depicted in Figure 2.17.

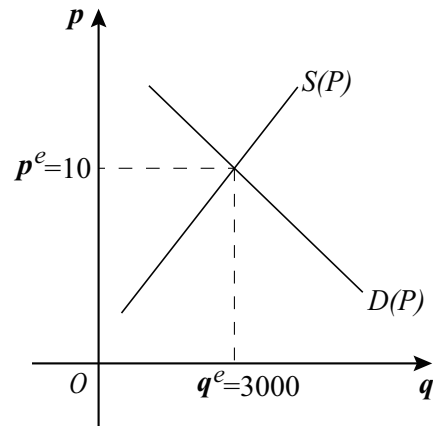


Figure 2.17 The determination of equilibrium price and quantity

Example 2.4 Find the market equilibrium price p^e and equilibrium quantity q^e of the following demand and supply.

$$D(p) = 80 - 4p,$$

$$S(p) = -10 + 6p.$$

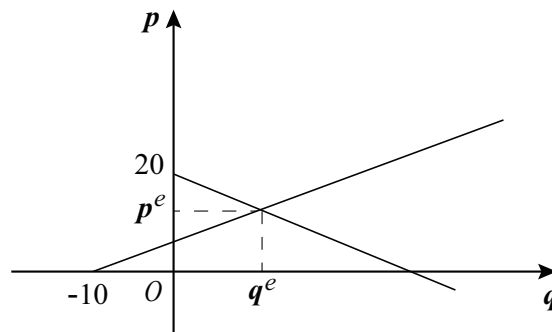


Figure 2.18 Finding market equilibrium: a numerical example

$p = 0$ implies $D(0) = 80$ and $S(0) = -10$. $q^d = 0$ implies $p = 20$, and $q^s = 0$ implies $p = 10/6 = 5/3$. We then can draw the demand curve and

supply curve as depicted in Figure 2.18, giving us the market equilibrium price p^e and equilibrium quantity q^e .

Algebraically, equaling $D(p^e) = S(p^e)$, we have

$$80 - 4p^e = -10 + 6p^e,$$

and thus

$$90 = 10p^e,$$

which yields $p^e = 9$.

Substituting $p^e = 9$ into either the equation, we have

$$q^e = D(p^e) = S(p^e) = 80 - 4 \times 9 = 44.$$

2.4 Market Adjustment

The market adjustment mechanism works as follows:

- Suppose $p > p^e$. Then $q^s > q^d$, yielding **surplus**. Producers compete to extract the surplus by price cutting. Price falls implies that q^s falls and q^d rises. Eventually $q^s = q^d$ at p^e .
- Suppose $p < p^e$. Then $q^d > q^s$, yielding **shortage**. Consumers compete and force p up, having q^d falls and q^s rises. Eventually $q^d = q^s$ at p^e .

Changes in Supply and/or Demand: Effect on Equilibrium

Example 2.5 (a) Demand increases from D_1 to D_2 .

When demand increases (say, due to an increase in income) from D_1 to D_2 , we have $q^d > q^s$ at original equilibrium price p_1^e , resulting in shortage, which in turn results in a price rise. Thus consumers move from A to E_2 , and producers move from E_1 to E_2 as depicted in Figure 2.19.

Result: An increase in demand leads to an increase in both the equilibrium price p^e and the equilibrium quantity q^e .

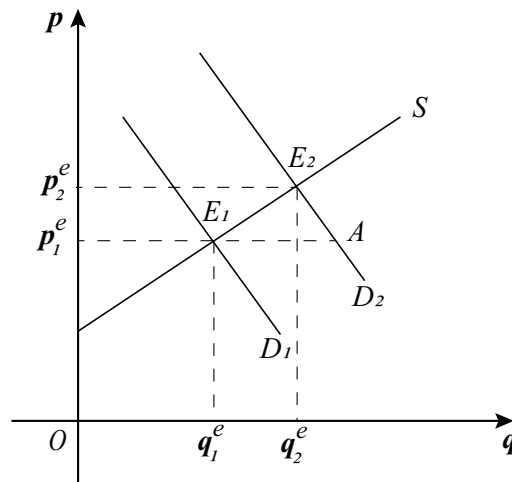


Figure 2.19 The effect of an increase in demand on market equilibrium: resulting in increase in both p^e and q^e

Example 2.6 (b) Supply increases from S_1 to S_2 .

When supply increases (say, due to an increase in productivity or a decrease in cost of production) from S_1 to S_2 , we have $q^s > q^d$ at p_1^e , resulting in surplus, which in turn results in price falls. Thus consumers move from E_1 to E_2 , and producers move from B to E_2 as depicted in Figure 2.20.

Result: Increase in $S \Rightarrow p^e$ falls and q^e rises.

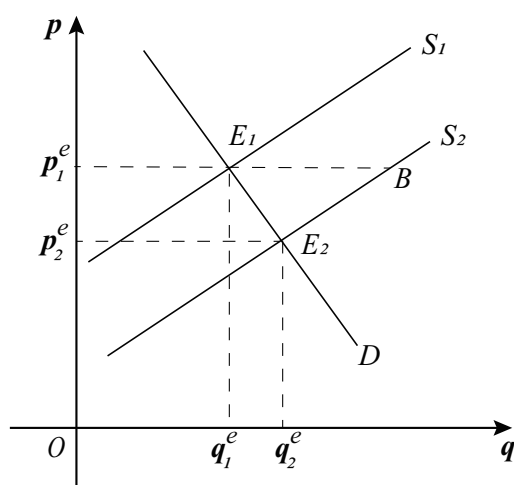


Figure 2.20 The effect of an increase in supply on market equilibrium: resulting in decrease in p^e and increase in q^e

Example 2.7 (c) Supply and demand rise

Result: Increase in S and D will cause the equilibrium q^e rises as depicted in Figure 2.21, but the equilibrium p^e is uncertain without further information on demand and supply.

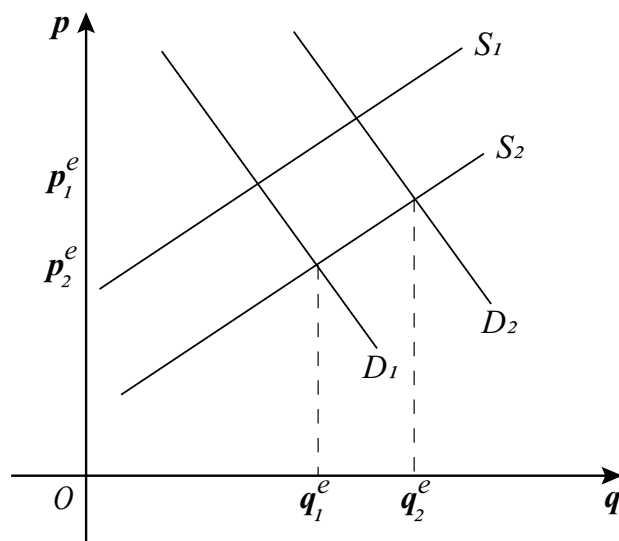


Figure 2.21 The effect of simultaneous increase in demand and supply on market equilibrium: resulting in increase in q^e

Figure 2.22 graphically shows 9 possibilities of the effects of simultaneous changes in demand and/or supply on market equilibrium price and quantity.

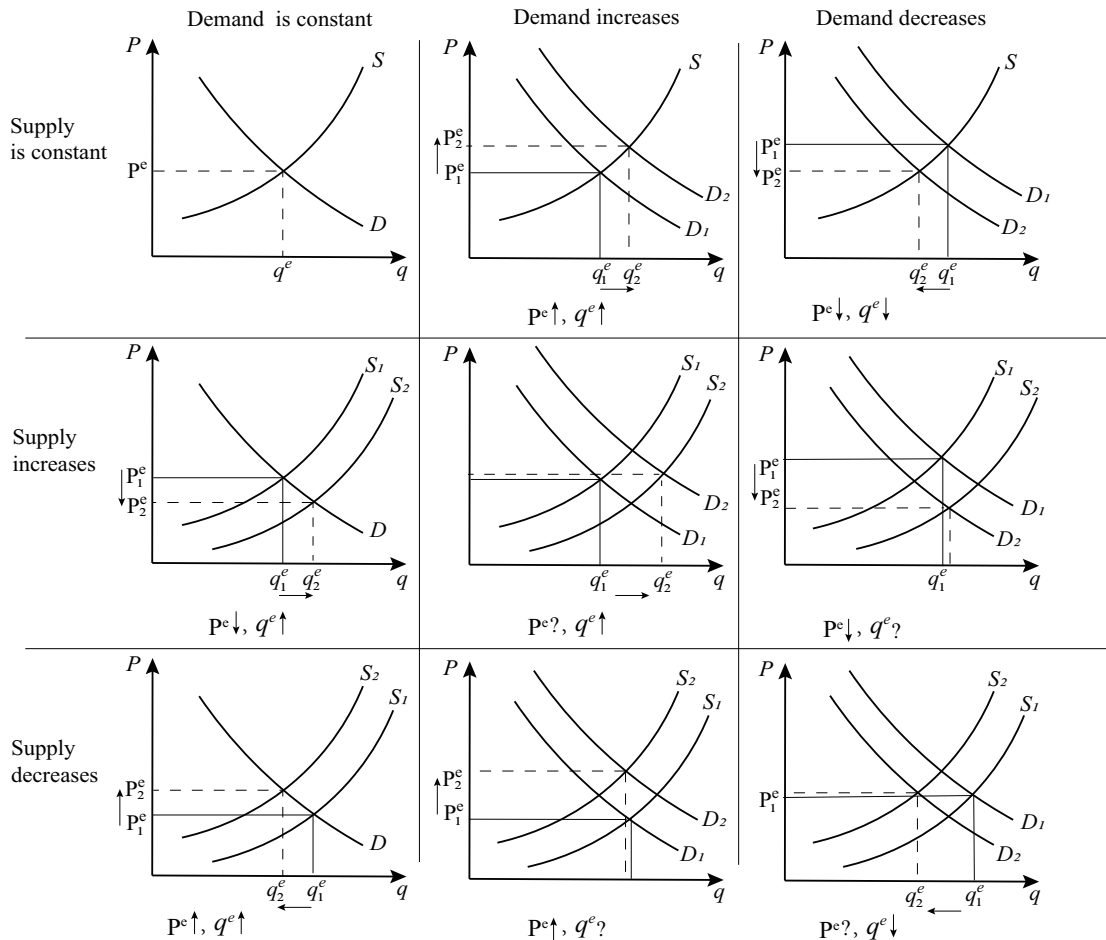


Figure 2.22 Nine possibilities of simultaneous change in demand and supply

Note that when both demand and supply curves shift, there are four possible scenarios as shown in Figure 2.22. In these cases, it is uncertain whether the equilibrium price or quantity will increase, decrease, or remain unchanged without further information on the magnitudes of the shifts.

However, with specific information on the changes in demand and supply, we can determine the direction of the changes in equilibrium price and quantity, as shown in the following example.

Example 2.8 (Markets for eggs and college (continued)) From 1970 to 2010, the real price of eggs fell by 55 percent, while the real price of college education rose by 82 percent.

The mechanization of poultry farms sharply reduced the cost of producing eggs, shifting the supply curve to the right. At the same time, the demand curve for eggs shifted to the left as a more health-conscious population tended to avoid eggs. As a result, the real price of eggs fell sharply and egg consumption rose, as depicted in Figure 2.23(a).

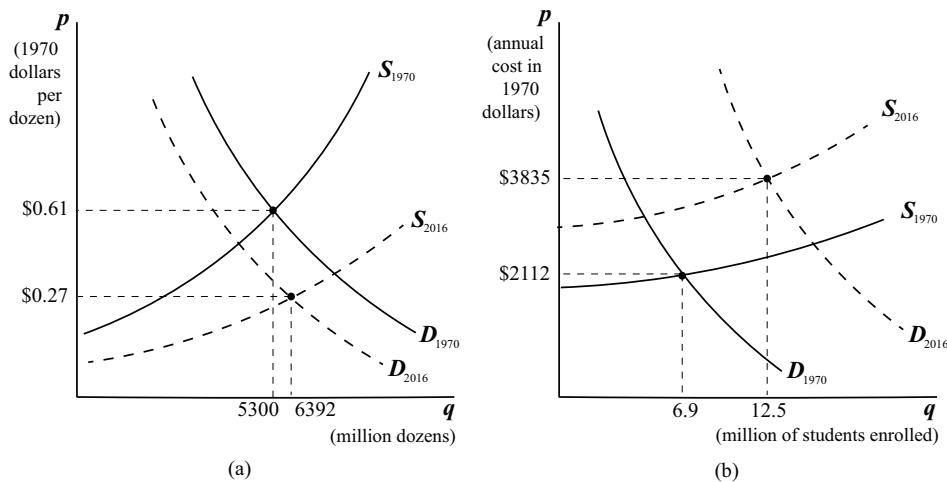


Figure 2.23 (a) Markets for eggs; (b) Markets for college

As for college, increases in the costs of equipping and maintaining modern classrooms, laboratories, and libraries, along with increases in faculty salaries, pushed the supply curve up. At the same time, the demand curve shifted to the right as a larger percentage of a growing number of high school graduates decided that a college education was essential. As a result, both price and enrollments rose sharply as depicted in Figure 2.23(b).

Example 2.9 (Explaining Wage Inequality in the United States) Over the past four decades, there has been a significant increase in wage inequality in the United States, with the wages of skilled high-income workers growing substantially, while the wages of unskilled low-income workers have fallen slightly.

From 1978 to 2009, people in the top 20 percent of the income distribution experienced an increase in their average real (inflation-adjusted) pretax household income of 45 percent, while those in the bottom 20 percent saw their average real pretax income increase by only 4 percent.

More surprisingly, by the end of 2021, the top 1% of Americans owned a record-high 32.3% of the country's wealth while the share of wealth held by the bottom 90% of Americans is only 30.2% (so the top 10% of Americans owned almost 70% of the country's total wealth). The top 20% of Americans owned 86% of the country's wealth while the bottom 80% of the population owned 14% in 2020.

One of the reasons for this wage inequality is the differences in human capital and the impact of new technological revolutions, such as artificial intelligence and the digital economy. The supply of unskilled workers with limited education or outdated skills has grown substantially, while the demand for them has risen only slightly. In contrast, the supply of skilled workers, such as engineers, scientists, managers, and economists, has grown slowly, but the demand has risen dramatically, pushing their wages up significantly.

Example 2.10 (Supply and Demand for City Office Space) Since the outbreak of COVID-19, there has been a decrease in demand for city office space as more people have started working from home. However, the decrease in supply has been relatively small, leading to a decrease in the average rental price for office space in cities.

2.5 Elasticity of Demand and Supply

The concept of elasticity is of immense importance in consumers' consumption decisions, businessmen's pricing strategies, government policies (such as taxation), and international trade (such as the terms of trade between two countries).

Elasticity measures the responsiveness of the percentage change in quantity demanded (or supplied) to a percentage change in a variable (such as own price, prices of other goods, and income).

Is it appropriate to use the slope of the curve to measure the elasticity? No, because a change in scale can make a curve look flatter or steeper without altering absolute responsiveness. Thus, changing units (say from a dollar to a cent) will alter the slope. For this reason, economists use a unitless measure to measure the elasticity.

2.5.1 Elasticity of Demand

Price elasticity of demand ("own" Price Elasticity): Percentage change in quantity demanded resulting from a percentage change in its price:

$$\begin{aligned} E_d^p &= \frac{\text{percentage change in quantity demanded}}{\text{percentage change in its price}} \\ &= \frac{\Delta Q/Q}{\Delta P/P} \\ &= \frac{P}{Q} \times \frac{\Delta Q}{\Delta p} = \frac{P}{Q} \times \text{the slope of } D, \end{aligned}$$

where " Δ " = "change". Note that since demand curves in general slope downward, E_d^p will be negative.

Range of Value for E_d^p :

(a) **Inelastic demand:** $|E_d^p| < 1$.

$$\left| \frac{\Delta Q/Q}{\Delta P/P} \right| < 1 \Rightarrow |\Delta Q/Q| < |\Delta P/P|.$$

When demand is inelastic, the quantity demanded is relatively unresponsive to changes in price; e.g., cigarettes.

- (b) **Elastic demand:** $|E_d^p| > 1$. That is $|\Delta Q/Q| > |\Delta P/P|$. When demand is elastic, the quantity demanded is relatively responsive to changes in price; e.g., automobiles in the short run, competing goods.
- (c) **Unit elasticity of demand:** $|E_d^p| = 1$, i.e., $|\Delta Q/Q| = |\Delta P/P|$.
- (d) **Iso-elastic demand curve Demand curve:** the price elasticity is constant.
- (e) **Perfectly inelastic demand:** $|\Delta Q/Q| = 0$ for all changes in price —i.e., totally unresponsive.
- (f) **Perfectly elastic demand:** $|E_d^p| = \infty$. A very small percentage change in price leads to a tremendous percentage change in quantity demanded.

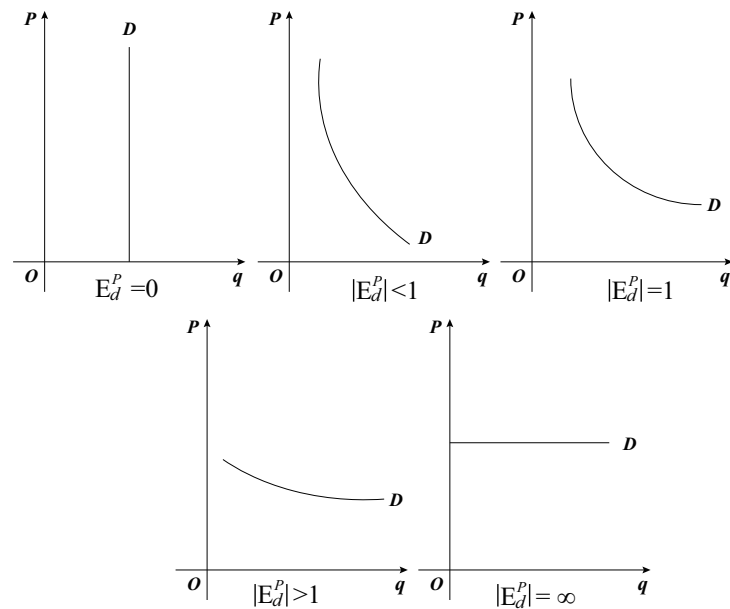


Figure 2.24 Types of demand elasticity

Example 2.11 Suppose the price of good x increases from 1 to 2, and the quantity demanded changes from 10 to 5.

P	Q
\$1	10
\$2	5

We can calculate the price elasticity of demand using the formula:

$$E_d^p = -\frac{\frac{\Delta Q}{Q}}{\frac{\Delta P}{P}} = -\frac{5 - 10}{10} \div \frac{2 - 1}{1} = -\frac{5}{10} \div \frac{1}{1} = -\frac{1}{2}.$$

Now suppose the price of good x decreases from 2 to 1, and the quantity demanded changes from 5 to 10.

P	Q
\$2	5
\$1	10

Using the same formula, we get:

$$E_d^p = \frac{\frac{\Delta Q}{Q}}{\frac{\Delta P}{P}} = \frac{10 - 5}{5} \div \frac{1 - 2}{2} = \frac{5}{5} \div \left(-\frac{1}{2}\right) = 1.$$

This example demonstrates how the elasticity of demand can vary depending on the direction of the price change and the reference (initial) point used. To avoid this issue, we can use the **midpoint elasticity**, also known as the **arc elasticity** of demand. The midpoint elasticity measures the average responsiveness of quantity demanded to a change in price, regardless of the direction of the change.

Midpoint elasticity of demand measures the price elasticity of de-

mand between two points (P, Q) and (P', Q') using the midpoints as reference points:

Midpoint elasticity of demand: E_d^p between points (P, Q) and (P', Q') is given by

$$E_d^p = \frac{\Delta Q / \frac{1}{2}(Q + Q')}{\Delta P / \frac{1}{2}(P + P')},$$

where the numerator and denominator use the average of the initial and final values as the base for computing the percentage changes.

Using the midpoint elasticity formula avoids the problem of varying elasticities that arises from using different P - Q combinations as the reference point.

Example 2.12 (Example 2.11 (continued)) Consider the example again.

P	Q
\$2	5
\$1	10

Note that

$$\Delta Q / \frac{1}{2}(Q + Q') = -\frac{5}{\frac{1}{2} \cdot 15} = -\frac{2}{3}$$

and

$$\Delta P / \frac{1}{2}(P + P') = \frac{1}{\frac{1}{2} \cdot 3} = \frac{2}{3},$$

so we have

$$E_d^p = \frac{-2/3}{2/3} = -1.$$

Only very special demand curves have constant elasticity between any two points.

Elasticity along Straight Line Demand Curve

The straight line demand function

$$D = a - bP$$

does not have a constant elasticity throughout. Indeed,

$$\begin{aligned} E_d^p &= \frac{\Delta Q/Q}{\Delta P/P} = \frac{P}{Q} \cdot \frac{\Delta Q}{\Delta P} \\ &= \frac{P}{Q} \times \text{the slope of } D \\ &= a \times \frac{P}{Q} \\ &\neq \text{constant} \end{aligned}$$

because $\frac{P}{Q}$ is not constant even though the slope of a linear demand curve, a , is constant.

Moreover, from Figure 2.25, we have

$$|E_d^p| = \left| \frac{\Delta Q}{\Delta P} \right| \cdot \frac{P}{Q} = \frac{LB}{AL} \cdot \frac{OL}{LB} = \frac{OL}{AL}.$$

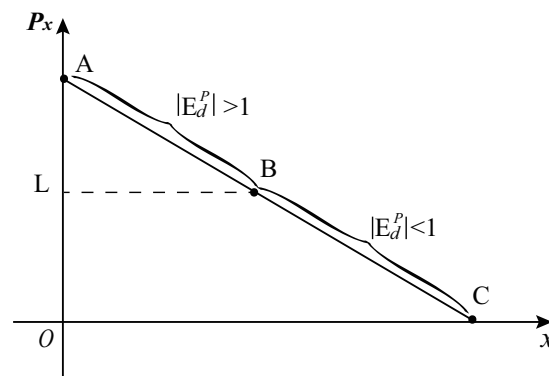


Figure 2.25 Elasticities vary along a linear demand curve

Thus, if B is the midpoint of the demand curve, then $|E_d^p| = 1$. If B is a point above the midpoint, then $AL < OL \Rightarrow |E_d^p| > 1$. If B is a point below the midpoint, $AL > OL \Rightarrow |E_d^p| < 1$.

Therefore, *along a downward-sloping straight-line demand curve, the price elasticity varies although the slope is constant.*

2.5.2 Elasticity and Total Expenditure

The **total expenditure** (TE) for consuming a good is:

$$TE = P \times Q.$$

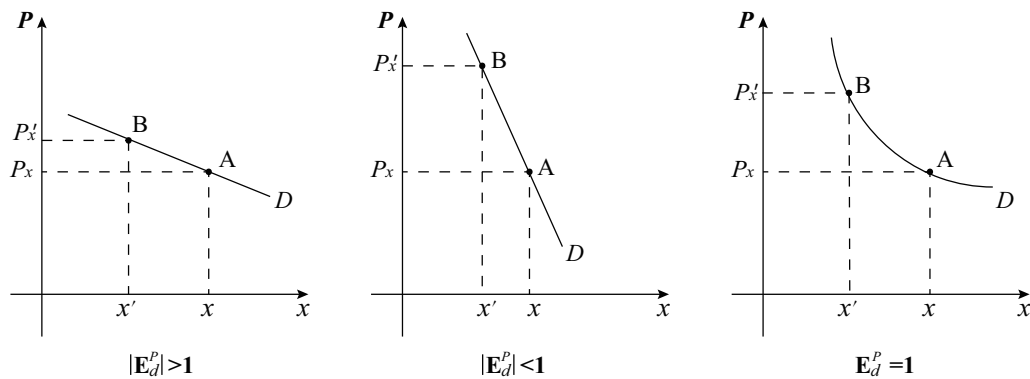


Figure 2.26 Total expenditure under alternative demand elasticities

We are now interested in what happens to the total expenditure $P \times Q$ when P varies. Since P and Q are inversely related by downward-sloping demand, we need further information about the magnitude of the changes in P and Q to determine the effect on $P \times Q$, which is the price elasticity of demand. The relationships are given in Table 2.2.

	$ E_d^p < 1$	$ E_d^p > 1$	$ E_d^p = 1$
P rises	TE rises	TE falls	TE holds constant

Table 2.2: The relationship between elasticity and total expenditure.

In other words, when demand is inelastic, price and total expenditure move in the same direction (this should be easily understood by intuition such as cigarettes). When demand is elastic, price and total expenditure move in opposite directions. When demand is unit elastic, the total expenditure remains constant when the price varies.

Therefore, when the price rises, an inelastic demand implies that the total expenditure increases, an elastic demand implies that the total expenditure decreases, and consequently, the *total expenditure reaches its maximum when demand is unit elastic*.

Algebraically, we can verify that these relationships hold true. Suppose $|E_d^p| > 1$ and $P' > P$.

$$\begin{aligned} \frac{\Delta Q / \frac{1}{2}(Q + Q')}{\Delta P / \frac{1}{2}(P + P')} &> 1 \\ \Rightarrow \frac{\Delta Q}{Q + Q'} &> \frac{\Delta P}{P + P'} \\ \Rightarrow (Q - Q')(P + P') &> (P' - P)(Q + Q') \\ \Rightarrow PQ - P'Q' &> -PQ + P'Q' \\ \Rightarrow 2PQ &> 2P'Q' \\ \Rightarrow PQ &> P'Q'. \end{aligned}$$

This shows that if P rises, the total expenditure falls.

Other Elasticities:

- Income elasticity (E_d^I):

$$E_d^I = \frac{\Delta D/D}{\Delta I/I}.$$

- Cross-price elasticity of demand: Let p_y be the price of good y . The cross-price elasticity of demand for good x with respect to the price

is defined as

$$E_{d_x}^{p_y} = \frac{\Delta D_x / D_x}{\Delta p_y / p_y}.$$

2.5.3 Price Elasticity of Supply

The Price Elasticity of Supply: a measure of the responsiveness of quantity supplied to a change in price. It is defined as the percentage change in quantity supplied divided by the percentage change in price:

$$E_S^P = \frac{\Delta S / S}{\Delta P / P} = \frac{P}{S} \times \frac{\Delta S}{\Delta P} = \frac{P}{S} \times \text{the slope of } S.$$

We have the following typical cases:

- $E_S^P > 0$ since supply slopes upwards.
- If $E_S^P > 1$, then supply is **elastic**.
- If $E_S^P < 1$, then supply is **inelastic**.
- If $E_S^P = 1$, then supply is **unit elastic**.
- If $E_S^P = 0$, then supply is **perfectly inelastic**.
- If $E_S^P = \infty$, then supply is **perfectly elastic**.

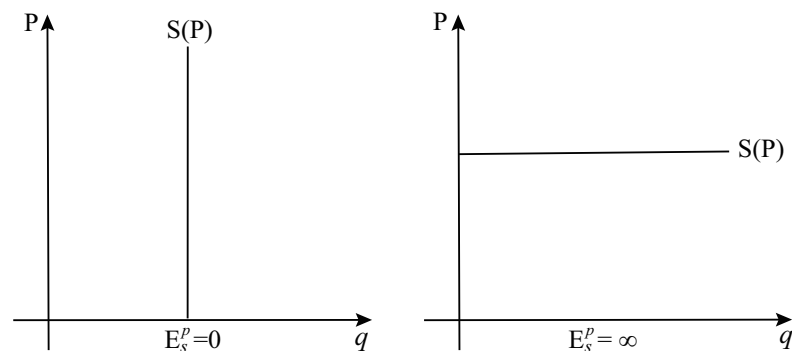


Figure 2.27 Perfectly inelastic and perfectly elastic supplies

Example 2.13 (Market for Wheat) During recent decades, changes in the wheat market had major implications for both American farmers and U.S. agricultural policy.

To understand what happened, let's examine the behavior of supply and demand beginning in 1981.

$$Q_s = 1800 + 240P$$

$$Q_d = 3550 - 266P$$

By setting the quantity supplied equal to the quantity demanded, we can determine the market-clearing price and the equilibrium quantity of wheat for 1981:

$$P = \$3.46,$$

and

$$Q = 2630.$$

We then can use the demand curve to find the price elasticity of demand at market equilibrium:

$$E_D^P = \frac{P}{Q} \times \frac{\Delta Q_D}{\Delta P} = \frac{3.46}{2630}(-266) = -0.35$$

and so demand is inelastic at equilibrium.

We can likewise calculate the price elasticity of supply at market equilibrium

$$E_S^P = \frac{P}{Q} \times \frac{\Delta Q_S}{\Delta P} = \frac{3.46}{2630}(240) = 0.36.$$

Suppose that a drought caused the supply decreases significantly, which pushes the price up to \$4.00 per bushel. In this case, the quantity demanded would fall to $3550 - (266)(4.00) = 2486$ million bushels. At this price and quantity, the elasticity of demand would be

$$E_D^P = \frac{P}{Q} \times \frac{\Delta Q_D}{\Delta P} = \frac{4.00}{2486}(-266) = -0.43$$

In 2007, demand and supply were

$$Q_s = 1400 + 115P$$

$$Q_d = 2900 - 125P$$

The market-clearing price and the equilibrium quantity are then

$$P = \$6,$$

and

$$Q = 2150.$$

Dry weather and heavy rains, combined with increased export demand caused the price to rise considerably. You can check to see that, at the 2007 price and quantity, the price elasticity of demand was -0.35 and the price elasticity of supply 0.32. Given these low elasticities, it is not surprising that the price of wheat rose so sharply.

2.5.4 Short-Run versus Long-Run Elasticities

Consumption of Durables and Nondurables

Consumer expenditures include **durable goods** (automobiles, appliances, furniture, etc.) and **nondurable goods** (fuel, food, clothing, services, etc.).

For nondurable goods, the price elasticity of demand is larger in the long run than in the short run. For a durable good, the opposite is true. The short-run price elasticity of demand will be much larger than the long-run elasticity for durable goods. These relationships are also true for income elasticity of demand.

We can verify these assessments by the following example.

Example 2.14 (Elasticities of Demand for Gasoline and Automobiles) Consider the price and income elasticities of demand for gasoline and automobiles, which are given in Table 2.3 and Table 2.4, respectively.

2.6. EFFECTS ON GOVERNMENT INTERVENTION: PRICE CONTROLS 55

Elasticity for Gasoline	1	2	3	5	10
price	-0.2	-0.3	-0.4	-0.5	-0.8
income	0.2	0.4	0.5	0.6	1.0

Table 2.3: The price and income elasticities of demand for gasoline: Number of years allowed to pass following a price or income change

In the short run, an increase in price of gasoline has only a small effect on the quantity of gasoline demanded. Motorists may drive less, but they will not change the kinds of cars they are driving overnight. In the longer run, however, because they will shift to smaller and more fuel-efficient cars, the effect of the price increase will be larger. Demand for gasoline, therefore, is more elastic in the long run than in the short run.

Elasticity for Automobiles	1	2	3	5	10
price	-1.2	-0.9	-0.8	-0.6	-0.4
income	3.0	2.3	1.9	1.4	1.0

Table 2.4: The price and income elasticities of demand for automobiles: Number of years allowed to pass following a price or income change

The opposite is true for automobile demand. If the price of automobile increases, consumers initially defer buying new cars; thus annual quantity demanded for automobile falls sharply. In the longer run, however, old cars wear out and must be replaced; thus annual quantity demanded picks up. Demand for automobiles, therefore, is less elastic in the long run than in the short run.

2.6 Effects on Government Intervention: Price Controls

Markets can be thought of as a **self-adjustment mechanism**; they automatically adjust to any change affecting the behavior of buyers and sellers

in the market. But for this mechanism to operate effectively, the price must be free to move in response to the interplay of supply and demand. When the government steps in to regulate prices, the market does not function in the same way.

There are two types of price controls: **price ceiling** and **price floor**.

Price Ceiling:

A price above which buying or selling is illegal. It is aimed to help consumers.

Allocation Methods:

- i) first come, first served;
- ii) rationing (using coupons).

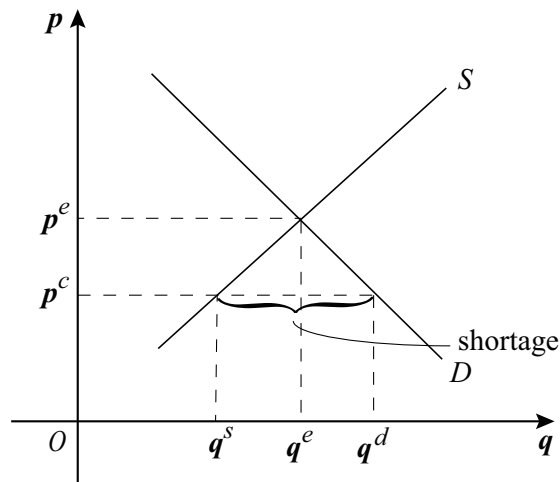


Figure 2.28 Price ceiling: the emergence of shortage

Effects of Price Ceiling:

- a. in general it results in shortage;
- b. there is a tendency to form a black market;
- c. bad service and bad quality of goods;

2.6. EFFECTS ON GOVERNMENT INTERVENTION: PRICE CONTROLS⁵⁷

- d. production is reduced;
- e. provide wrong information about production and consumption;
- f. it hurts producers who provide goods, and some consumers gain from the price ceiling but other may be worse off.

Price Floor (also known as Price Support):

A price below which buying or selling is prohibited. It is aimed to help producers. Examples include setting prices of agricultural products and minimum wage rate.

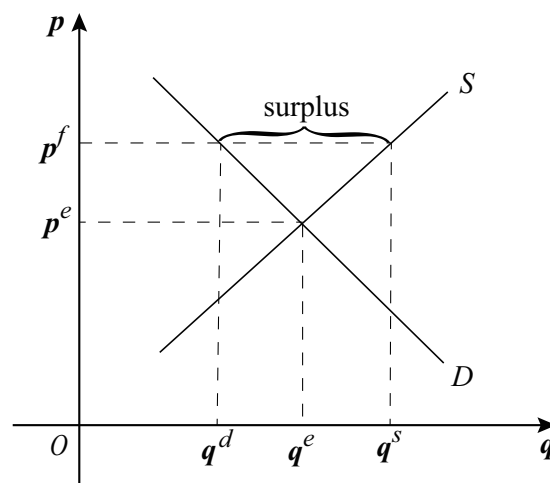


Figure 2.29 Price floor: the emergence of surplus

Effects of Price Floor:

- a. in general it results in surplus;
- b. inefficiency in terms of resources allocation;
- c. the government may need to spend money on storing the surplus or subsidize producers;
- d. consumers may switch to substitutes;

- e. firms may reduce their output, leading to unemployment and reduced income;
- f. some producers gain from the price floor but others may be worse off, and some consumers may benefit from the lower supply price.

Methods for Maintaining Price Support:

- i) the government purchases surplus, and then the total revenue of the producer $= p^f \times q^s$.
- ii) output is restricted at q^d , and then the total revenue of the producer $= p^f \times q^d$.

Besides the effects mentioned for these two types of price controls, we will discuss they also result in welfare losses.

Example 2.15 (Price Control and Wheat) Suppose that the demand and supply of wheat are respectively given by

$$D(p) = 90 - 20p,$$

$$S(p) = -15 + 10p.$$

- a) Find the market equilibrium price and quantity.

Setting $D(p) = S(p)$, we have $90 - 20p = -15 + 10p$ which gives us $p^e = 105/30 = 3.5$ and $q^e = 20$.

- b) Suppose a price support is set at \$4. What is the surplus?

Since

$$D(4) = 90 - 20 \times 4 = 10,$$

$$S(4) = -15 + 10 \times 4 = 25,$$

so the surplus is given by

$$S(4) - D(4) = 25 - 10 = 15.$$

Part II

Demand Side of Market

Part 2 presents theoretical core of consumer behavior and individual and market demands.

Chapter 3

Theory of Consumer Choice

The theory of consumer choice is a fundamental concept in economics that explains how individuals make decisions. It provides a framework for understanding how consumers allocate their incomes to purchase various goods, which is essential for corporate decision-making and public policy.

Consumers have various characteristics, including gender, appearance, age, lifestyle, wealth, preferences, ability, and so on. However, which of these characteristics are critical in determining the optimal choice of the consumer? In principle, a consumer's choice is determined by their **subjective preferences** subject to **objective restrictions**, typically budget constraints.

3.1 Budget Constraints

Budget constraints: Constraints that consumers face as a result of limited incomes.

3.1.1 Budget Line

The **budget line:** A straight line representing all possible combinations of goods that a consumer can obtain at given prices by spending a given income, namely, the total expenditure of consumptions is equal to income.

A budget line with two commodities, as depicted in Figure 3.1, is:

$$p_x x + p_y y = I, \quad (3.1)$$

where p_x and p_y represent prices of goods x and y , and hence $p_x x + p_y y$ stands for total expenditure which is equal to income I .

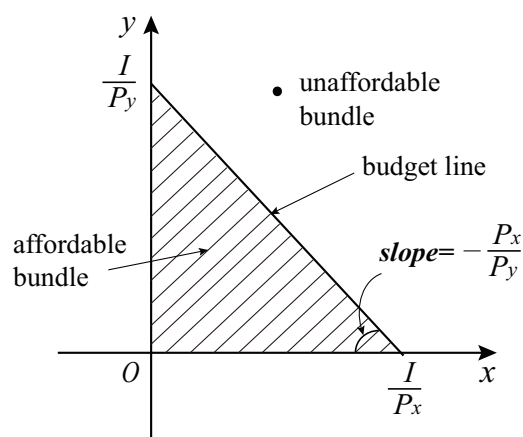


Figure 3.1 Budget constraints and budget line

We can rewrite the budget line (3.1) as

$$y = \frac{I}{p_y} - \frac{p_x}{p_y} x, \quad (3.2)$$

where the slope of (3.1) is $-\frac{p_x}{p_y}$, x -axis intercept is $\frac{I}{p_x}$ representing the maximum units of good x that can be purchased, and y -axis intercept is $\frac{I}{p_y}$ representing the maximum units of good y that can be purchased.

Example 3.1 Two goods x and y , with prices $p_x = 10$ and $p_y = 5$. Income is $I = 100$. So the budget line is

$$10x + 5y = 100.$$

The slope of budget line is $-\frac{p_x}{p_y} = -10/5 = -2$, y -axis intercept is $\frac{I}{p_y} =$

$\frac{I}{p_y} = 100/5 = 20$, and x -axis intercept is $\frac{I}{p_x} = 100/10 = 10$.

Combination: $p_x \times \text{unit of } x + p_y \times \text{unit of } y = \text{income}$

a.	10×10	+	5×0	=	\$100
b.	10×8	+	5×4	=	\$100
c.	10×6	+	5×8	=	\$100
d.	10×4	+	5×12	=	\$100
e.	10×2	+	5×16	=	\$100
b.	10×0	+	5×20	=	\$100

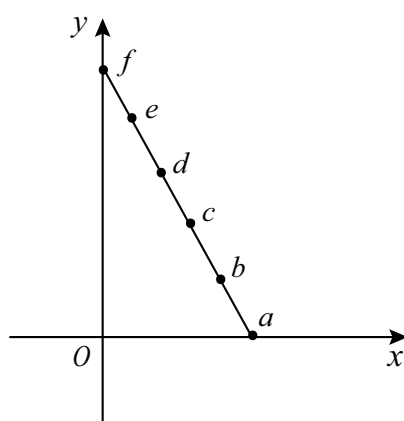


Figure 3.2 A budget line with two consumption goods

3.1.2 Changes in Budget Line

What if prices and income increase at the same rate? If we double both prices and income, then $2p_x x + 2p_y y = 2I$, and nothing changes.

What if only one price changes? If p_y in the above example is changed to $p_y^* = 10$, and p_x and I are the same as before, the new budget line is $10x + 10y = 100$, with slope $-\frac{p_x}{p_y} = -1$. That is, a change in the price of one good causes the budget line to rotate about one intercept.

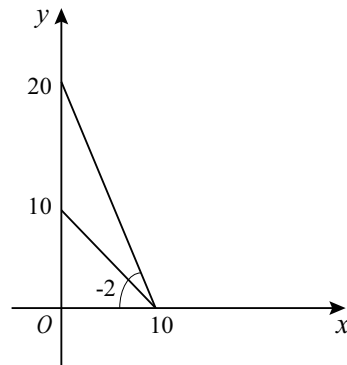


Figure 3.3 The effect of a change in price on budget line

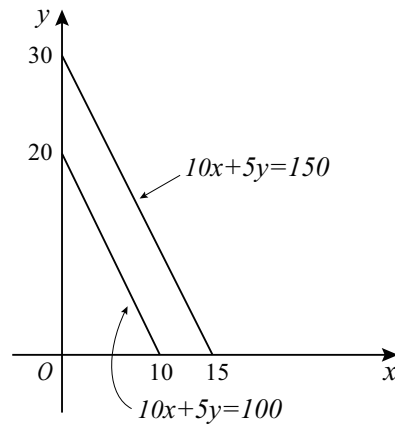


Figure 3.4 The effect of a change in income on budget line

What if only income changes? If the income in the above example changes from \$100 to \$150, the new budget line is $10x + 5y = 150$. Then a change in income (with prices unchanged) causes the budget line to shift parallel to the original line.

3.2 Consumer Preferences

Consumers are assumed to have preferences over bundles (baskets) of goods. Suppose that there are two goods available, x and y , and two bun-

dles of these goods, A and B , where each bundle contains a given amount of x and y :

$$A = (x^A, y^A), B = (x^B, y^B).$$

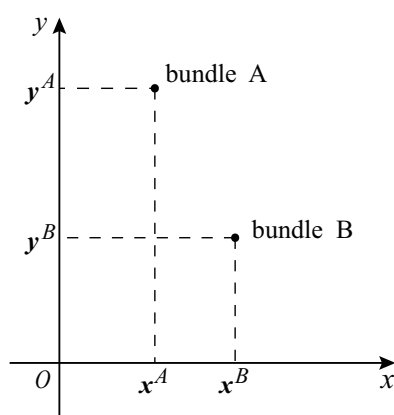


Figure 3.5 Two alternative consumption bundles A and B

3.2.1 Basic Assumptions on Preferences

We make the following assumptions on the consumer's preferences.

1. **Completeness:** consumers can compare and rank all possible baskets. Between any two bundles, the consumer can only make one of the following statements:
 - (a) A is preferred to B ($A \succ B$),
 - (b) B is preferred to A ($B \succ A$), or
 - (c) A is indifferent to B ($A \sim B$).

By *indifferent*, we mean that the consumer will be equally satisfied with either basket. Note that these preferences ignore costs. A consumer might prefer steak to hamburger but buy hamburger because it is cheaper.

2. **Transitivity:**

(a) $A \succ B$ and $B \succ C$ imply $A \succ C$.

Transitivity is normally regarded as necessary for consumer consistency.

3. **More is preferred to less:** goods are desirable;

(a) if $A = (x^A, y^A)$, $B = (x^A, y^A + c)$, $c > 0$, then $B \succ A$.

Consequently, consumers always prefer more of any good to less. In addition, consumers are never satisfied or satiated; more is always better, even if just a little better.

Indifference curve: a curve representing all combinations of market baskets that provide a consumer with the same level of satisfaction. Thus, a consumer is indifferent between any two bundles that lie on the same indifference curve.

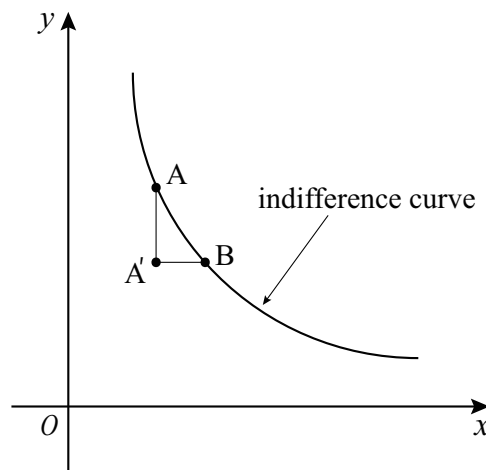


Figure 3.6 The process of formulating an indifference curve

To find an indifference curve, we can start from bundle A . Subtracting one unit of good y puts us at a point A' , strictly less preferred to A by assumption iii), i.e., $A' \prec A$. However, if we add more x to A' , we know that

A' will be less preferred to the resulting new point. If we add "enough" x to A' , then we find a point B such that $A \sim B$, as shown in Figure 3.6, etc.

Similarly, we can trace out a family of indifference curves, namely, an **indifference map** — i.e., a graph containing a set of indifference curves showing the market baskets among which a consumer is indifferent. In Figure 3.7, we have $A \sim B$, $\bar{A} \sim \bar{B}$, $\bar{\bar{A}} \sim \bar{\bar{B}}$, but any point on U^1 is preferred to any point on U^0 , and is less preferred to any point on U^2 by assumptions ii) and iii).

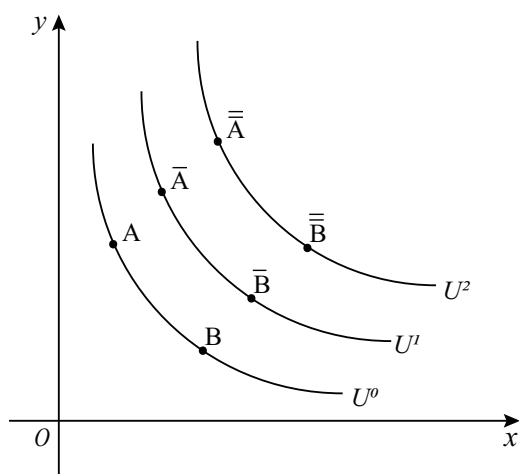


Figure 3.7 Indifference map: a set of indifference curves

3.2.2 Properties of Indifference Curves

There are two crucial properties of indifference curves:

- i) *Indifference curves slope downward* by assumption ii).
- ii) *Indifference curves cannot intersect*.

Suppose they did intersect. Note that $A \sim B$, $C \sim B$, and $C \succ A$. Therefore, transitivity implies $C \succ B$. But this contradicts the fact that $C \sim B$. Hence, indifference curves cannot intersect.

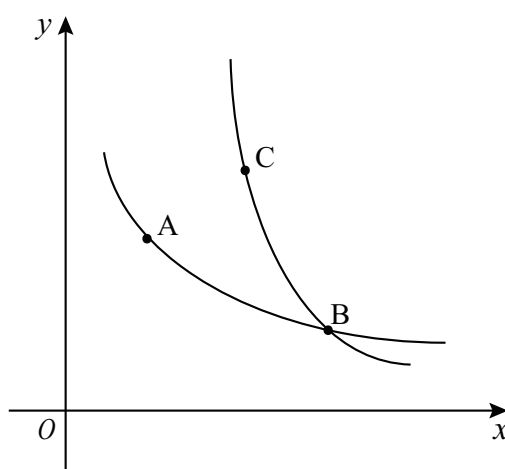


Figure 3.8 Indifference curves cannot intersect

3.2.3 Marginal Rate of Substitution

The slope of an indifference curve reflects the consumer's willingness to trade one good for another while remaining on the same indifference curve, leading to the important concept of **marginal rate of substitution**.

The **marginal rate of substitution of x for y** (MRS_{xy}): The maximum amount of good y that a consumer is willing to give up in exchange for one more unit of good x , while remaining on the same indifference curve.

Formally, MRS_{xy} is defined as the absolute value of the slope of the indifference curve, denoted as $\left| \frac{\Delta y}{\Delta x} \right|$ where " Δ " stands for small changes. The magnitude of the slope of an indifference curve measures the consumer's marginal rate of substitution (MRS) between two goods x and y .

Indifference curves generally satisfy the following important property:

Diminishing MRS: The amount of good y that the consumer is willing to give up for one additional unit of x decreases as the quantity of x increases.

Diminishing MRS implies that the MRS falls as we move down the indifference curve, which is equivalent to the strict convexity of consumer preferences:

Strict Convexity: Indifference curves are strictly convex to the origin, resulting in diminishing MRS, as depicted in Figure 3.9.

In Figure 3.9, at point *A*, *y* is abundant while *x* is scarce; thus, the consumer is willing to give up a relatively large amount of the plentiful good to obtain more of the scarce good. At point *E*, *y* is scarce while *x* is abundant, and the consumer is willing to give up less of *y* for another unit of *x*.

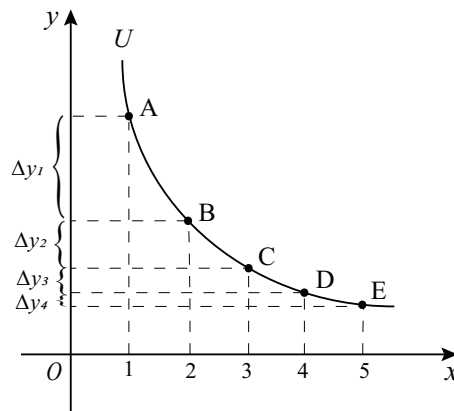


Figure 3.9 The shape of indifference curves: convex to the origin

Example 3.2 Consider the numerical example depicted in Figure 3.10.

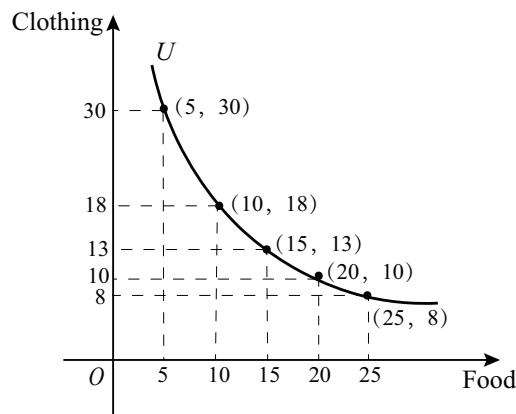


Figure 3.10 MRS between clothing and food

Clothing (C)	Food (F)	MRS of F for C	
30	5		
18	10	$ \frac{\Delta C}{\Delta F} = \frac{30-18}{10-5} = 2.4$	↓
13	15	$ \frac{\Delta C}{\Delta F} = \frac{18-13}{15-10} = 1.0$	↓
10	20	$ \frac{\Delta C}{\Delta F} = \frac{13-10}{20-15} = 0.6$	↓
8	25	$ \frac{\Delta C}{\Delta F} = \frac{10-8}{25-20} = 0.4$	↓
7	30	$ \frac{\Delta C}{\Delta F} = \frac{8-7}{30-25} = 0.2$	↓

Table 3.1: MRS_{xy} decreases as more food is consumed relative to clothing.

Table 3.1 shows how MRS between two goods, clothing (C) and food (F), decreases as more of one good is consumed relative to the other. As the MRS decreases, the consumer is less willing to give up units of one good to obtain additional units of the other good.

The convexity of preferences implies that individuals prefer to diversify their consumption choices, meaning they prefer to consume a variety of goods rather than just one or a few. This preference for diversification is a fundamental aspect of economic markets, and convexity can be seen as a formal expression of this preference.

3.2.4 Special Shapes of Indifference Curves:

An indifference curve *may not be strictly convex* to the origin (although it is convex) for some special shapes of indifference curves.

i) **Perfect substitutes** (linear indifference curves): Since the slope of a straight line is constant, MRS is constant.

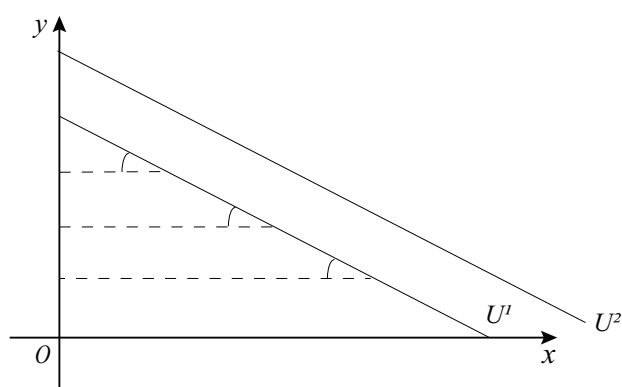


Figure 3.11 Perfect substitutes: constant MRS

ii) **Perfect complements:** two goods for which the MRS is zero or infinite; the indifference curves are shaped as right angles, e.g., x = left shoe, y = right shoe.

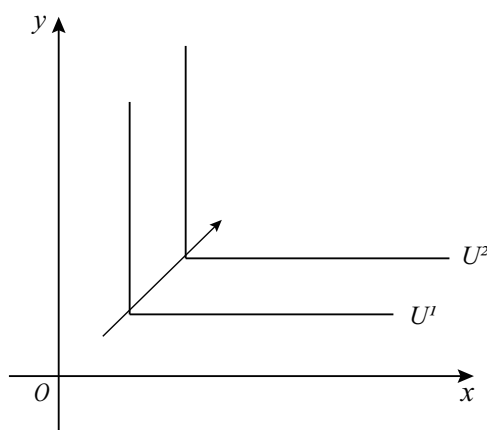


Figure 3.12 Perfect complements: shaped as right angles

iii) Only the consumption of good y matters; see Figure 3.13.

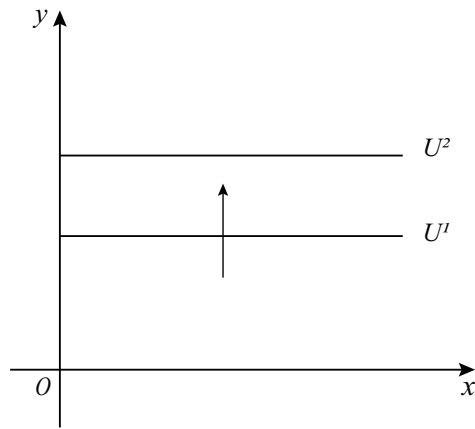


Figure 3.13 Horizontal indifference curves

iv) Only the consumption of good x matters; see Figure 3.14.

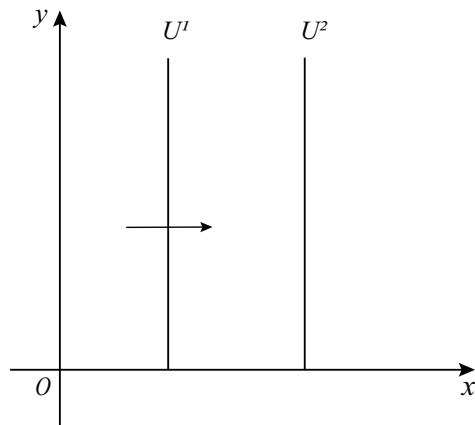


Figure 3.14 Vertical indifference curves

v) Bads: Bad good for which less is preferred rather than more; see Figure 3.15.

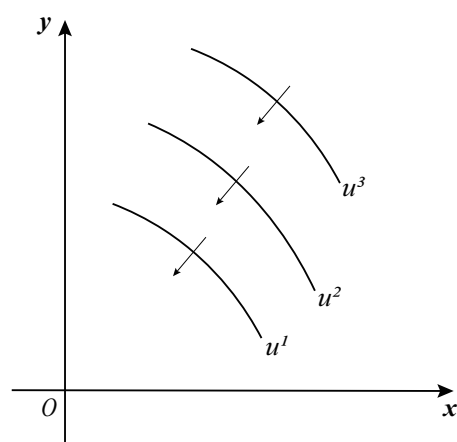


Figure 3.15 Vertical indifference curves

3.2.5 Utility Functions

Indifference curves, which represent consumer preferences, enable us to rank commodity bundles. That is, as shown in Figure 3.16, $A \prec B$, and $B \prec C$. Sometimes it is convenient to summarize these rankings with a numerical score. Therefore, #1 = C , #2 = B , #3 = A .

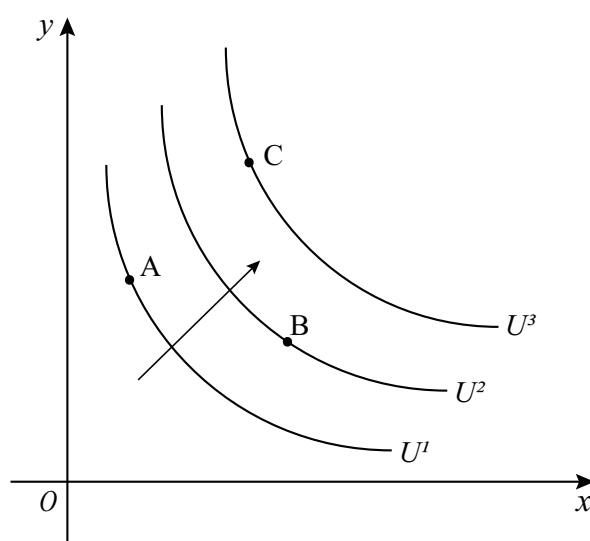


Figure 3.16 Ranking alternative market baskets using indifference curves

A **utility function** can be derived from a set of indifference curves, each with a numerical indicator that represents the consumer's preferences. The utility function $U(x, y)$ assigns a number to commodity bundle (x, y) such that:

1. If $U(x, y) > U(\bar{x}, \bar{y})$, then bundle (x, y) is preferred to bundle (\bar{x}, \bar{y}) .
2. If $U(x, y) = U(\bar{x}, \bar{y})$, then the consumer is indifferent between (x, y) and (\bar{x}, \bar{y}) .

Thus, $U(x, y)$ can be used to rank commodity bundles, in which situation it is known as the **ordinal utility function**. If it is used to measure the levels of utility, it is known as the **cardinal utility function**.

- Ordinal utility function: A utility function that generates a ranking of market baskets in order of most to least preferred.
- Cardinal utility function: A utility function describing by how much one market basket is preferred to another.

The notion of cardinal utility function can be used to measure the happiness of people.

Example 3.3 (Can Money Buy Happiness?) A cross-country comparison shows that individuals living in countries with higher GDP per capita are on average happier than those living in countries with lower per-capita GDP.

The ordinal feature of utility functions implies that the *utility function is unique up to arbitrarily monotonic transformations*. In other words, for any strictly increasing function f (such as the squared function), and the utility function U , its composition $f(U)$ (e.g., $f = U^2$) represents the same preference ordering (indifference map) as U .

To find an indifferent curve from a utility function, we provide the following examples:

Example 3.4 Suppose

$$U(x, y) = x + 2y.$$

Along an indifferent curve the consumer is indifferent between alternative bundles. That is, along an indifference curve $U(x, y) = \bar{U}$ is constant.

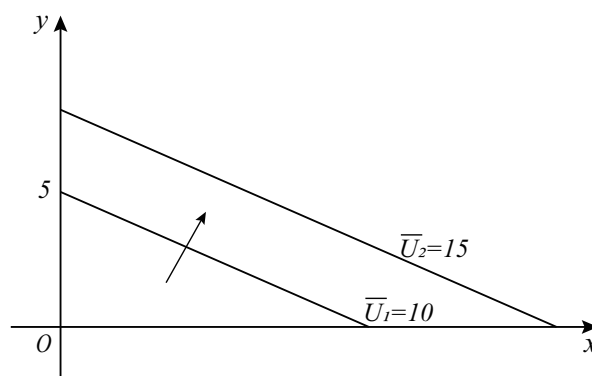


Figure 3.17 Tracing linear indifference curves

Suppose $\bar{U}_1 = 10$. To trace an indifference curve, we find all combinations of (x, y) which satisfy $U(x, y) = \bar{U}_1 = 10 \Rightarrow x + 2y = 10$.

Suppose $\bar{U}_2 = 15 \Rightarrow x + 2y = 15$.

Since $U(x, y) = 10 < U(x, y) = 15$, the latter indifference curve represents bundles preferred to the original set. That is consistent with the indifference curve being further from the origin.

Example 3.5 Suppose

$$U(x, y) = xy.$$

At $\bar{U} = 50 \Rightarrow xy = 50$. Bundles which satisfy this equation include

- $x = 25$ and $y = 2$,
- $x = 10$ and $y = 5$,
- $x = 5$ and $y = 10$,
- $x = 2$ and $y = 25$.

We then have the indifference curve as depicted as in Figure 3.18.

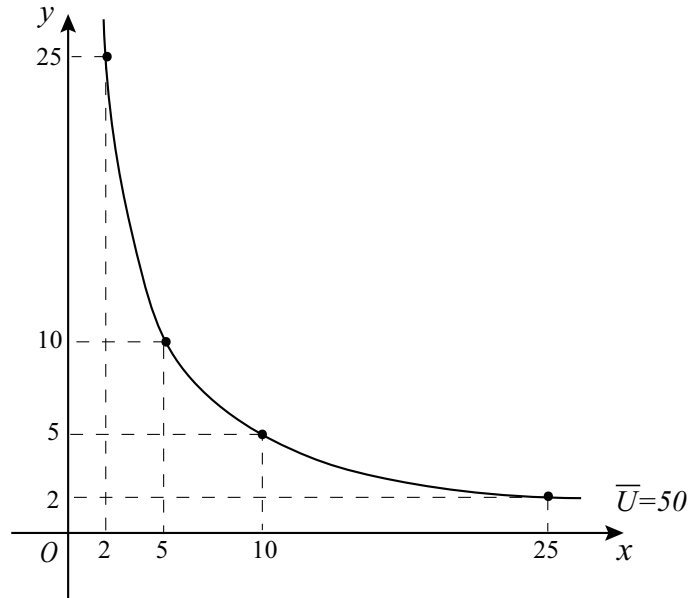


Figure 3.18 Tracing convex indifference curves

Computing MRS from Utility Function

If we know a particular utility function, we can compute MRS of the corresponding indifference curve. Indeed, along an indifference curve represented by a utility level \bar{U} , we have $\Delta\bar{U} = 0$, hence

$$0 = MU_x \times \Delta x + MU_y \times \Delta y.$$

We then have

$$\frac{\Delta y}{\Delta x} = -\frac{MU_x}{MU_y}.$$

Since the slope of an indifference curve is $\frac{\Delta y}{\Delta x} = -MRS_{x,y}$, we have

$$MRS_{x,y} = \frac{MU_x}{MU_y}.$$

Example 3.6 (Example 3.4 continued) Suppose

$$U(x, y) = x + 2y.$$

Since $MU_x = 1$ and $MU_y = 2$, we have

$$MRS_{xy} = \frac{MU_x}{MU_y} = \frac{1}{2}.$$

Example 3.7 (Example 3.5 continued)

$$U(x, y) = xy$$

Since $MU_x = y$ and $MU_y = x$, we have

$$MRS_{xy} = \frac{MU_x}{MU_y} = \frac{y}{x}.$$

Now consider the squared transformation of $U(x, y) = xy$ so that

$$U(x, y) = x^2y^2$$

Since $MU_x = 2xy^2$ and $MU_y = 2x^2y$, we have

$$MRS_{xy} = \frac{MU_x}{MU_y} = \frac{2xy^2}{2x^2y} = \frac{y}{x},$$

which is the same as the one for $U(x, y) = xy$. Once again, it shows that the invariance of utility function to a monotonic transformation.

3.3 Consumer's Optimal Choice

The consumer chooses a bundle (x, y) to maximize their preference subject to the budget constraint. That is, the maximizing market basket must satisfy two conditions based on Assumptions 1-3:

It must be located on the budget line.

It must give the consumer the most preferred combination of goods and services.

There are two cases to consider.

Case 1: Interior solution. Indifference curves are strictly convex and do not cross the axes.

From Figure 3.19, one can see:

- C is too expensive and hence is not affordable for the consumer.
- $B \succ A$.
- Hence B is the utility-maximizing bundle; at this point, the budget line and indifference curve U_2 are tangent.

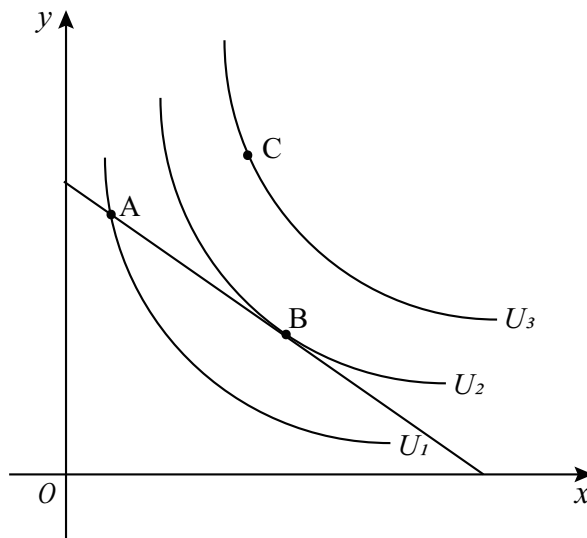


Figure 3.19 Consumer's optimal choice as an interior solution

Thus, at the interior optimal bundle, the following two conditions must be satisfied:

- (1) *The slope of the indifference curve equals the slope of the budget line.* Since the slope of the indifference curve is $-MRS_{xy}$ and the slope of the budget line is $-\frac{p_x}{p_y}$ at B , then we have

$$MRS_{xy} = \frac{p_x}{p_y}. \quad (3.3)$$

- (2) *The choice is on the budget line:*

$$p_x x + p_y y = I. \quad (3.4)$$

In other words, at the point of satisfaction maximization, the MRS between the two goods equals the price ratio, and also satisfies the budget line. Thus, *equations (3.3) and (3.4) fully characterize the consumer's interior optimal choice.*

Note that, since $MRS_{xy} = \frac{MU_x}{MU_y}$, inserting it into the marginal equality condition (3.3), it can be rewritten as

$$\frac{MU_x}{MU_y} = \frac{p_x}{p_y}, \quad (3.5)$$

or equivalently,

$$\frac{MU_x}{p_x} = \frac{MU_y}{p_y}, \quad (3.6)$$

which means the marginal utility per dollar for x equals the marginal utility per dollar for y .

Example 3.8 (Example 3.5 continued again) Suppose that a consumer's utility function is given by

$$U(x, y) = xy,$$

and the prices and income are given by

$$p_x = 2, \quad p_y = 1, \quad I = 100.$$

Substituting $MRS = \frac{y}{x}$, $p_x = 2$ and $p_y = 1$ into equations (3.3) and (3.4), we obtain

$$(1) \frac{y}{x} = \frac{2}{1} \Rightarrow y = 2x.$$

$$(2) 2x + y = 100.$$

Substituting $y = 2x$ from (1) into the budget line (2), we have

$$2x + 2x = 100$$

and then

$$4x = 100.$$

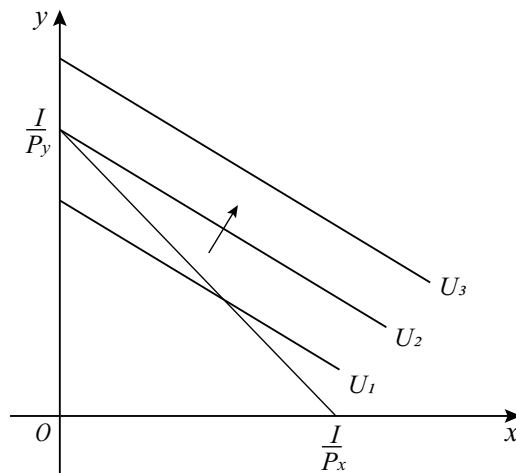
Thus, we have $x^* = 25$ and $y^* = 50$.

Case 2: Corner solution (such as a linear indifference curve):

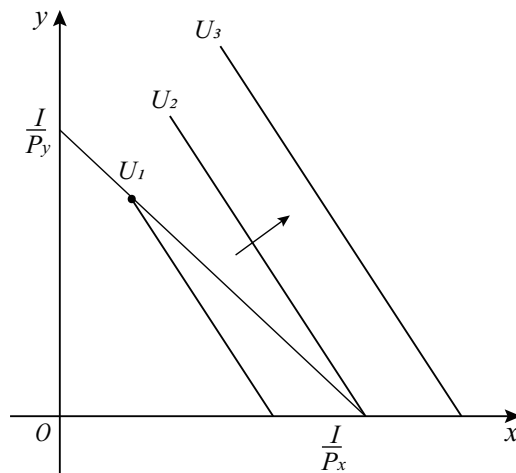
In this case, the marginal rate of substitution for any good is not equal to the slope of the budget line, and the consumer maximizes satisfaction by consuming only one of the two goods. This situation is referred to as a corner solution.

Example 3.9 (Example 3.4 continued again) Consider the utility function $U = x + 2y$. Then $MRS = \frac{1}{2}$. The optimal consumption depends on the slopes of the budget line and the indifference curve.

i) If $MRS_{xy} < \frac{p_x}{p_y}$, the consumer will not consume good x , as depicted in Figure 3.20. For instance, let $p_x = 1$, $p_y = 1$, and $I = 20$. The budget line is $x + y = 20$, and its slope $= -1 \neq -MRS$. So y -intercept $= \frac{I}{p_y} = 20$. Thus $x^* = 0$ and $y^* = 20$.

Figure 3.20 Corner solution: only good y matters

ii) If $MRS_{xy} > \frac{p_x}{p_y}$, the consumer will not consume good y , as depicted in Figure 3.21. For instance, let $p_x = 1$ and $p_y = 3$. So $x^* = \frac{I}{p_x} = 20$ and $y^* = 0$.

Figure 3.21 Corner solution: only good x matters

iii) If $MRS_{xy} = \frac{p_x}{p_y}$, all consumption bundles on the budget are optimal consumptions, as depicted in Figure 3.22. For example, let $p_x = 1$ and $p_y = 2$. The slopes of the budget line and the indifference curves are the

same, and any bundle (x^*, y^*) satisfying $x + 2y = 20$ is optimal.

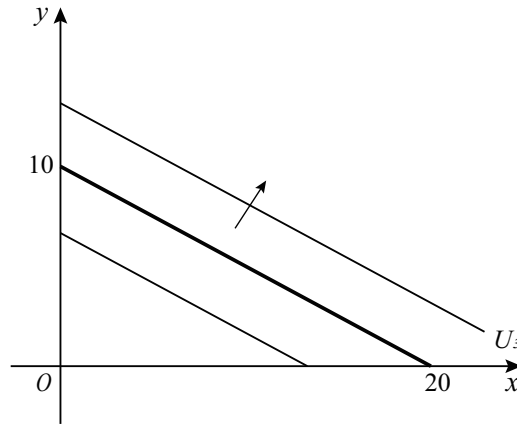


Figure 3.22 Indifference curves and budget line are parallel: infinitely many optimal choices

3.4 The Composite-Good Convention

So far, our analysis has been focused on a two-good world, but the general principles can be extended to a world of many goods. While it is difficult to represent many goods on a two-dimensional graph, we can simplify the analysis by treating some goods as a composite good.

Suppose there are many goods, x, y, \dots, z . We can measure the consumption of good x by treating the other goods, (y, \dots, z) , as a composite good. Consumption of the composite good is gauged by total outlays on it, in other words, total outlays on all goods other than x . Thus, all analysis and conclusions for a two-good world also hold for a world of many goods.

Note that the price of the composite good is set to one. Therefore, the slope of the budget line is $-\frac{p_x}{1} = -p_x$, and the marginal rate of substitution is $\frac{p_x}{1} = p_x$.

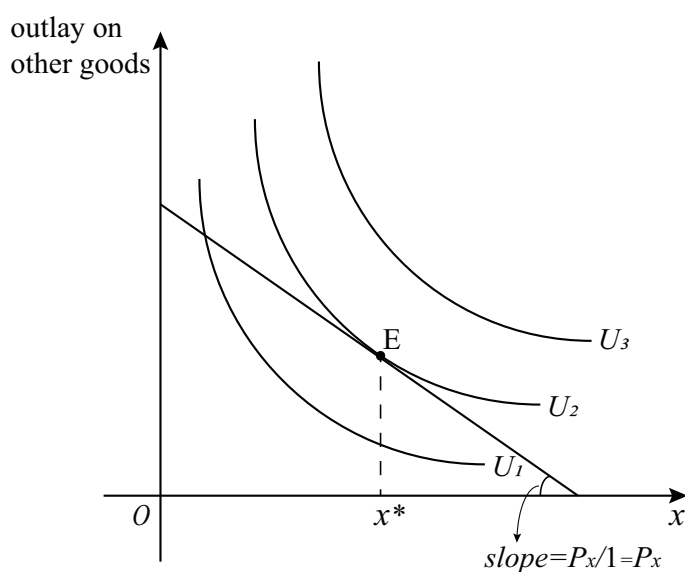


Figure 3.23 The composite-good convention: optimal choice with more than two goods

3.5 Revealed Preference

Revealed preference theory suggests that a consumer's preferences can be inferred from their observed choices. If a consumer chooses one market basket over another and the chosen market basket is more expensive than the alternative, then the consumer must prefer the chosen market basket.

In the examples shown in Figures 3.24 and 3.25, the consumer is faced with different budget lines and chooses different market baskets. By analyzing these choices, we can determine the consumer's preferences. For instance, in Figure 3.24, the consumer chooses market basket A over B when faced with budget line l_1 , and chooses B over D when faced with l_2 . This implies that A is preferred to B , and B is preferred to D . Whereas A is preferred to all market baskets constrained by l_1 and l_2 , all baskets greater than A are preferred to A .

Similarly, in Figure 3.25, the consumer chooses market basket E over A when faced with l_3 , and chooses G over A when faced with l_4 . This

implies that both E and G are preferred to A . Whereas A is preferred to all market baskets by l_1 and l_2 , all market baskets in the upper shaded area are preferred to A .

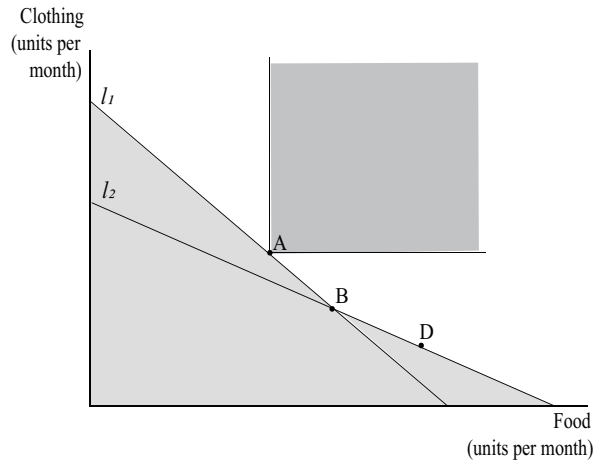


Figure 3.24 Revealed preference: Two budget lines

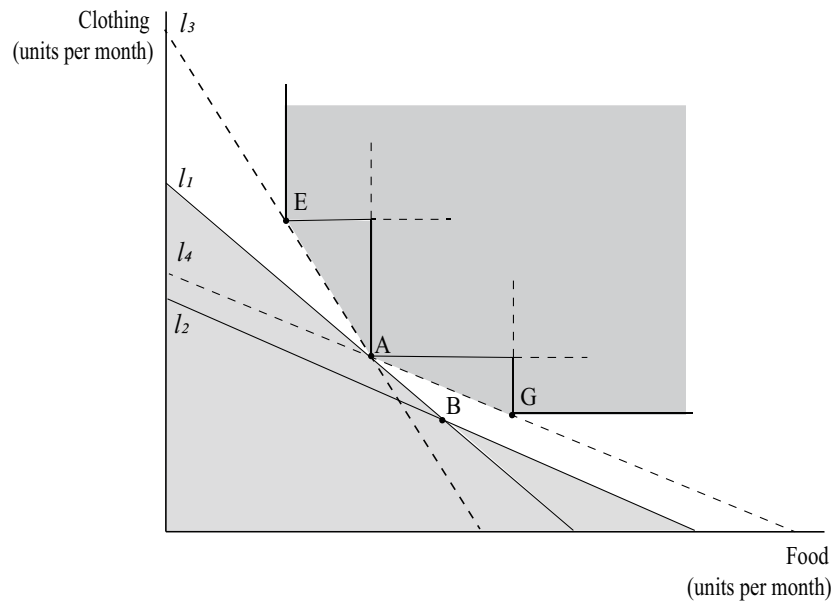


Figure 3.25 Revealed preference: Four budget lines

As more and more budget lines are added, the consumer's preferences

can be further revealed. The resulting set of preferences can be used to construct an indifference curve map, which shows all combinations of goods that are equally preferred by the consumer. This map can be used to make predictions about the consumer's behavior in different situations, such as when faced with new budget constraints or changes in prices.

Chapter 4

Individual and Market Demand

This chapter discusses the influences of income and price changes, and how to determine individual and market demand.

4.1 Effect of Income Changes

An increase in income, with the prices of all goods fixed, causes consumers to alter their choice of market baskets.

Income-consumption curve (ICC): A curve that traces the utility-maximizing combinations of two goods as a consumer's income changes.

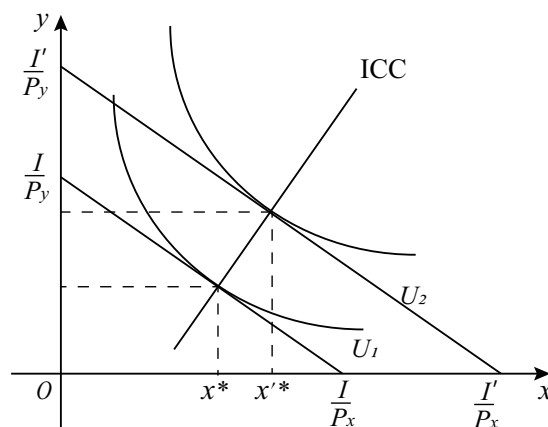


Figure 4.1 Tracing an income consumption curve

Figure 4.1 shows how an ICC can be traced by changing income while holding prices constant. At each point along the price consumption curve, utility is maximized when all income is spent.

As shown in Figure 4.1, the demand for both goods x and y increases when income rises.

Normal good: A good for which an increase in a person's income leads to an increase in the consumption of that good when the prices of other goods remain fixed. Most goods are normal goods, especially when income is low.

Inferior good: A good for which an increase in a person's income leads to a decrease in the consumption of that good when the prices of other goods remain fixed.

As income continuously increases, more and more goods become inferior goods. Figure 4.2 shows an ICC for a situation where good y is an inferior good.

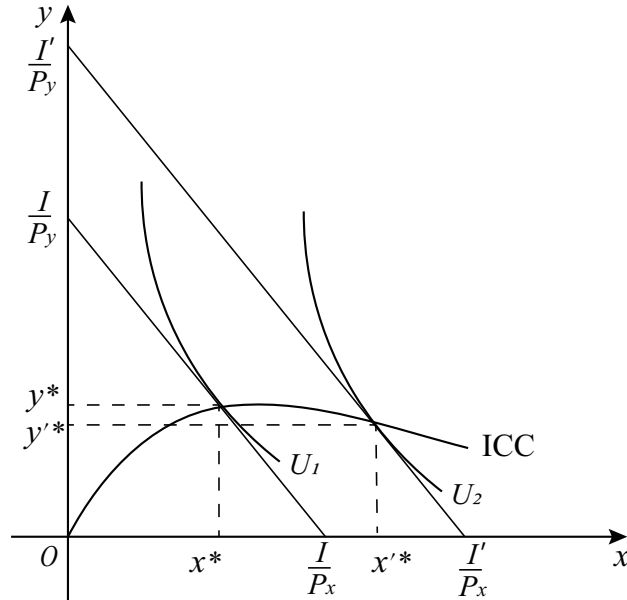


Figure 4.2 Income-consumption curve when good y is an inferior good

In Figure 4.2, $I' > I$, $x'^* > x^*$, and $y'^* < y^*$. Thus, x is a normal good

and y is an inferior good. This curve illustrates that, for all income levels, only x is a normal good. If there are only two goods in the economy, they cannot both be inferior goods at the same time.

Engel curve: A curve that shows the relationship between the quantity of a good consumed and a consumer's income.

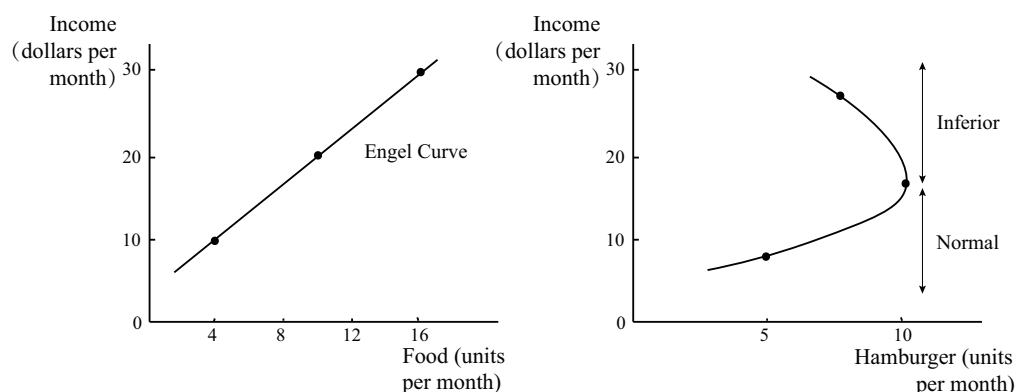


Figure 4.3 Engel curves

In the left diagram of Figure 4.3, food is a normal good and the Engel curve is upward-sloping, indicating that as income increases, the quantity of food consumed also increases.

In the right diagram of Figure 4.3, hamburger is a normal good for incomes less than \$18 per month and becomes an inferior good for incomes greater than \$18 per month. This means that the income-consumption curve has a positive slope for low incomes, but takes a negative slope for even higher incomes.

Example 4.1 (Consumer Expenditures in the United States) Engel curves can be a useful tool to analyze how consumer spending varies among different income groups. Based on the data in Table 4.1, it can be observed that health care and entertainment are normal goods as their expenditures increase with income. However, rental housing is an inferior good for incomes above \$40,000, indicating that as income increases, consumers tend to spend less on rental housing and more on other goods and services.

Expenditures	Less than 19,999	10,000- 29,999	20,000- 39,999	30,000- 49,999	40,000- 59,999	50,000- 69,999	70,000 and above
Entertainment	1,038	1,165	1,407	1,969	2,131	2,548	4,655
Owned Dwelling	1,770	2,134	2,795	3,581	4,198	5,566	11,606
Rented Dwelling	3,919	3,657	4,054	3,878	4,273	3,812	3,072
Health Care	1,434	2,319	3,124	3,539	3,709	4,702	6,417
Food	3,466	3,706	4,432	5,194	5,936	6,486	10,116
Clothing	798	766	960	1,321	1,518	1,602	2,928

Table 4.1: Annual U.S. Household Consumer Expenditures

The Supplemental Nutrition Assistance Program (SNAP)

The Supplemental Nutrition Assistance Program (SNAP), formerly known as the Food Stamp Program, is a federal program that provides food-purchasing assistance for low- and no-income people. Approximately 1 in 7 Americans receive aid through SNAP. If recipients only have SNAP funds, they cannot withdraw cash or use their cards to pay for housing or non-food items. What are the effects of this program?

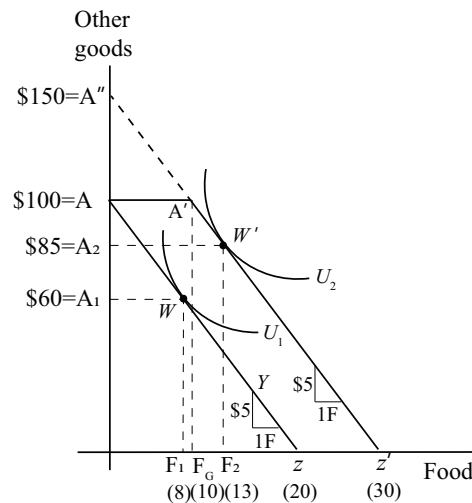


Figure 4.4 Evaluating SNAP using consumer theory

Consumer theory can be used to evaluate the program. In Figure 4.4, we consider a specific example in which a consumer receives \$50 worth of SNAP funds per week. We assume the consumer has a weekly income of \$100 and the price of food is $p_f = 5$ per unit.

The pre-subsidy budget line is AZ . The SNAP subsidy shifts the budget line to $AA'Z'$. Over the AA' range, the budget line is horizontal since the \$50 in free SNAP funds permits the recipient to purchase up to 10 units of food while leaving their entire income of \$100 to be spent on other goods. Over 10 units of food, the consumer has to pay for it by \$5 per unit. Thus, the $A'Z'$ portion of the budget line has a slope of -5 . Note that this new budget line is not straight, but has a kink at A' .

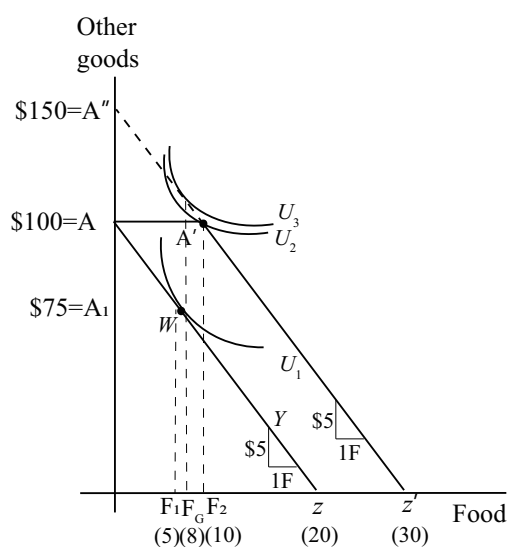


Figure 4.5 Another illustration of the effect of SNAP

The SNAP funds will affect the recipient in one of two ways. Figure 4.4 shows one possibility. If the consumer spends more than \$50 on food, the equilibrium, W' , occurs on the $A'Z'$ portion of the budget line. The consequences of the SNAP funds are the same as when the consumer receives a cash grant of \$50, leading to the budget line $A''Z$.

Figure 4.5 show another possible outcome of the SNAP subsidy. With

a direct cash grant of \$50, the consumer would be better off on the indifference curve U_3 , which is prohibited by the SNAP funds. The consumer has to choose among the options on the $AA'Z'$ budget line, and the best choice is the kink point A' . Therefore, the consumer would be better off if the subsidy were given as cash instead of as SNAP funds.

Similar arguments and figures could be used to discuss a college trust fund. When given a college trust fund that must be spent on education, the student moves from W to A' , a corner solution. If, however, the trust fund could be spent on other consumption as well as education, the student would be better off on the indifference curve U_3 .

4.2 Effect of Price Changes: Deriving the Demand Curve

An increase in the price of a good, with the prices of all other goods and income fixed, can also cause consumers to alter their choice of market baskets.

Price-consumption curve: A curve that traces the utility-maximizing combinations of two goods as the price of one changes.

Individual demand curve: A curve that relates the quantity of a good that a single consumer will buy to its price.

There are two approaches to derive the **demand curve** of a consumption good from utility maximization.

1. Graphical derivation

To find the demand for good x , we change the price of x (p_x) while holding the prices of all other goods and income constant.

Let $p_x > p_x' > p_x''$. We can obtain the baskets that maximize utility for these prices and have other optimal baskets in a similar way. Connecting these points smoothly, we can get the **price-consumption curve** along

4.2. EFFECT OF PRICE CHANGES: DERIVING THE DEMAND CURVE⁹⁵

which *utility is maximized and all income is spent*, as depicted in the upper diagram of Figure 4.6.

The lower diagram in Figure 4.6 gives the demand curve, which relates the price of good x to the quantity demanded. Thus, **demand** for good x is a function of p_x , p_y , and I .

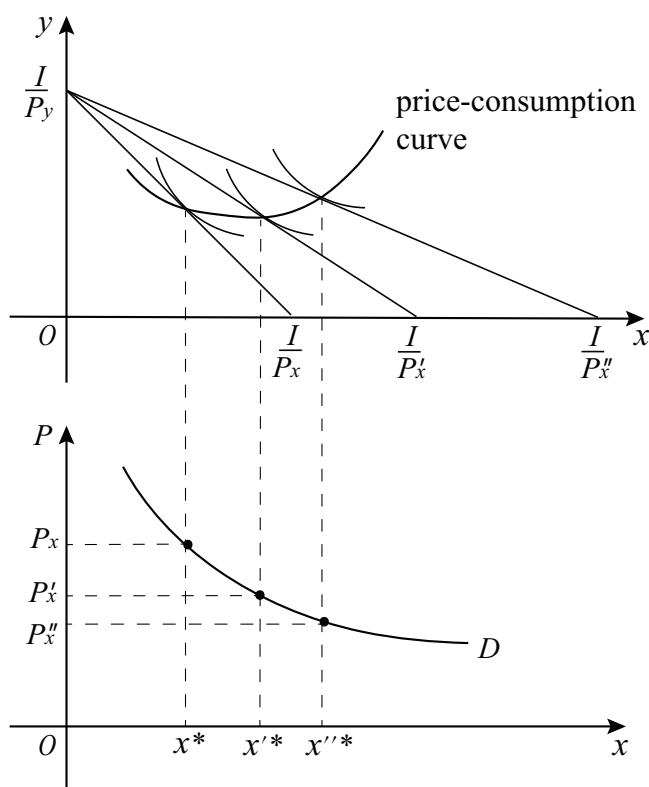


Figure 4.6 Deriving demand curve from utility maximization

2. Algebraic derivation

Use the two conditions for utility maximization:

$$MRS = \frac{p_x}{p_y}, \quad (4.1)$$

and

$$p_x x + p_y y = I. \quad (4.2)$$

Solving equation (4.1) and (4.2), we can find x^* and y^* as functions of p_x , p_y and I . Let illustrate with the following example.

Example 4.2 Suppose that preferences are represented by Cobb-Douglas utility function

$$U(x, y) = x^{\frac{1}{3}}y^{\frac{2}{3}}.$$

Then,

$$MRS = \frac{y}{2x}.$$

Equalizing MRS and $\frac{p_x}{p_y}$, we have

$$\frac{y}{2x} = \frac{p_x}{p_y},$$

and then

$$y = \frac{2xp_x}{p_y}.$$

Substituting $y = \frac{2xp_x}{p_y}$ into the budget line, we have

$$p_x x + p_y \left(\frac{2xp_x}{p_y} \right) = I$$

or

$$3p_x x = I.$$

Therefore, we obtain

$$x^* = \frac{I}{3p_x} = D_x.$$

Let $I = 50$ and $p_y = 2$. Then $x^* = \frac{50}{3p_x}$.

To derive the demand curve, consider the following numerical illustration:

- $p_x = 1 \Rightarrow x = \frac{50}{3} = 16.6,$
- $p_x = 5 \Rightarrow x = \frac{50}{15} = \frac{10}{3} = 3.3,$
- $p_x = 10 \Rightarrow x = \frac{50}{30} = \frac{5}{3} = 1.6.$

4.3. INCOME AND SUBSTITUTION EFFECTS OF A PRICE CHANGE⁹⁷

Connecting these points and other points obtained in a similar way smoothly, we can have an indifference depicted in Figure 4.7.

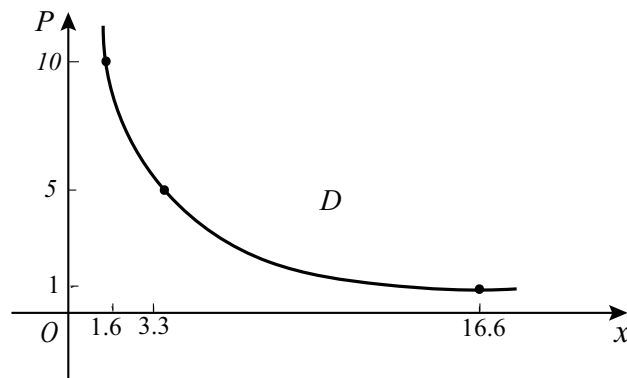


Figure 4.7 A downward-sloping and convex-to-origin demand curve

For a general Cobb-Douglas utility function:

$$u(x, y) = x^a y^{1-a}, \quad 0 < a < 1,$$

by the same way, we can derive the demand functions for x and y :

$$x(p_x, p_y, I) = \frac{aI}{p_x}$$

and

$$y(p_x, p_y, I) = \frac{(1-a)I}{p_y}.$$

4.3 Income and Substitution Effects of a Price Change

Goods can have different relationships with each other, which can affect the consequences of a price change. Specifically:

- Two goods are **substitutes** if an increase in the price of one leads to an increase in the demand for the other.

- Two goods are **complements** if an increase in the price of one leads to a decrease in the demand for the other.
- Two goods are **independent** if a change in the price of one has no effect on the demand for the other.

The fact that goods can be complements or substitutes suggests that when studying the effects of price changes in one market, it may be important to look at the consequences in related markets.

A change in the price of a good has two effects:

- **Substitution effect:** The change in consumption of a good associated with a change in its price, with the **level of utility held constant**.

Say, when the price of a good falls, consumers will tend to buy more of the good that has become cheaper and less of those goods that are now relatively more expensive. This response to a change in the relative prices of goods is called the substitution effect.

- **Income effect:** The change in consumption of a good resulting from a change in purchasing power, with **prices held constant**.

Say, when the price of a good falls, consumers enjoy an increase in real purchasing power.

The total effect of a change in price is given theoretically by the sum of the substitution effect and the income effect:

$$\text{Total effect} = \text{substitution effect} + \text{income effect}$$

Income and Substitute Effects: Normal Good

In Figure 4.8, the consumer is initially at A on budget line RS and U_1 . With a decrease in the price of food, the consumer moves to B on the

4.3. INCOME AND SUBSTITUTION EFFECTS OF A PRICE CHANGE⁹⁹

new budget line RT and U_2 . When the price of food falls, consumption increases by F_1F_2 as the consumer moves to B . The resulting change in food purchased can be broken down into substitution and income effects.

Since the real purchasing power increases due to the price decrease, to find the substitution effect, the consumer should spend less income in order to keep the same utility level as U_1 . Note that any parallel line of RT has the same slope.

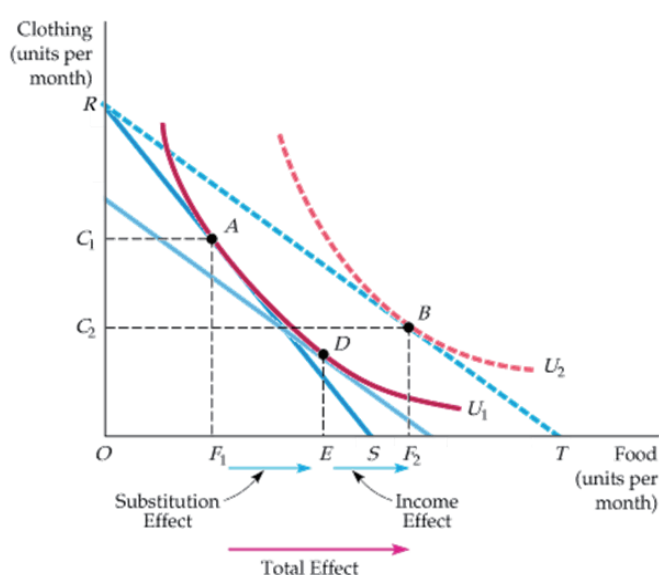


Figure 4.8 Income and substitution effects: normal good

Thus, the way to determine the substitution effect (and consequently income effect) is simply as follows:

Draw a parallel line of the new budget line RT , which is tangent to the initial indifference curve U_1 .

That is, we shift the new budget line RT parallelly toward the initial indifference curve U_1 and stop at the tangent point D on U_1 . Thus, *the two points (e.g., A and D) on the indifference curve U_1 determine the substitution effect*, which is F_1E , while maintaining the same level of satisfaction.

The remaining change, from D on U_1 to B on U_2 , is the **income effect**. The difference between the budget line RT and its parallel budget line is EF_2 that represents the effect of the increase in real purchasing power on food consumption, resulting in the increase in utility from U_1 to U_2 .

Because food is a normal good, the income effect EF_2 is positive, hence their income and substitute effects move in the same direction.

Income and Substitute Effects: Inferior Good

In Figure 4.9, the consumer is initially at A on budget line RS . With a decrease in the price of food, the consumer moves to B . Again, the resulting change in food purchased can be broken down into a substitution effect, F_1E (associated with a move from A to D), and an income effect, EF_2 (associated with a move from D to B). In this case, food is an inferior good since the income effect is negative. Thus, the *income and substitute effects move in the opposite directions for inferior good*.

However, since the substitution effect dominates the income effect, the decrease in the price of food leads to an increase in the quantity of food demanded.

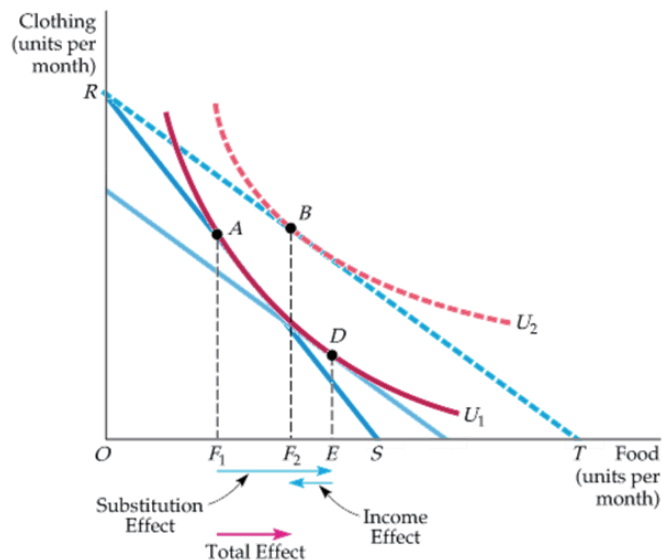


Figure 4.9 Income and substitution effects: inferior good

Income and Substitution Effects: Giffen Good

So far, we have learned that the demand curves are typically downward-sloping, meaning that as the price of a good increases, the quantity demanded of that good decreases.

However, there is a rare case in which the law of demand does not hold for a specific type of inferior good, known as a **Giffen good**. A Giffen good is a good for which a decrease in price leads to a decrease in the quantity demanded. The reason for this counterintuitive phenomenon is that *for a Giffen good, the income effect is so strong that it dominates the substitution effect*.

To illustrate this, consider Figure 4.10, which shows the demand curve for a Giffen good. A lower price could lead to less consumption. The consumer purchases less of food when its price falls. Note that the indifference curves that produce this result are downward-sloping, nonintersecting, and convex; that is, they do not contradict any of the basic assumptions about preferences.

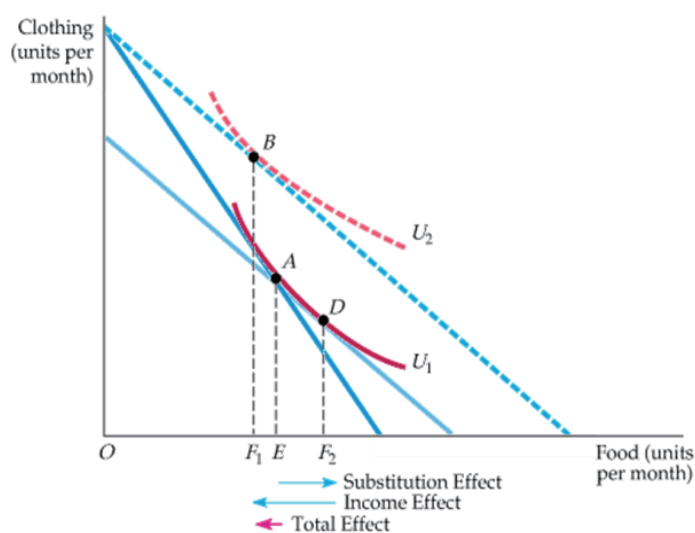


Figure 4.10 Upward-sloping demand curve: the Giffen good

Because the income effect F_2F_1 is negative (so that substitution effect and income effect move in the opposite directions,) and dominates the

substitution effect EF_2 , the decrease in the price of food leads to a lower quantity of food demanded.

Thus, a Giffen good is fully characterized by the following two features:

- (1) it must be inferior good;
- (2) its income effect dominates its substitution effect (in absolute value).

That is, *a Giffen good is the special subset of inferior goods in which the income effect dominates the substitution effect.*

Therefore, *a Giffen good must be an inferior good, but an inferior good may not be a Giffen good.*

4.4 From Individual to Market Demand

We have derived the demand curve for an individual consumer. To obtain the market demand curve, we simply add all individual demands at given prices. Two important points to note are:

1. The market demand curve will shift to the right as more consumers enter the market.
2. Factors that influence the demands of many consumers, such as changes in income or preferences, will also affect market demand.

The aggregation of individual demands into the market becomes important when market demands are built up from the demands of different demographic groups or from consumers located in different areas.

Example 4.3 Consider the numerical example with two consumers. Making the summation of two individuals' demand, we obtain the market demand as shown in Table 4.3 and Figure 4.11.

p_x for good x	D_x^A for A	D_x^B for B	Market demand D_x
\$1	10	12	22
\$2	7	5	12
\$3	3	1	4

Table 4.2: Determining the market of demand curve

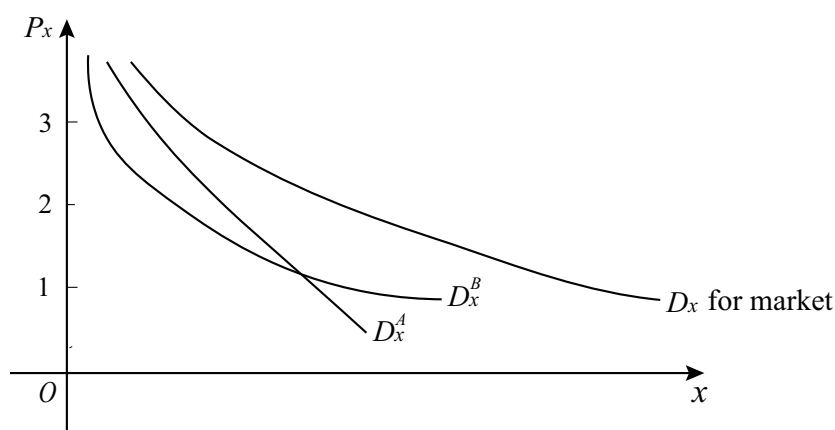


Figure 4.11 From individual demand to market demand

4.5 Consumer Surplus

Consumers purchase goods and services because they are better off from doing so; otherwise, the purchase would not take place. The term **consumer surplus** refers to the net benefit, or gain.

Consumer surplus: Difference between what a consumer is willing to pay for a good and the amount actually paid.

To calculate consumer surplus for a specific amount of a good or service, we can ask the question: What is the maximum amount you would be willing to pay, and what is the total cost? Consumer surplus is then defined as the difference between the total benefit and total cost.

$$\text{Consumer surplus} = \text{Total benefit} - \text{Total cost.}$$

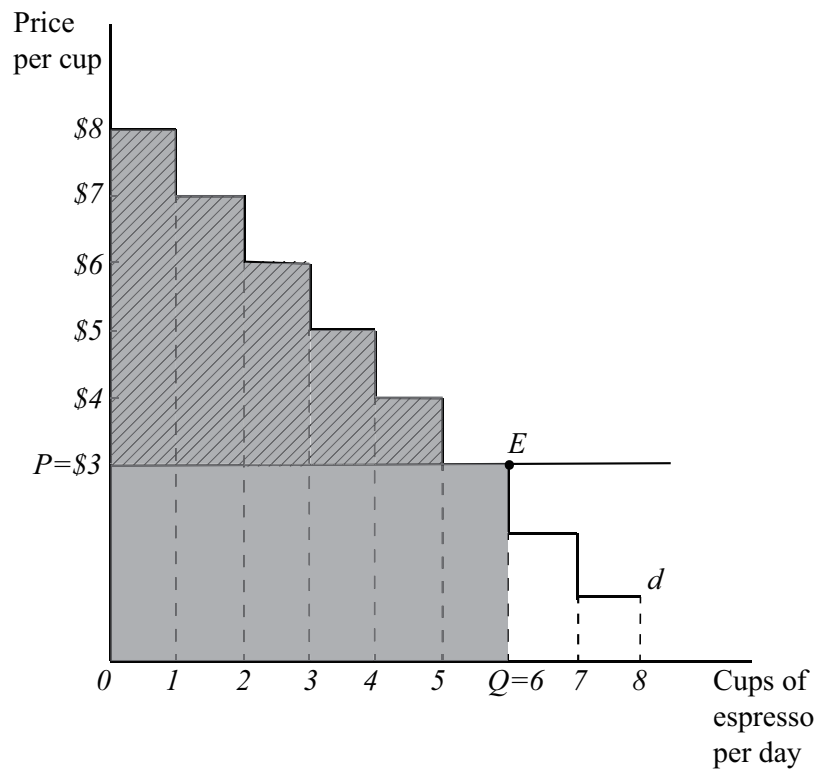


Figure 4.12 The discrete approach of calculating consumer surplus

Consumer surplus can be illustrated graphically using a demand curve. To see this, let us consider a specific example. Suppose that a person purchases 6 cups of espresso at the price $p = \$3$. The total cost $= 3 \times 6 = 18$. Total benefit from purchasing 6 units at a price \$3, however, is the sum of marginal benefit (the sum of 6 units shaded rectangles of Figure 4.12), i.e.,

$$\text{total benefit} = \$8 + \$7 + \$6 + \$5 + \$4 + \$3 = 33.$$

Thus, the consumer surplus $= \text{total benefit} - \text{total cost} = 33 - 18 = 15$.

In general, with a smooth demand curve indicated in Figure 4.13, consumer surplus equals the area TEP .

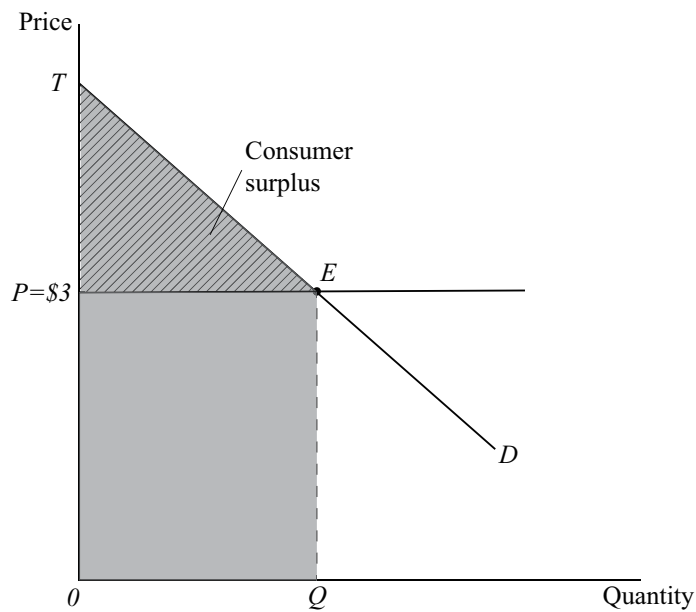


Figure 4.13 Consumer surplus under a downward-sloping continuous demand curve

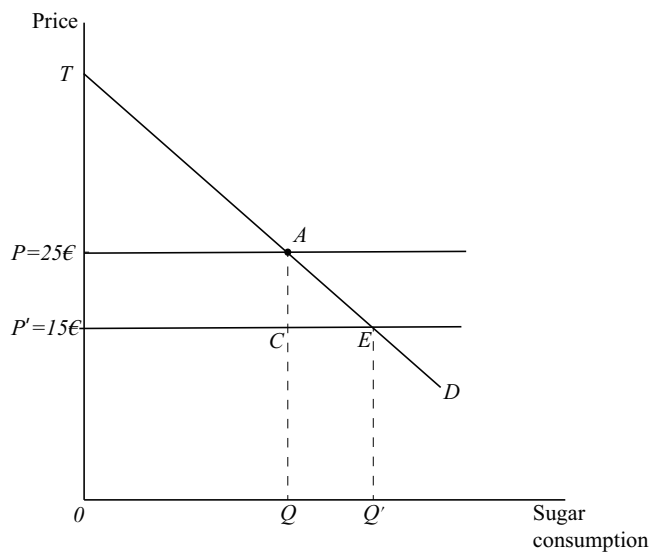


Figure 4.14 The effect of a price reduction on consumer surplus

The concept of consumer surplus can also be used to identify the net benefit of a change in the price of a commodity. In Figure 4.14, at a price

of 25 cents per unit, consumer surplus is TAP . At a price of 15 cents per unit, consumer surplus is TEP' . The increase in consumer surplus from the price reduction is thus the shaded area $PAEP'$, which is a measure of the benefit to consumers of a reduction in the price from 25 to 15 cents.

Consumer surplus, when combined with producer surplus, can be used to evaluate alternative market structures and public policies that affect consumer and producer behavior in those markets.

4.6 Network Externalities

Network externality occurs when an individual's demand for a good depends on the purchases of other individuals.

Positive network externality occurs when the quantity of a good demanded by a typical consumer increases in response to the growth in purchases of other consumers (e.g., social networks like telephones, emails, Facebook, TikTok, WeChat, and fads).

Negative network externality occurs when the quantity demanded decreases in response to the growth in purchases of other consumers (e.g., when an individual desires to own exclusive or unique goods).

Bandwagon Effect

Positive network externalities give rise to the bandwagon effect.

Positive network externality: The quantity of a good demanded by a typical consumer increases in response to the growth in purchases of other consumers (e.g., social network—telephones, emails, Facebook, Tik Tok, WeChat; toys and fads etc.).

Negative network externality: The quantity demanded decreases to the growth in purchases of other consumers (e.g., an individual has the desire to own exclusive or unique goods).

Bandwagon Effect

The existence of positive network externalities gives rise to Bandwagon effect.

Bandwagon effect: Positive network externality in which a consumer wishes to possess a good in part because others do, i.e., to have a good because of the perception that almost everyone else has it.

With a positive network externality, the quantity of a good that an individual demands grows in response to the growth of purchases by other individuals. Here, as the price of the product falls from \$30 to \$20, the bandwagon effect causes the demand for the good to shift to the right, from D_{40} to D_{80} .

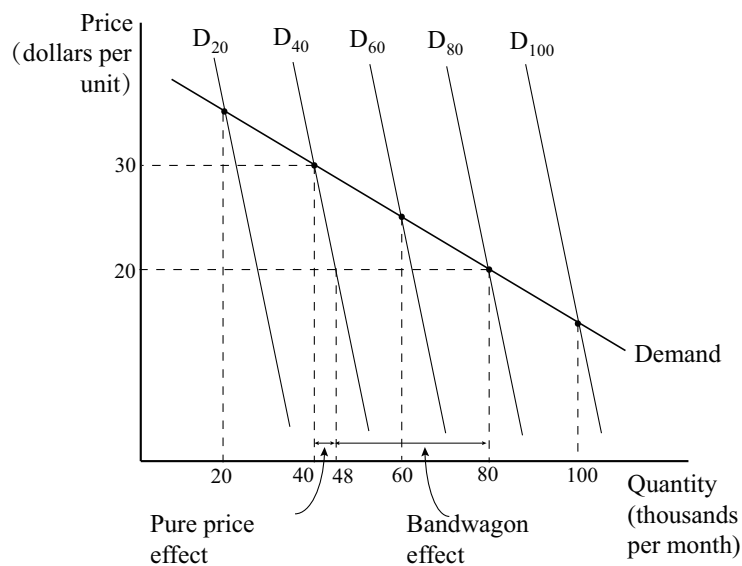


Figure 4.15 Positive network externalities: Bandwagon effect

Positive network externalities have been crucial drivers for many modern technologies over many years.

Example 4.4 (Facebook (Meta)) By early 2011, with over 700 million users, Meta (formerly known as Facebook) became the world's second most

Year	Facebook (Meta) Users (Millions)	Hours Per User Per Month
2004	1	—
2005	5.5	—
2006	12	<1
2007	50	2
2008	100	3
2009	350	5.5
2010	500	7
2011	766	7.5
2012	980	8.5
2013	1171	9
2014	1334	10
2015	1517	10.5
2016	1654	11

Table 4.3: Facebook Users

visited website (after Google). As of 2022, there are about 2 billion daily users. A strong positive network externality was central to Facebook's success.

Snob Effect

The existence of negative network externalities gives rise to the snob effect.

Snob effect: A negative network externality in which a consumer wishes to own an exclusive or unique good.

The quantity demanded of a "snob" good is higher when the number of people who own it is lower (e.g., garments specially designed by a well-known fashion designer, limited edition watches, high-end cars, etc.).

Thus, the snob effect is a negative network externality in which the quantity of a good that an individual demands falls in response to the growth of purchases by other individuals.

In Figure 4.16, as the price falls from \$30,000 to \$15,000 and more people buy the good, the snob effect causes the demand for the good to shift

to the left, from D_2 to D_6 .

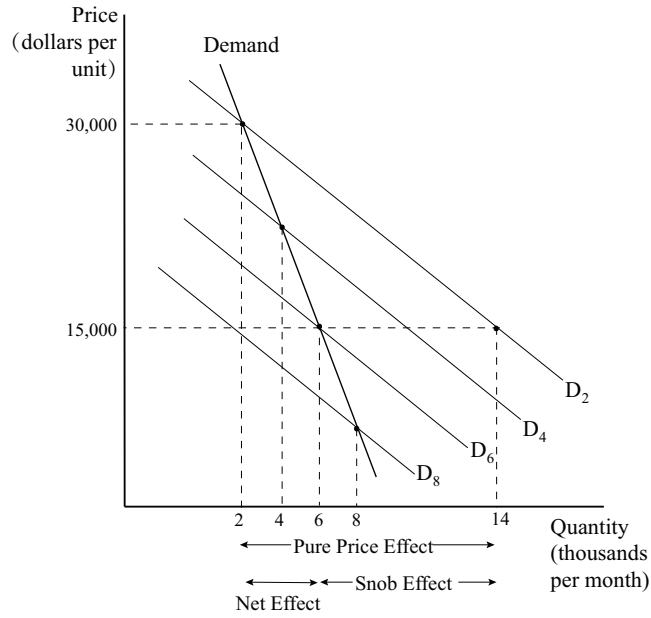


Figure 4.16 Negative network externalities: Snob effect

Part III

Supply Side of Market

Part 2 presents the theoretical core of production and competitive firm's supply and market supply.

Chapter 6

Theory of Production

In this chapter and the next we discuss the theory of the firm, which describes how inputs (such as labor, capital, and raw materials) can be transformed into outputs, how a firm makes cost-minimizing production decisions, and how the firm's resulting cost varies with its output.

6.1 The Technology of Production

Firm: any organization that engages in production.

The production decisions of firms can be understood in three steps:

1. **Production Technology:** How inputs (also known as the factors of production) can be transformed into outputs.
2. **Cost Constraints:** What possible combinations of inputs can be used with a given expenditure on production.
3. **Input Choices:** Just as a consumer is constrained by a limited budget, the firm is concerned about the cost of production and the prices of labor, capital, and other inputs.

We can divide inputs into the broad categories of labor, materials and capital, each of which might include more narrow subdivisions.

- **Labor inputs** include skilled workers (financial analyst, carpenters, engineers) and unskilled workers (cleaners, manual workers), as well as the entrepreneurial efforts of the firm's managers.
- **Raw materials** include steel, plastics, electricity, water, and any other goods that the firm buys and transforms into final products.
- **Capital** includes land, buildings, machinery and other equipment, as well as inventories.

Production Function: A relationship between inputs and outputs that identifies the *maximum output* produced by a firm for every combination of inputs with a given technology.

A production is **technologically efficient** if the maximum quantity of a commodity can be produced by *each* specific combination of inputs. Thus, *production specified by production function is technologically efficient*. If a firm is rational, it should always operate in a technologically efficient way to produce outputs.

We can present a production function in tabular, graphical, or mathematical form. For example, in mathematical form, we have

$$q = F(K, L),$$

where q is the number of units of output, K the number of units of capital input, L the number of units of labor input, and F is production function.

A common production function used as an example in economics is the so-called **Cobb-Douglas production function**:

$$F(K, L) = AK^\alpha L^\beta,$$

where A is a parameter that can be interpreted as total productivity.

Suppose that $\alpha = \beta = \frac{1}{2}$ and $A = 1$. We have

$$q = K^{\frac{1}{2}}L^{\frac{1}{2}}.$$

Then, for a particular combination of inputs, say, $K = 16$ and $L = 36$, the maximum output obtainable with this technology is

$$q = (16)^{\frac{1}{2}}(36)^{\frac{1}{2}} = 4 \times 6 = 24.$$

6.2 Production in the Short Run

We first define the relevant concepts as follows:

- **Short run:** A period of time in which changing the employment levels of some inputs is impractical. It is a time period in which at least one input is fixed.
- **Fixed inputs:** Production factors that cannot be varied over the time period involved.
- **Long run:** A period of time in which the firm can vary all its inputs. For example, for a factory, short run is long enough to hire an extra worker but is not long enough to build an extra production line.

6.2.1 Various Product Curves in the Short Run

Assuming two factors of production, labor (L) and capital (K), in the short run, we usually assume that K is fixed and L is a variable input. Given a fixed K , the firm can vary L to produce different amounts of output. We use the following concepts to describe production in the short run:

- **Total Product (TP):** The total output produced.
- **Average Product (AP):** Output per unit of a variable factor. That is, $AP = \text{total product}/\text{variable factor}$. For example, the average product of labor is given by:

$$AP_L = \frac{TP}{L}.$$

- **Marginal Product (MP):** The change in output resulting from a change in the amount of the input, holding the quantities of other inputs constant. For example, the marginal product of labor is given by:

$$MP_L = \Delta TP / \Delta L.$$

The Average-Marginal Products Relationship

- If $MP_L > AP_L$, then AP_L must rise.
- If $MP_L < AP_L$, then AP_L must fall.
- If $MP_L = AP_L$, then AP_L reaches its maximum.

Note that if MP_L is constant, AP_L is identical to MP_L , hence constant in L .

Example 6.1 Suppose $q = F(K, L) = 10KL^2$. Then $AP_L = \frac{q}{L} = 10KL$ and $MP_L = \partial q / \partial L = 20KL$. It can be verified that $MP_L > AP_L$ implies AP_L increases.

Fixed amount of land	Amount of labor (L)	Total product (TP_L)	Average product of labor (AP_L)	Marginal product of labor (MP_L)
5	0	0	---	---
5	1	50	50	50
5	2	150	75	100
5	3	300	100	150
5	4	400	100	100
5	5	480	96	80
5	6	540	90	60
5	7	580	83	40
5	8	610	76	30
5	9	610	68	0
5	10	580	58	-30

Table 6.1: Production with one variable input (labor)

Example 6.2 (Production with One Variable Input (Labor)) Consider the numerical example depicted in Table 6.1.

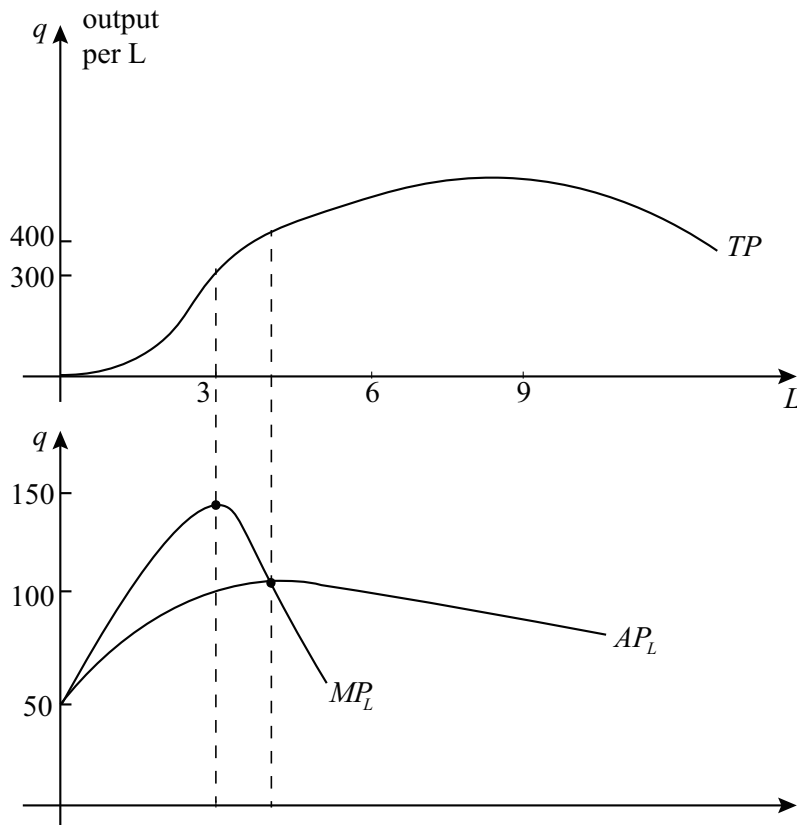


Figure 6.1 The relationship between TP, MP and AP

The total output curve in the upper diagram in Figure 6.1 shows the output produced for different amounts of labor input. The average and marginal products in the lower diagram in Figure 6.1 can be obtained (using the data in Table 6.1) from the total product curve.

With 3 units of labor, the marginal product is 150. The average product of labor, however, is 100, and then the average product of labor continues to increase. With 4 units of labor, the marginal product of labor and the average product of labor intersect, and the average product of labor reaches its maximum at this point.

When the labor input is 5 units, the marginal product is below the average product, so the average product is falling. Once the labor input exceeds 9 units, the marginal product becomes negative, so that total output falls as more labor is added. When total output is maximized, the slope of the tangent to the total product curve is 0, as is the marginal product. Beyond that point, the marginal product becomes negative.

6.2.2 The Geometry of Production Curves

1. *Average product ($AP_L = \frac{q}{L}$) is the slope of the line which connects the origin to the TP curve.*

This is because the slope of any line from the origin to a point on the TP curve has slope = $\frac{\Delta q}{\Delta L} = \frac{q-0}{L-0} = \frac{q}{L}$. At point C in Figure 6.3, AP_L reaches its maximum since the ray OC is the steepest ray from the origin that still touches the TP curve.

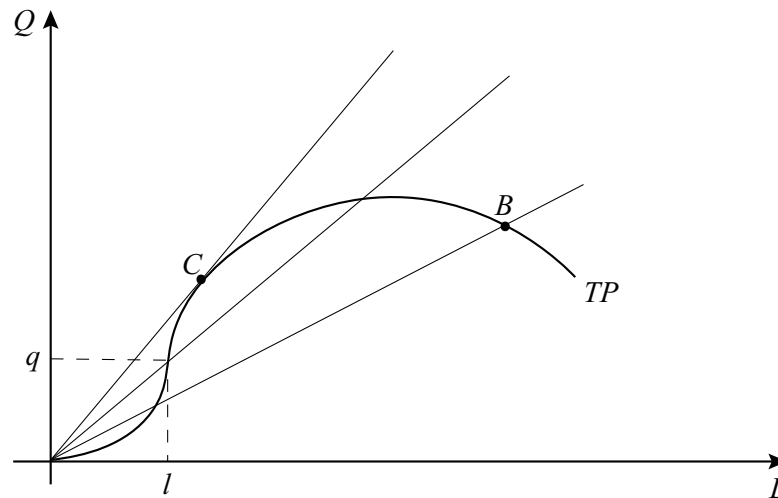


Figure 6.2 The geometry of production curves

2. *Marginal product ($MP_L = \frac{\Delta q}{\Delta L}$) is the slope of the TP curve.*

The following law of diminishing marginal product (DMP) reveals the shape of the TP curve: MP_L increases to a point and then decreases. That

is, the slope of TP first increases and then eventually starts to decrease. When $MP_L = 0$, the TP curve reaches its maximum.

6.2.3 The Law of Diminishing Marginal Returns

The law of diminishing (marginal) returns (DMR): As the amount of a variable input increases with *a fixed amount of other inputs and fixed technology*, a point is reached beyond which the marginal product of the variable input begins to fall.

In short, *the marginal product of a variable input eventually decreases with a given technology and other inputs fixed.*

Example 6.3 A farm adds fertilizer (variable) to an acre of land (fixed); and the numerical example is as follows:

K,L	q	MP_L	Diminishing Returns
1,0	0	–	
1,1	10	10	
1,2	30	20	↓
1,3	40	10	↓
1,4	45	5	↓
1,5	48	3	↓

Table 6.2: Production with one variable input (labor)

Remarks on DMR

Technology Improvement. Labor productivity (output per unit of labor for an economy or industry as a whole) can increase if there are improvements in technology, even though any given production process exhibits diminishing returns to labor. The law of diminishing marginal returns was central to the thinking of political economist Thomas Malthus (1766-1834). Malthus predicted that as both the marginal and average productivity of

labor fell and there were more mouths to feed, mass hunger and starvation would result. Malthus was wrong (although he was right about the diminishing marginal returns to labor). Over the past century, technological improvements have dramatically altered food production in most countries (including developing countries, such as India). As a result, the average product of labor and total food output have increased. Hunger remains a severe problem in some areas, in part because of the low productivity of labor there.

Example 6.4 (Malthus and The Food Crisis) Table 6.3 shows that technological improvements have dramatically altered food production.

Year	Index of World Food Production Per Cap
1961-64	100
1965	101
1970	105
1975	106
1980	109
1985	115
1990	117
1995	119
2000	127
2005	135
2010	146
2013	151

Table 6.3: Index of world food production per cap.

6.2.4 Labor Productivity and the Standard of Living

Consumers in the aggregate can increase their rate of consumption in the long run only by increasing the total amount they produce. Understand-

ing the causes of productivity growth is an important area of research in economics.

Development of new technologies allowing factors of production to be used more effectively.

Example 6.5 (Labor Productivity and the Standard of Living) Will the standard of living in the United States, Europe, and Japan continue to improve, or will these economies barely keep future generations from being worse off than they are today?

Because the real incomes of consumers in these countries increase only as fast as productivity does, the answer depends on the labor productivity of workers.

	United States	Japan	France	Germany	UK
GDP					
Per Hour	\$62.41	\$39.39	\$60.28	\$58.92	\$47.39
Years	Labor (%) Productivity	Labor (%) Productivity	Labor (%) Productivity	Labor (%) Productivity	Labor (%) Productivity
1970-1979	1.7	4.5	4.3	4.1	3.2
1980-1989	1.4	3.8	2.9	2.1	2.2
1990-1999	1.7	2.4	2.0	2.3	2.3
2000-2009	2.1	1.3	1.2	1.1	1.5
2010-2014	0.7	1.2	0.9	1.2	0.5

Table 6.4: Annual rate of growth of labor productivity (in 2010 U.S dollars) in developed countries

6.3 Production in the Long-Run

Now we return to the case of long-run and assume that labor and capital both are variable, and introduce the important concept of isoquant in production decision.

6.3.1 Production Isoquants

Production Isoquant: A curve that shows all the combinations of inputs that, when used in a technologically efficient way, yield the same total output.

Isoquants show the **input flexibility** that firms have when making production decisions: They can usually obtain a particular output by substituting one input for another. It is important for managers to understand the nature of this flexibility.

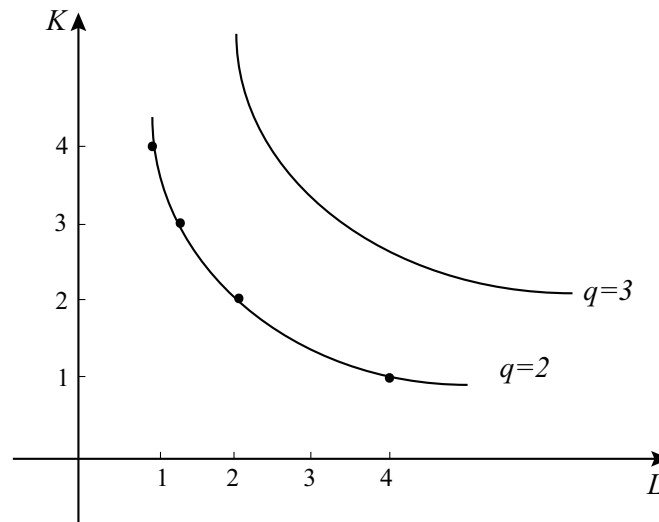


Figure 6.3 A set of production isoquants or an isoquant map

For example, if $q = K^{\frac{1}{2}}L^{\frac{1}{2}}$, the isoquant for $q = 2$ must include the following pair of inputs:

$$K = 1, L = 4;$$

$$K = 2, L = 2;$$

$$K = 3, L = \frac{4}{3};$$

$$K = 4, L = 1.$$

Isoquants are similar to indifference curves in their characteristics. By

analogous reasoning, we can explain several characteristics of isoquants.

- i) *Isoquant slopes downward.* If we increase the quantity of one input employed and keep output unchanged, then we must reduce the amount of the other inputs.
- ii) *Isoquants can never intersect.*
- iii) *Lying further to the northeast identify higher levels of outputs.*
- iv) *Isoquants are generally convex to the origin.*

6.3.2 Marginal Rate of Technical Substitution

The slope of an isoquant measures the marginal rate of technical substitution between the inputs.

Marginal rate of technical substitution (MRTS): The rate at which one input can be substituted for another with output remaining constant.

By the same reasoning as indifference curves, the marginal rate of technical substitution is equal to the absolute value of the slope of an isoquant:

$$MRTS_{LK} = \left| \frac{\Delta K}{\Delta L} \right|.$$

Also, it is equal to the ratio of the marginal products of the inputs, i.e.,

$$MRTS_{LK} = \frac{MP_L}{MP_K}.$$

A strictly convex isoquant implies the marginal rate of technical substitution diminishes, known as the **diminishing marginal rate of technical substitution**.

Limiting Isoquants

- **Perfect substitutes:** The rate at which capital and labor can be substituted for each other is the same no matter what level of inputs is

being used. That is, isoquants are straight lines so that the MRTS is constant, and thus it is known as the **linear production function**, which can be written as

$$q = F(K, L) = aK + bL.$$

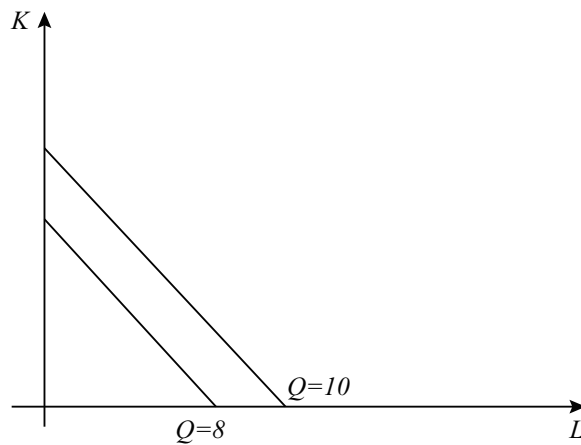


Figure 6.4 Perfect substitutes production function

- **Perfect complements:** Indicate that capital and labor cannot be substituted for each other in production.

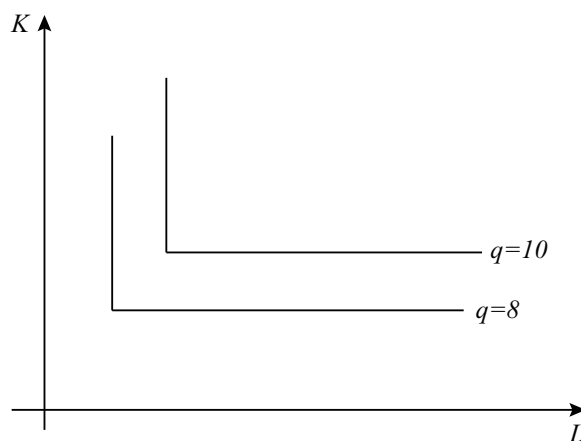


Figure 6.5 Production function with L-shaped isoquants

A production function with perfect complements is said to be the **fixed-proportions production function** (also known as the **Leontief production function**), which can be written as

$$q = F(K, L) = \min aK, bL.$$

The isoquants for these two production functions are convex, but not strictly convex.

6.3.3 Returns to Scale

Returns to scale is an important concept in understanding how production and economic activities are affected by changes in scale. A firm can increase its output by increasing all inputs. We then want to know the scale of return.

Returns to scale: Effect on output of equal proportionate change in all inputs.

For example, if all inputs are doubled, what will happen to output?

There are three types of production processes:

- **Constant returns to scale (CRS):** output doubles when all inputs are doubled;
- **Increasing returns to scale (IRS):** output more than doubles when all inputs are doubled;
- **Decreasing returns to scale (DRS):** output less than doubles when all inputs are doubled.

Graphically, the three types of returns to scale are illustrated in Figure 6.6.

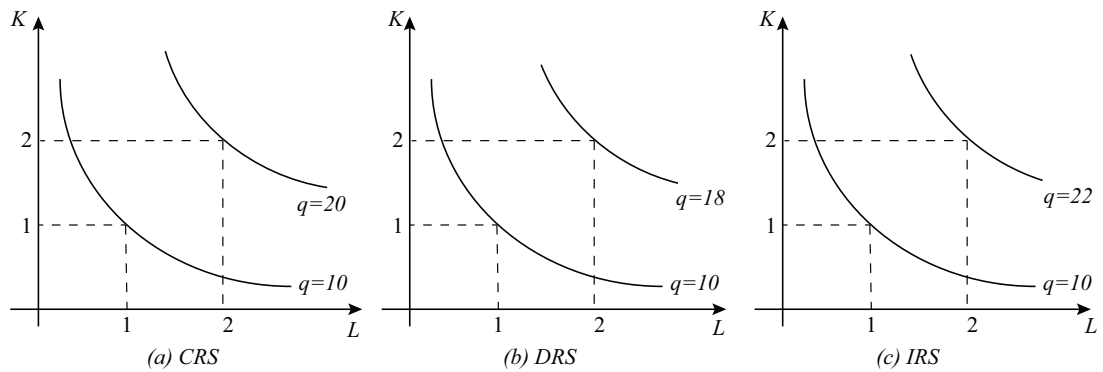


Figure 6.6 Three types of returns to scale

Returns to scale can be checked in the following way if a production function is a **homogeneous function**, i.e.,

$$F(\lambda K, \lambda L) = \lambda^t F(K, L), \quad \lambda > 0.$$

- if the exponent $t < 1$, $F(K, L)$ displays DRS,
- if the exponent $t = 1$, $F(K, L)$ displays CRS,
- if the exponent $t > 1$, $F(K, L)$ displays IRS.

Example 6.6 Suppose

$$F(K, L) = 5K^{\frac{1}{3}}L^{\frac{2}{3}}.$$

Then

$$F(\lambda K, \lambda L) = 5(\lambda K)^{\frac{1}{3}}(\lambda L)^{\frac{2}{3}} = 5\lambda^{\frac{1}{3} + \frac{2}{3}}K^{\frac{1}{3}}L^{\frac{2}{3}} = 5\lambda K^{\frac{1}{3}}L^{\frac{2}{3}} = \lambda F(K, L).$$

Since the exponent of λ is 1, it is CRS.

Example 6.7 Suppose

$$F(K, L) = KL.$$

Then

$$F(\lambda K, \lambda L) = (\lambda K)(\lambda L) = \lambda^2 KL = \lambda^2 F(K, L).$$

Since the exponent of λ is 2, it is IRS.

For a general Cobb-Douglas production

$$F(K, L) = K^\alpha L^\beta \quad \alpha > 0, \beta > 0,$$

we have

$$F(\lambda K, \lambda L) = (\lambda K)^\alpha (\lambda L)^\beta = \lambda^{\alpha+\beta} K^\alpha L^\beta = \lambda^{\alpha+\beta} F(K, L).$$

Therefore, we have

- if the exponent $(\alpha + \beta) < 1$, $F(K, L)$ displays DRS,
- if the exponent $(\alpha + \beta) = 1$, $F(K, L)$ displays CRS,
- if the exponent $(\alpha + \beta) > 1$, $F(K, L)$ displays IRS.

Example 6.8 Suppose

$$F(K, L) = aK + bL.$$

Then

$$F(\lambda K, \lambda L) = a(\lambda K) + b(\lambda L) = \lambda(aK + bL) = \lambda F(K, L).$$

Since the exponent of λ is 1, it is CRS. Thus, any linear production function is CRS.

Example 6.9 Suppose the production is given by a fixed-proportion production function

$$q = F(K, L) = \min\{aK, bL\}.$$

Then

$$F(\lambda K, \lambda L) = \min\{\lambda aK, \lambda bL\} = \lambda \min\{aK, bL\} = \lambda F(K, L).$$

Since the exponent of λ is 1, it is CRS. Thus, any fixed proportional production function is CRS.

Remarks: Returns to scale need not be uniform across all possible levels of output. As a general rule, increasing returns to scale are likely prevail when the scale of operations is small, perhaps followed by an intermediate range when constant returns prevail, with decreasing returns to scale becoming more relevant for large-scale operations. In other words, a production function could embody increasing, constant, and decreasing returns to scale at different levels of output.

Chapter 7

The Cost of Production

In this chapter, we will discuss the various types of production costs and analyze the relationship between the cost of production and the output of production.

7.1 The Nature of Cost

When analyzing the production decision of a firm, the basic concept is the economic costs of production.

Economic costs: The *sum* of explicit and implicit costs.

Explicit costs (i.e., **accounting cost**): These are the payments explicitly made for resources that the firm purchases or hires from outside sources, such as wages, interest paid on debt, and land rent.

Implicit costs: These are the costs of resources which the firm uses but neither buys nor hires from outside sources.

— Provided these resources have an *alternative use*, there is a cost involved although no explicit monetary payment is made. They represent the monetary payments the resources could earn in their best alternative use. For example,

- If you own a building, the implicit costs of running a small store include the rent that could have been earned if the building was leased

to another firm.

- The salary that could be earned by the owner if employed in another business.
- The interest that could be earned by lending money to someone else.

Thus, the sum of explicit and implicit costs can be regarded as opportunity costs. That is, *economic cost equals opportunity cost*.

Opportunity cost: This is the cost associated with opportunities forgone when one alternative is chosen. It refers to *the loss of potential gain from other alternatives when one alternative is chosen*.

— If resources are used to produce one good, they are not available for producing other goods. For example, the cost of a refrigerator might be the number of washing machines that could have been produced with the same resources.

The concept of opportunity cost is particularly useful in situations where alternatives that are forgone do not reflect monetary outlays.

Sunk cost: This is an expenditure that has been made and cannot be recovered (i.e., no alternative use).

Because a sunk cost cannot be recovered, it should not influence the firm's decisions. For example, if specialized equipment for a plant cannot be converted for alternative use, the expenditure on this equipment is a sunk cost. *Because it has no alternative use, its opportunity cost is zero. Thus, it should not be included as part of the firm's economic costs.*

A prospective sunk cost is an investment. Here, the firm must decide whether that investment in specialized equipment is economical.

7.2 Short-Run Costs of Production

7.2.1 Short-Run Total, Average, and Marginal Costs

The short-run costs of production refer to the costs that a firm incurs when producing a certain level of output within a specific period, while at least one input is fixed. Here are the main types of costs that are involved:

(a) **Total Fixed Cost (TFC):** This refers to the costs of fixed factors of production in the short run. Fixed costs do not vary with the level of output, so they must be paid even if the firm produces zero output.

(a') **Average Fixed Cost (AFC):** This is the fixed cost per unit of output, and it can be calculated as:

$$AFC = \frac{TFC}{q},$$

where q represents the output level.

(b) **Total Variable Cost (TVC):** This type of cost is incurred by the firm and depends on how much output it produces. These costs are associated with the variable inputs.

(b') **Average Variable Cost (AVC):** This is the variable cost per unit of output, and it can be calculated as:

$$AVC = \frac{TVC}{q}.$$

(c) **Total Cost (TC):** This is the sum of total fixed costs and total variable costs. It can be expressed as:

$$TC = TFC + TVC.$$

(c') **Average Total Cost (ATC):** This is the total cost per unit of output,

and it can be calculated as:

$$ATC = \frac{TC}{q}.$$

Since $TC = TFC + TVC$, we can also write:

$$ATC = \frac{TFC + TVC}{q} = \frac{TFC}{q} + \frac{TVC}{q}.$$

(d) **Marginal Cost (MC):** This is the marginal cost defined as the increase in total cost resulting from the production of one additional unit of output. It can be calculated as:

$$MC = \frac{\Delta TC}{\Delta q} = \frac{\Delta TFC + \Delta TVC}{\Delta q}.$$

Since fixed cost does not change with output level, $\Delta TFC = 0$ and

$$MC = \frac{\Delta TVC}{\Delta q}.$$

It is worth noting that the TVC equals the sum of all marginal costs incurred in producing each additional unit of output. This is because marginal cost is equal to the increase in variable cost or the increase in total cost that results from producing an additional unit of output.

Remarks:

- (1) *Determining fixed and variable costs.* Over a short period of time, most costs are fixed because the firm is obligated to pay for contracted shipments of materials. Over a longer period, nearly all costs become variable as the firm can adjust its level of production and make changes to its workforce and equipment.
- (2) *Fixed costs vs. sunk costs.* Fixed costs can be avoided if the firm shuts down or goes out of business, while sunk costs

are costs that have already been incurred and cannot be recovered. Fixed costs affect a firm's decisions going forward, while sunk costs do not. A high level fixed cost may cause a firm to shut down, while a high level sunk cost may lead to regret for past decisions but do not affect future decisions.

Example 7.1 Short-Run Cost Schedule for an Individual Firm:

q	TFC	TVC	TC	MC	AFC	AVC	ATC
0	100	0	100	---	---	---	---
1	100	90	190	90	100	90	190
2	100	170	270	80	50	85	135
3	100	240	340	70	$33\frac{1}{2}$	80	$113\frac{1}{2}$
4	100	300	400	60	25	75	100
5	100	370	470	70	20	74	94
6	100	450	550	80	$16\frac{2}{3}$	75	$91\frac{2}{3}$
7	100	540	640	90	$14\frac{2}{7}$	$77\frac{1}{7}$	$91\frac{3}{7}$
8	100	650	750	110	$12\frac{1}{2}$	$81\frac{1}{4}$	$93\frac{3}{4}$
9	100	780	880	130	$11\frac{1}{9}$	$86\frac{2}{3}$	$97\frac{7}{9}$
10	100	930	1030	150	10	93	103

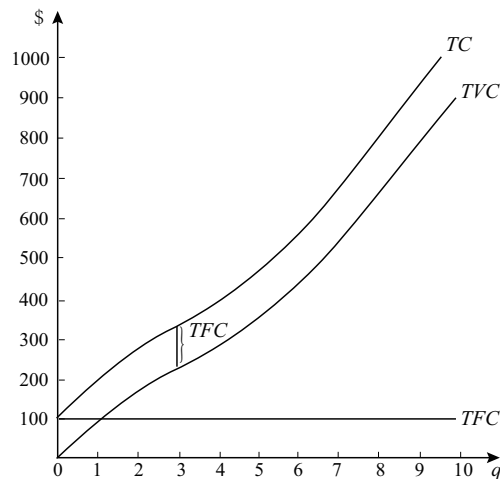


Figure 7.1 TFC is the gap between TC and TVC

Note that in Figure 7.1 the vertical distance between TC and TVC is equal to TFC . Also, in Figure 7.2, the vertical distance between AVC and ATC is AFC .

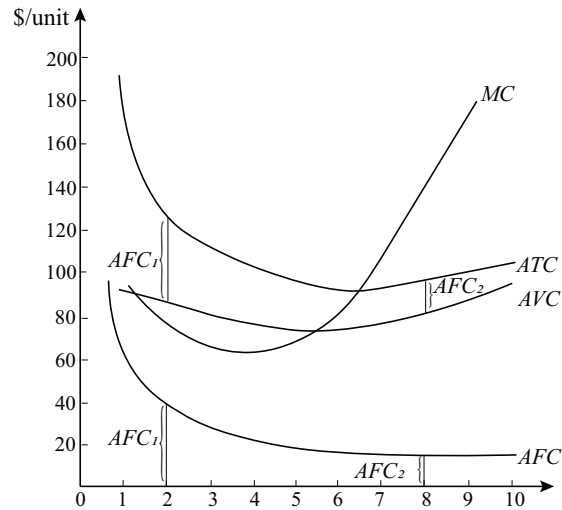


Figure 7.2 AFC is the gap between AVC and ATC

If we have a specific cost function, we can easily find the related various cost curves.

Example 7.2 Suppose that $TC = 10 + 2q + 5q^2$. Then, we have:

$$TFC = 10, TVC = 2q + 5q^2, AC = 10/q + 2 + 5q,$$

$$AFC = 10/q, AVC = 2 + 5q, MC = 2 + 10q.$$

7.2.2 The Shapes of Short-Run Cost Curves

Now let us examine what shapes the short-run cost curves have. We will show that all short-run cost curves have the same shapes as the shapes implied by the data in the previous example.

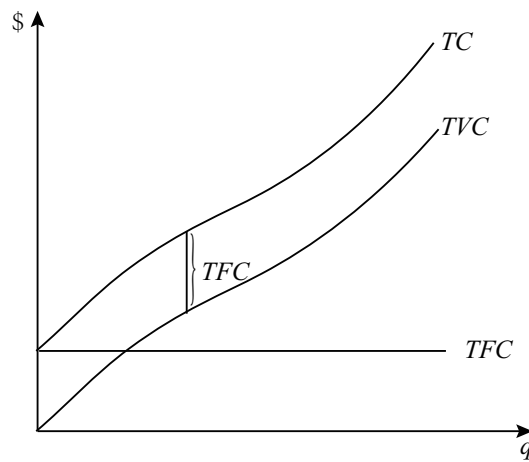


Figure 7.3 TFC is the gap between TC and TVC

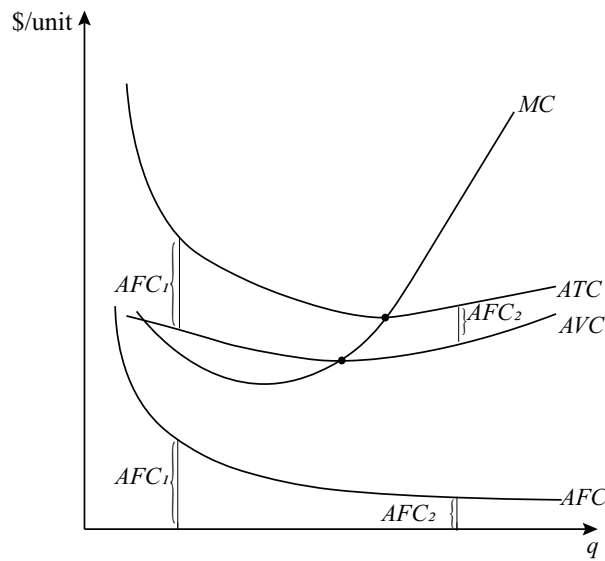


Figure 7.4 MC curve cuts curves of AVC and ATC at their respective minimum

The same as the product curves, we have:

- (1) *The average total cost of a given level of output is the slope of the line from the origin to the total cost curve at that level of output.*

- (2) *The marginal cost of a given level of output is the slope of the line that is tangent to the total cost curve at that level of output.*

The U-shaped Marginal Cost Curve

The marginal cost curve is generally U-shaped: With the cost of additional units of output first falling, reaching a minimum, and then rising.

The U-shape of the marginal cost curve is attributable to the law of diminishing marginal returns.

To see why, recall the MC is defined as

$$MC = \frac{\Delta TVC}{\Delta q}.$$

We know $TVC = wL$ where w is the wage rate and L is the amount of the variable input (labor). Thus $\Delta TVC = w\Delta L$, yielding

$$MC = \frac{\Delta TVC}{\Delta q} = \frac{w\Delta L}{\Delta q} = w / \frac{\Delta q}{\Delta L} = w / MP_L.$$

Thus, the relationship between MC and MP_L is negative. Due to the law of diminishing marginal returns, MP_L varies with the level of output and therefore, MC must also vary accordingly. At low levels of output, MP_L is increasing, and thus MC (which is equal to w/MP_L) must be decreasing. As MP_L reaches its maximum point, MC must be at its minimum. After that, MP_L starts to decrease, and correspondingly, MC will start to increase. In other words, MP_L and MC have an inverse relationship, where MP_L first increases and then decreases, while MC first decreases and then increases.

The average variable cost curve (AVC) also follows a U-shaped curve due to the law of diminishing marginal returns. AVC is defined as TVC/q , which is equal to wL/q , or w/AP_L . As we saw in the previous chapter, the law of diminishing marginal returns leads to an AP_L curve that is shaped like an inverted U. In other words, AP_L first increases, reaches a maxi-

mum, and then decreases. As a result, w/MP_L (which is equal to MC) must also follow a U-shaped curve, where MC first decreases, reaches a minimum, and then increases.

Therefore, MC cuts both the AVC and the average total cost (ATC) curves at their respective minimum points.

The Average-Marginal Costs Relationship

- If $MC < AVC$ (resp. $MC < AC$), the AVC (resp. AC) must be falling.
- If $MC > AVC$ (resp. $MC > AC$), the AVC (resp. AC) must be rising.
- If $MC = AVC$ (resp. $MC = AC$), the AVC (resp. AC) must be at the minimum.

Again, when MC is constant, AVC is identical to MC .

Knowledge of short-run costs is particularly important for firms that operate in an environment in which demand conditions fluctuate considerably. If the firm is currently producing at a level of output at which marginal cost is sharply increasing, and if demand may increase in the future, management might want to expand production capacity to avoid higher costs.

7.3 Long-Run Costs of Production

In the long run, firms have more flexibility in adjusting their production levels and costs. They can enter or exit from an industry, and a firm can vary **all** inputs, including labor, capital, and raw materials. This means that the law of diminishing marginal returns does not apply, and all costs are variable. As a result, *there is no distinction between fixed and variable costs in the long run.*

The types of cost that are relevant in the long run are total cost (TC), average total cost (ATC), and marginal cost (MC). These costs reflect the full range of expenses that a firm incurs as it varies its inputs to produce different levels of output. By analyzing these costs, a firm can make strategic decisions about how to operate in the long run, such as whether to expand production capacity or exit the industry altogether.

7.3.1 Isocost Line

Isocost line: A graphical representation of all possible combinations of labor and capital that can be purchased for a given total cost and given prices of inputs, as depicted in Figure 7.5. The slope of the isocost line represents the ratio of the input prices.

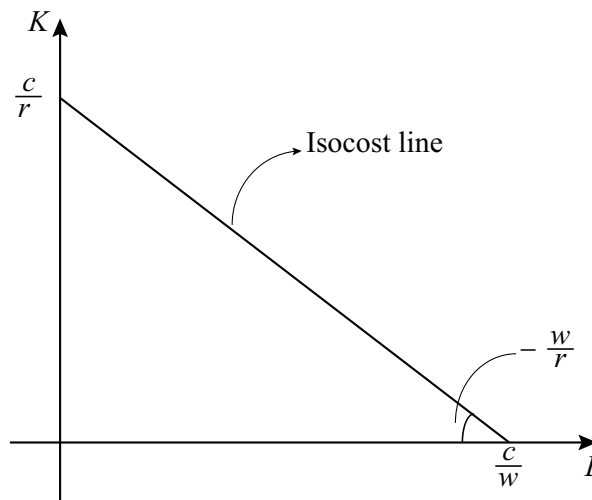


Figure 7.5 An isocost line with two inputs

To understand what an isocost line looks like, we can start with the total cost of producing any particular output, which is given by the sum of the firm's labor cost wL and its capital cost rK :

$$C = wL + rK,$$

where C is the total cost, w is the wage rate, r is the rental rate of K , and L and K represent the amounts of labor and capital used, respectively.

To draw the isocost map, we just vary total cost as shown in Figure 7.6.

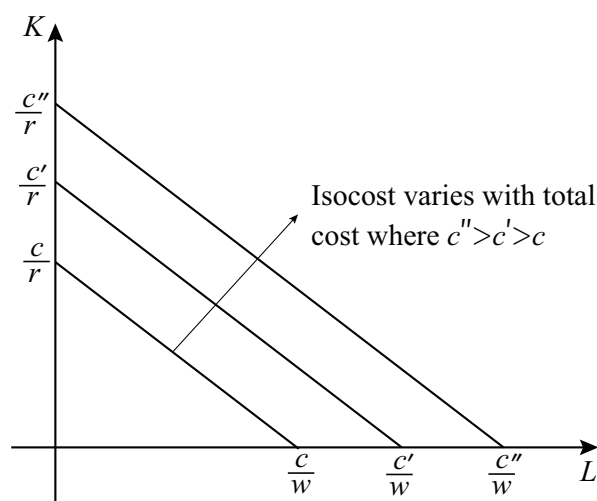


Figure 7.6 A set of isocost lines as total cost varies

Suppose that a firm wants to produce a given level of output, $q = \bar{q}$. We can use the isoquant to determine the possible input combinations which make \bar{q} feasible. Which combination will be chosen?

The firm would choose whichever combination of inputs that

- 1) yield \bar{q} units of output;
- 2) costs less than any other input combinations which also produce \bar{q} .

7.3.2 Cost Minimization Problem

The firm wishes to find the input combination which produces a given level of output and incurs the lowest possible costs. Thus, the firm must find a point on the isoquant $q = \bar{q}$ which is tangent to an isocost line.

In Figure 7.7, both D and E produce \bar{q} , but D costs more.

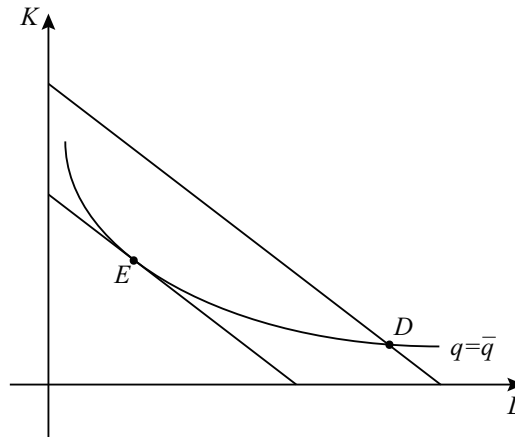


Figure 7.7 The cost-minimizing input choice

At the cost minimizing bundle, the slope of isocost generally equals the slope of isoquant, and hence we have

$$\frac{w}{r} = MRTS_{LK}. \quad (7.1)$$

Recall that we showed that the marginal rate of technical substitution of labor for capital ($MRTS_{LK}$) is the absolute value of the slope of the isoquant and is equal to the ratio of the marginal products of labor and capital: $MRTS_{LK} = \frac{MP_L}{MP_K}$, we can rewrite (7.1) as

$$\frac{MP_L}{MP_K} = \frac{w}{r}. \quad (7.2)$$

Rearranging terms, we obtain

$$\frac{MP_L}{w} = \frac{MP_K}{r}, \quad (7.3)$$

which means that the total cost of producing a given level of output is minimized when *the ratio of marginal product to input price is equal for all inputs*. That is, the firm should employ inputs such that the marginal product cost per dollar's worth of all inputs is equal.

Expansion path: Line which shows input combinations that lead to cost minimization, and it is formed by connecting all tangency points when the level of output varies.

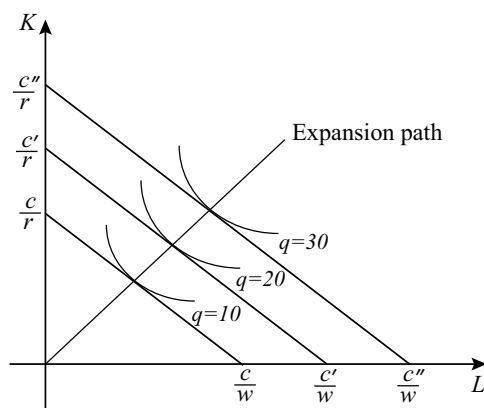


Figure 7.8 The expansion path

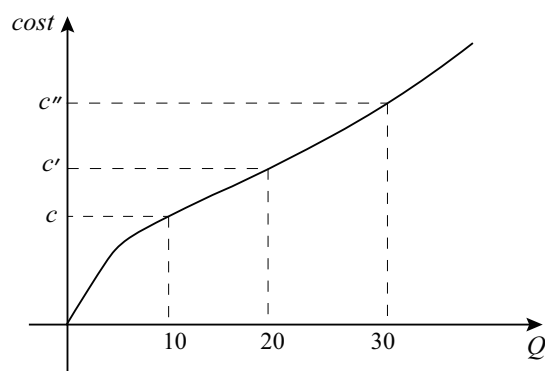


Figure 7.9 Generating a long-run total cost curve through expansion path

We can use the expansion path to generate a long-run total cost curve. To move from the expansion path to the cost curve, we follow three steps:

- Choose an output level represented by an isoquant. Then find the point of tangency of that isoquant with an isocost line.
- From the chosen isocost line, determine the minimum cost of producing the output level that has been selected.

- Graph the output-cost combination in Figure 7.9.

7.3.3 Long-Run Cost Curve

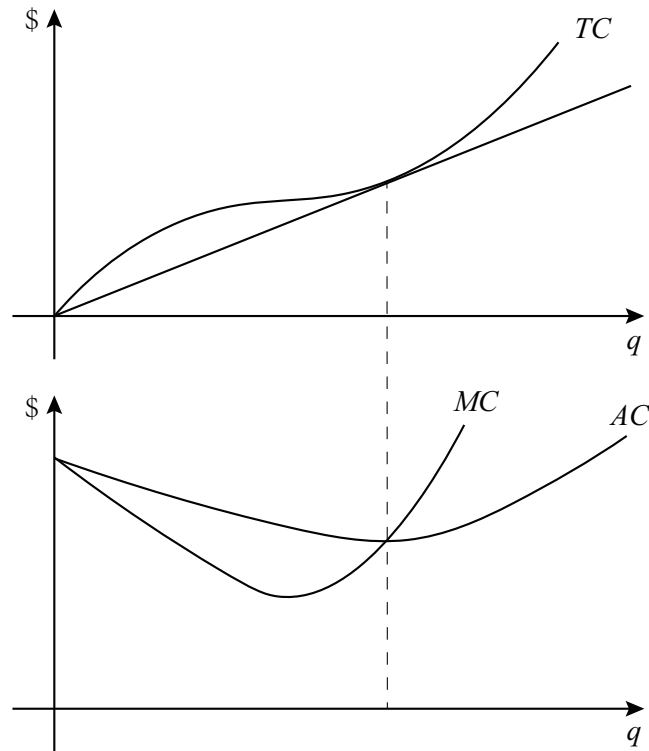


Figure 7.10 The relationship between TC , MC and AC

The long-run total cost shows the minimum cost at each level of output. The long-run marginal cost and average cost curves are derived from the long-run total cost curve in the same way that the short-run per-unit curves are derived from the short-run total cost curves.

We have drawn the long-run TC curve which yields a U-shaped long-run AC and MC curves. Why would the AC and MC curves have this shape? In the long-run all inputs are variable, and hence the law of diminishing marginal returns is not responsible for their U-shapes.

7.3.4 Economies of Scale and Diseconomies of Scale

The U-shaped long-run AC and MC curves are a result of the combination of two different phenomena: the economies and diseconomies of scale.

Economies of scale: The per-unit cost of producing a product falls as the scale of production rises. It refers to the situation in which output can be doubled for less than a doubling of cost.

Diseconomies of scale: The per-unit cost of producing a product rises as the scale of production rises. It refers the situation in which a doubling of output requires more than a doubling of cost.

A firm enjoys economies of scale when it can double its output for less than twice the cost. At low levels of output, there are economies of scale, which means that as the level of output increases, the average cost per unit of output decreases. This is because there are fixed costs that can be spread over more units of output, making each unit less expensive to produce. In addition, specialization and the division of labor become more feasible with larger production runs, which leads to higher productivity and lower costs.

However, as the level of output continues to increase, the firm may experience diseconomies of scale. This is because the firm may become too large and difficult to manage efficiently, leading to coordination problems, communication difficulties, and bureaucratic inefficiencies. These diseconomies can cause the average cost per unit of output to start increasing as output increases, leading to the U-shape of the long-run AC and MC curves.

It is worth noting that returns to scale refer to the relationship between inputs and outputs, while economies of scale refer to the relationship between output and costs. While they are related concepts, it is possible for a firm to experience increasing returns to scale but not economies of scale (if the cost advantages of one input are offset by other factors such as diseconomies of scale). Similarly, a firm may experience economies of scale even if it has constant returns to scale (if the fixed costs can be spread out

more efficiently with larger output).

Economies of scale are often measured in terms of a **cost-output elasticity**, denoted as E_C . E_C is the percentage change in the cost of production resulting from a 1-percent increase in output:

$$E_c = \frac{\Delta C/C}{\Delta q/q}.$$

To see how E_C relates to our traditional measures of cost, rewrite equation as follows:

$$E_c = \frac{\Delta C/\Delta q}{C/q} = \frac{MC}{AC}.$$

Clearly, E_C is equal to 1 when marginal and average costs are equal. In that case, costs increase proportionately with output, and there are neither economies nor diseconomies of scale. When there are economies of scale (when the per-unit cost falls proportionately with output), marginal cost is less than average cost and E_C is less than 1. Finally, when there are diseconomies of scale, marginal cost is greater than average cost and E_C is greater than 1. Consequently, it results in the U-shape of the long-run AC and MC curves.

7.3.5 Input Price Changes and Cost Curves

When the price of inputs changes, it affects the cost of production and leads to a shift in the cost curves. Figure 7.11 illustrates the effect of an increase in the wage rate on the cost curves.

Initially, the firm produces q_1 using inputs K and L at point E . When the wage rate decreases, the cost of producing each level of output falls. Input combination E' becomes the least costly way to produce the same q_1 after the wage decrease. Thus, the change in the wage rate shifts the average cost (AC) and marginal cost (MC) curves upward to AC' and MC' .

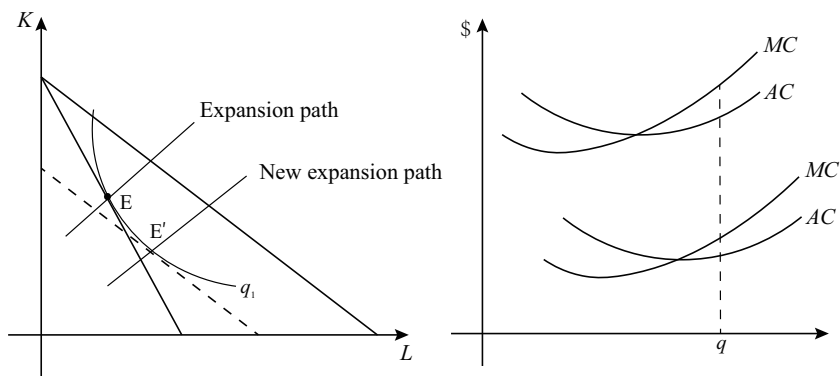


Figure 7.11 The effect of input price changes on cost curves

7.3.6 Short-Run versus Long-Run Average Cost Curves

In the short run, a firm is constrained by its fixed inputs, such as plant capacity, and can only adjust variable inputs, such as labor and materials. As a result, the short-run average total cost (*ATC*) curve may have different shapes depending on the level of fixed inputs.

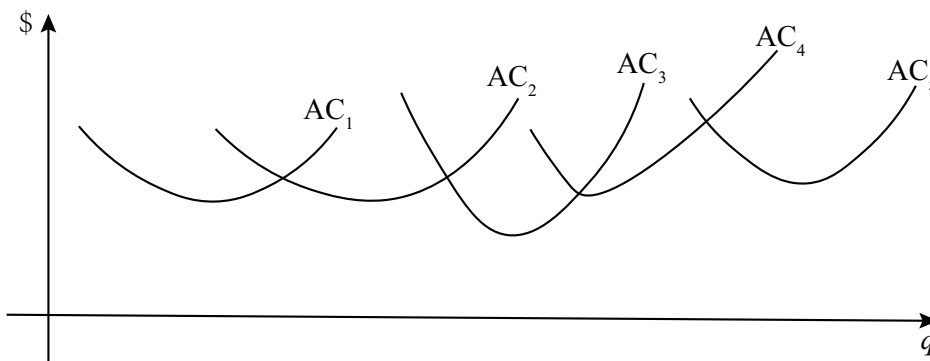


Figure 7.12 AC curves under five different plant capacities

Figure 7.12 shows five different short-run *ATC* curves corresponding to five different plant capacities. Small firms have plant capacities 1 and 2, medium-sized firms have plant capacity 3, and large firms have plant capacities 4 and 5. The short-run *ATC* declines from small to medium-

sized firms and then increases as firms become large.

In the long run, a firm has sufficient time to adjust all inputs, including plant capacity, and can choose the most efficient way to produce a given level of output. The long-run average cost (AC) curve shows the lowest per unit cost at which any output can be produced, given that the firm has sufficient time to vary all inputs, including plant capacity.

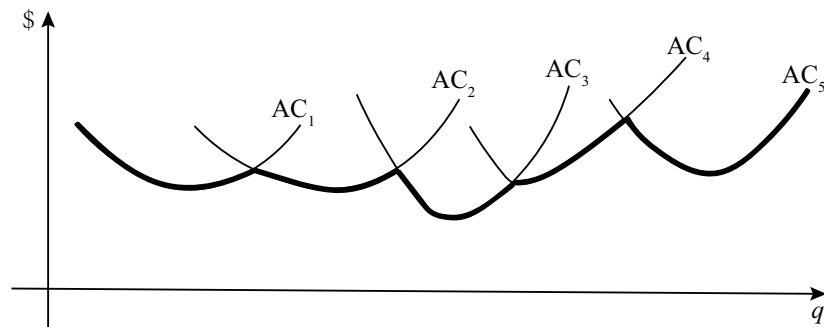


Figure 7.13 Generating the long-run AC curve

Figure 7.13 illustrates how the long-run AC curve is generated from segments of the short-run AC curves. The long-run AC curve is made up of points of tangency with an unlimited number of short-run AC curves. Therefore, the long-run AC curve shows the most efficient way to produce a given level of output, given the available technology and prices of inputs.

7.4 Economies and Diseconomies of Scope

In many situations, a company may choose to become a diversified company, also known as a conglomerate, as it can benefit from cost advantages by providing a variety of products rather than specializing in the production of a single product. This is because of economies of scope.

Product transformation curve is a curve that shows the various combinations of two different outputs (products) that can be produced with a

given set of inputs.

The product transformation curves O_1 and O_2 in Figure 7.14 are bowed out (i.e., concave) because there are economies of scope in production.

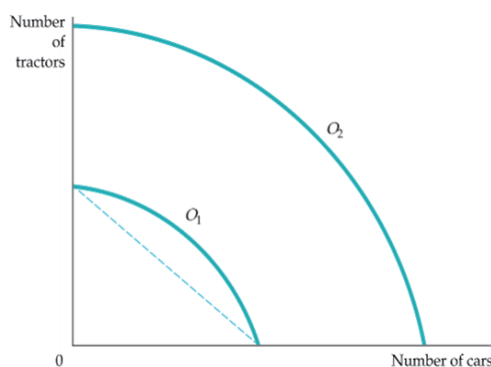


Figure 7.14 Product transformation curve

Economies of scope: Situation in which joint output of a single firm is greater than output that could be achieved by two different firms when each produces a single product. In other words, the total cost of joint production is lower than if they were produced separately.

Diseconomies of scope: Situation in which joint output of a single firm is less than could be achieved by separate firms when each produces a single product.

The Degree of Economies of Scope

To measure the degree of economies of scope, we should ask what percentage of the cost of production is saved when two (or more) products are produced jointly rather than individually. The degree of economies of scope (SC) is the percentage of cost savings resulting when two or more products are produced jointly rather than individually:

$$SC = \frac{C(q_1) + C(q_2) - C(q_1, q_2)}{C(q_1, q_2)}.$$

7.5 Using Cost Curves to Control Pollution

Many problems can be clarified by expressing them in terms of marginal cost. Here is an example of how cost curves can be used to control pollution in the cheapest way possible. Suppose there are two firms that release pollutants into the air during the production process. The government steps in and restricts the total pollution to a certain level, say 200 units.

In Figure 7.15, the amount of pollution generated by each firm is measured from right to left. For example, before the government restricts their activity, firm *A* discharges OP_1 (300 units) and firm *B* discharges OP_2 (250 units). Measuring pollution from right to left is the same as measuring pollution abatement - the number of units by which pollution is reduced from its initial level - from left to right. For example, if firm *B* cuts back its pollution from 250 to 100 units, it has produced 150 units of pollution abatement, the distance p_2X .

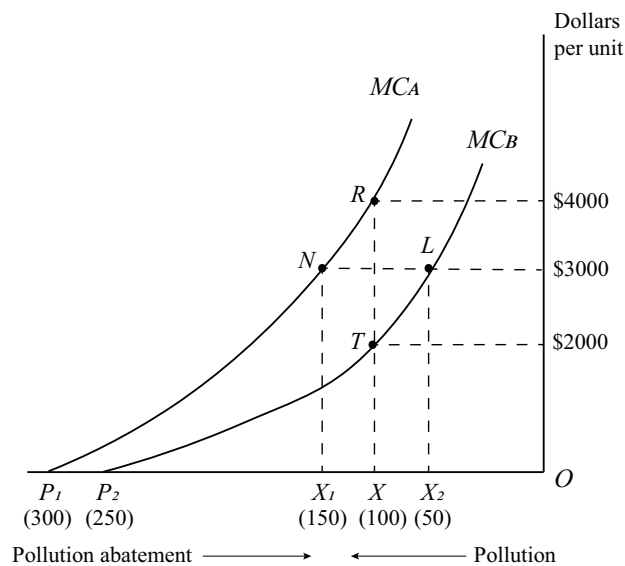


Figure 7.15 Using cost curves to illustrate pollution controls

One way to reduce pollution to 200 is to require each firm to reduce its pollution to 100 units. However, this may not be the cheapest way to do

it. At 100 units of pollution, the marginal cost of reducing pollution for firm *A* is \$4,000, but for firm *B*, it is only \$2,000. Thus, if firm *B* reduces one more unit of pollution, it would only cost \$2,000 more, but if firm *A* increases its pollution by one more unit, its cost would decrease by \$4,000. As a result, the combined cost for both firms can be reduced by \$2,000.

In fact, as long as the marginal costs differ, the total cost of pollution abatement can be minimized by increasing abatement where marginal cost is less and reducing it where marginal cost is higher. Therefore, to minimize the cost of pollution control, firms should produce at a point where their marginal costs are equal. To reduce pollution to 200 units in the cheapest way, firm *A* should discharge 150 units, and firm *B* should discharge 50 units.

Chapter 8

Profit Maximization and Competitive Firm

A **competitive firm** is a firm that operates in a market where there are many other firms producing identical or very similar products, and where the firm has no market power to influence the price of either its inputs or outputs. This means that the firm is a price taker, and the demand curve it faces is perfectly elastic or horizontal.

The two key characteristics of a competitive firm are:

1. **Product Homogeneity:** The products of all firms in the market are identical or very similar, and are perfect substitutes for each other. This means that consumers are indifferent between the products of different firms, and the firms cannot differentiate their products based on quality or other characteristics.
2. **Price Taking:** The firm has no market power and cannot influence the price of its output or its inputs. It must accept the market price as given and adjust its output accordingly.

These characteristics ensure that the competitive firm is a small player in the market, with no ability to influence market outcomes. As a result,

the firm must focus on maximizing its own profits within the constraints of the market.

8.1 Demand Curve under Competition

The demand curve facing a competitive firm is perfectly elastic or horizontal. This is because the firm is a price taker and cannot influence the market price of its output. Therefore, the firm can sell any quantity of output at the market price without affecting the price.

Figure 8.1 shows the demand curve faced by a competitive firm. The firm supplies only a small portion of the total output of all the firms in an industry. Therefore, the firm takes the market price of the product as given, choosing its output on the assumption that the price will be unaffected by the output choice. In the right graph of Figure 8.1 the demand curve facing the firm is perfectly elastic, even though the market demand curve in the left graph of Figure 8.1 is downward sloping.

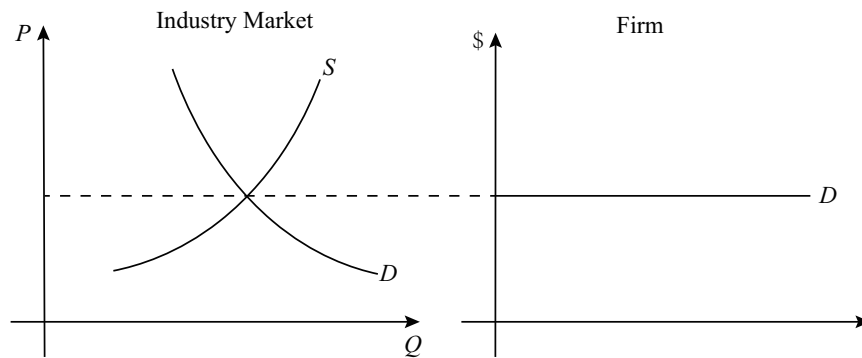


Figure 8.1 Demand curve under perfect competition

Accounting profit and economic profit

Economic profit takes into account opportunity costs. One such opportunity cost is the return to the firm's owners if their capital were used elsewhere.

Accounting profit equals revenues R minus labor cost wL , which is positive. Economic profit π , however, equals revenues R minus labor cost wL minus the capital cost, rK .

The goal of a competitive firm is to maximize its profit, which is the difference between total revenue and total cost. Total revenue is the product of the market price and the quantity of output sold. Total cost is the sum of all costs incurred in producing that output. Thus, the profit can be calculated as:

$$\text{Profit} = \text{Total Revenue} - \text{Total Cost},$$

$$\pi = TR - TC.$$

The assumption of profit maximization predicts business behavior reasonably accurately and avoids unnecessary analytical complications. Profit is likely to dominate almost all other decisions for smaller firms. However, managers who make day-to-day decisions in larger firms usually have little contact with the owners and may be more concerned with goals such as revenue maximization or revenue growth.

Firms that do not come close to maximizing profit are unlikely to survive, so firms that do survive make long-run profit maximization one of their highest priorities.

Total revenue (TR), average revenue (AR), and marginal revenue (MR) for a competitive firm are respectively given by:

$$TR = P \times q; \quad (8.1)$$

$$AR = \frac{TR}{q} = \frac{P \times q}{q} = P; \quad (8.2)$$

$$MR = \frac{\Delta TR}{\Delta q} = \frac{P \Delta q}{\Delta q} = P. \quad (8.3)$$

For a competitive firm, we thus have:

$$P = AR = MR.$$

Therefore, *along this demand curve, marginal revenue, average revenue, and price are all equal.*

8.2 Short-Run Profit Maximization

In a competitive market, a firm's profit-maximizing policy is related to the quantity produced, since it has no control over prices. Figure 8.2 illustrates how to identify the most profitable level of output using the typical total revenue (TR) and total cost (TC) curves. The profit (π) is greatest at the output level q^* , where TR and TC have equal slopes.

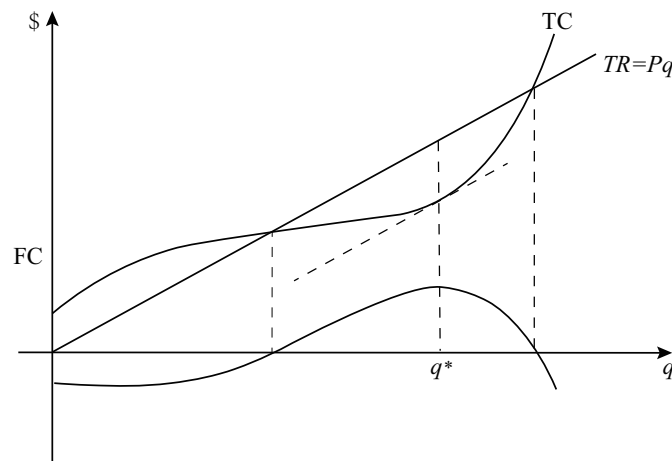


Figure 8.2 Identifying the most profitable output level using TR and TC curves

Should the firm produce any output?

1. Yes, it should produce if there is a level of output that can earn a positive profit, i.e., if $TR > TC$ (or equivalently $P = AR > AC$).
2. Yes, it should produce even if it cannot make a profit but it can make a loss smaller than fixed cost, i.e., if $TR > TVC$ (or equivalently $P = AR > AVC$).

- If $q = 0$, $TC = TFC$; $TR = 0$, so profit = $TR - TC = -TFC \Rightarrow$
Loss = TFC ;
- If $q > 0$ and loss occurs, then

$$\begin{aligned}\text{Loss} &= TC - TR \\ &= (TFC + TVC) - TR \\ &= TFC + (TVC - TR)\end{aligned}$$

Thus, Loss $< TFC$ provided $TVC < TR$ (or equivalently $AVC < AR = P$).

Therefore, in either situations, *the firm should produce a positive level of output as long as $P > AVC$ since $P = AR = MR$.*

What quantity should the firm produce when $P > AVC$?

The firm should produce the quantity that maximizes profits or minimizes losses:

- It is worthwhile producing for which $MR > MC$.
- It is not worthwhile continuing to produce when $MR < MC$. (Recall that MC must rise eventually).
- Thus, a firm will produce up to the level where $MC = MR$, or $MC = P$ since $P = MR$. That is, at that output, marginal revenue (the slope of the revenue curve) is equal to marginal cost (the slope of the cost curve).

Summarizing the above discussions, we reach the following conclusion.

Conditions for Short-Run Profit Maximization:

1. $P \geq AVC(q^*)$ (necessary condition for producing);

2. $P = MC(q^*)$ (how much should be produced).

Remarks:

1. If condition 1 is not satisfied, then the firm is best off producing $q^* = 0$ units so that $TR = 0$, $TC = FC + 0 = FC$ and thus $\pi = -TC$ (losing FC is better than losing $FC + \text{some } VC$).
2. When $P = MR(q^*) = AVC(q^*)$ and condition 2 is satisfied, then both q^* and $q = 0$ generate the same π (i.e., $\pi = -FC$).

Various Situations in Short-Run Profit Maximization

There are five cases for a competitive firm's profit maximization, depending on relationships among P , $AVC(q^*)$, and $AC(q^*)$:

Case 1: $P > AC(q^*)$, resulting in positive profit;

Case 2: $P = AC(q^*)$, zero profit;

Case 3: $AC(q^*) > P > AVC(q^*)$, loss minimization;

Case 4: $AC(q^*) > P = AVC(q^*)$, no difference between producing q^* and shutdown ($q = 0$) since Loss = TFC in either case;

Case 5: $P < AC(q^*)$, shutdown.

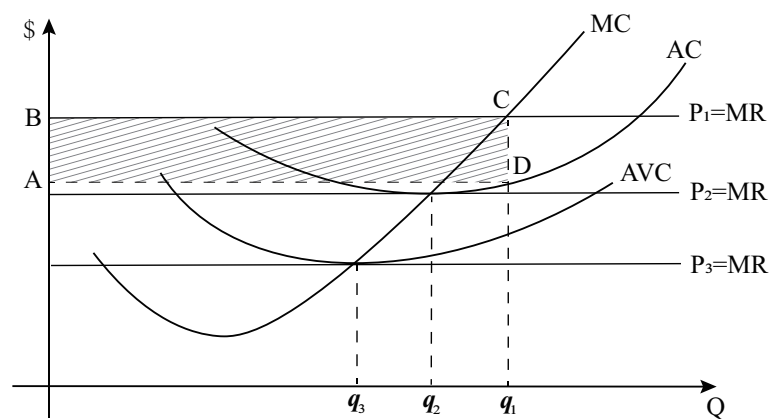


Figure 8.3 Profit maximization in the short run

As shown in Figure 8.3, when the price is P_1 , the profit-maximizing output is q_1 . The total profits are the rectangle $ABCD$. When the price is P_2 , the most profitable output is q_2 . The profits, however, are zero since the price just equals the average cost of production. When the price is P_3 , the firm can just cover its variable cost by producing q_3 , where AVC equals the price. At this point, the firm would be operating at a short-run loss; the loss is exactly equal to its total fixed cost. At a price below P_3 , the firm is unable to cover its variable cost and hence must shut down.

Let us consider several numerical examples.

Example 8.1 (Perfect Competition: Profit Maximization) Note that $TC = ATC \times q$, and $TR = p \times q$. From Table 8.1, we know $MR > MC$ for $q = 1, 2, \dots, 9$. $MR < MC$ for $q = 10$. $q = 9$ for profit maximization. Since $AR > ATC$ at $q = 9$, a positive profit is made.

q	AFC	AVC	ATC	MC	TC	$P = AR = MR$	TR	π
0	---	---	---	---	100	131	0	100
1	100	90	190	90	190	131	131	-59
2	50	85	135	80	270	131	262	-8
3	$33\frac{1}{3}$	80	$113\frac{1}{3}$	70	340	131	393	53
4	25	75	100	60	400	131	524	124
5	20	74	94	70	470	131	655	185
6	$16\frac{2}{3}$	75	$91\frac{2}{3}$	80	550	131	786	236
7	$14\frac{2}{7}$	$77\frac{1}{7}$	$91\frac{3}{7}$	90	640	131	917	277
8	$12\frac{1}{2}$	$81\frac{1}{4}$	$93\frac{3}{4}$	110	750	131	1048	298
9	$11\frac{1}{9}$	$86\frac{2}{3}$	$97\frac{7}{9}$	130	880	131	1179	299
10	10	93	103	150	1030	131	1310	280

Table 8.1

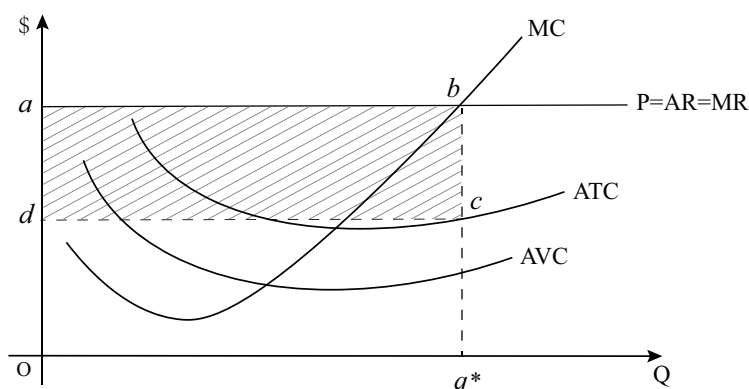


Figure 8.4 Identifying profit-maximizing output and short-run profit

From Figure 8.4, we know $TR = AR \times q^* = Oabq^*$, $TC = ATC \times q^* = Odcq^*$, Profit = $TR - TC = abcd$. At point b in Figure 8.4, $MR = MC \Rightarrow q^* = 9$.

Example 8.2 (Perfect Competition: Loss Minimization) By Table 8.2, $MR = MC$ at $q = 6$. Also, $ATC > AR > AVC$ implies loss minimization. Indeed, At $q = 6$, Loss = \$64 < $TFC = \$100$, so firm should not cease production.

q	AFC	AVC	ATC	MC	TC	$P = AR = MR$	TR	π
0	---	---	---	---	100	81	0	-100
1	100	90	190	90	190	81	81	-109
2	50	85	135	80	270	81	162	-108
3	$33\frac{1}{3}$	80	$113\frac{1}{3}$	70	340	81	243	-97
4	25	75	100	60	400	81	324	-76
5	20	74	94	70	470	81	405	-65
6	$16\frac{2}{3}$	75	$91\frac{2}{3}$	80	550	81	486	-64
7	$14\frac{2}{7}$	$77\frac{1}{7}$	$91\frac{3}{7}$	90	640	81	517	-73
8	$12\frac{1}{2}$	$81\frac{1}{4}$	$93\frac{3}{4}$	110	750	81	567	-102
9	$11\frac{1}{9}$	$86\frac{2}{3}$	$97\frac{7}{9}$	130	880	81	729	-151
10	10	93	103	150	1030	81	810	-220

Table 8.2

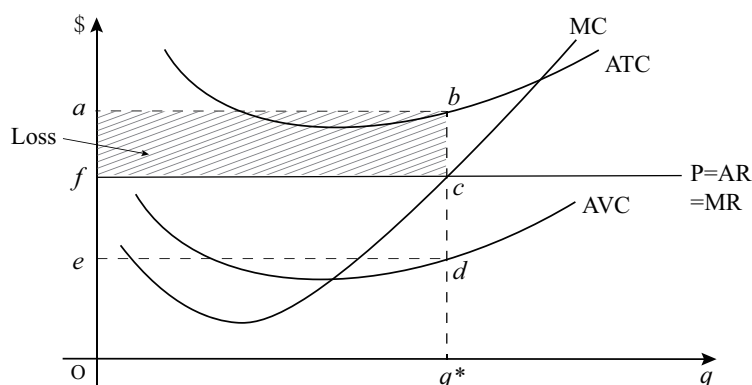


Figure 8.5 Loss minimization under perfect competition

From Figure 8.5, we know $TR = AR \times q^* = Ofcq^*$, $TC = Oabq^*$, and $\text{Loss} = TC - TR = abcf$. At point c in Figure 8.5, $MR = MC \Rightarrow q^* = 6$.

Example 8.3 (Perfect Competition: Production Shutdown) From Table 8.3, although $MR = MC$ at $q = 5$, but $AR < AVC$ at $q = 5$, which implies $\text{Loss} > TFC$ ($115 > 100$). Thus $q = 0$, i.e., shutdown is optimal.

q	AFC	AVC	ATC	MC	TC	$P = AR = MR$	TR	π
0	---	---	---	---	100	---	---	-100
1	100	90	190	90	190	71	71	-119
2	50	85	135	80	270	71	142	-128
3	$33\frac{1}{3}$	80	$113\frac{1}{3}$	70	340	71	213	-127
4	25	75	100	60	400	71	284	-116
5	20	74	94	70	470	71	355	-115
6	$16\frac{2}{3}$	75	$91\frac{2}{3}$	80	550	71	426	-124
7	$14\frac{2}{7}$	$77\frac{1}{7}$	$91\frac{3}{7}$	90	640	71	497	-143
8	$12\frac{1}{2}$	$81\frac{1}{4}$	$93\frac{3}{4}$	110	750	71	568	-182
9	$11\frac{1}{9}$	$86\frac{2}{3}$	$97\frac{7}{9}$	130	880	71	639	-241
10	10	93	103	150	1030	71	710	-320

Table 8.3

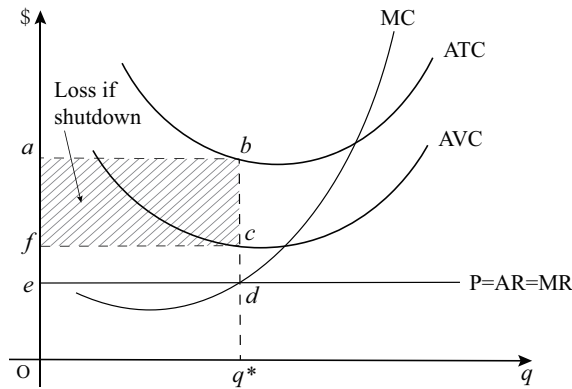


Figure 8.6 Production shutdown under perfect competition

By Figure 8.6, we know at point d in Figure 8.6, $MR = MC \Rightarrow q^* = 5$. At $q^* = 5$, $TR = Oedq^*$, $TC = Oabq^*$, \Rightarrow Loss = $eabd$. At $q = 0$, $TR = 0$, $TC = TFC = AFC \times q = abcf$, which is small than $eabd$.

The following is an algebraic example.

Example 8.4 Suppose that $TC(q) = 8 + 5q + 2q^2$, $MC(q) = 5 + 4q$, and $P = 45$.

1. Find the average variable cost (AVC).

The total variable cost (TVC) is the portion of TC that involves terms with output q :

$$TVC(q) = 5q + 2q^2.$$

Thus, the average variable cost (AVC) is:

$$AVC = \frac{TVC}{q} = \frac{5q + 2q^2}{q} = 5 + 2q.$$

2. Find the profit-maximizing level of output and the maximizing profit.

The profit-maximizing level of output should satisfy the two conditions:

- (1) $P \geq AVC$;
 (2) $MR = MC$, which is the same as the market price P in a perfectly competitive market.

Setting $P = MC(q)$ leads to $45 = 5 + 4q$ and thus $q^* = 10$.

We also need to verify if $P \geq AVC(q)$ at $q^* = 10$. Indeed,

$$AVC(10) = 5 + 2 \times 10 = 5 + 20 = 25 < P = 45.$$

Therefore, the profit-maximizing level of output is $q^* = 10$, and the maximizing profit is:

$$\pi = TR - TC = Pq - TC(q^*) = 45 \times 10 - (8 + 5 \times 10 + 2 \times 10^2) = 392.$$

3. At what price and level of output are the firm's profit zero?

The firm's profit is zero when total revenue (TR) equals total cost (TC), which occurs at the break-even point where $P = AC$. To find the minimum average cost, setting $MC(q) = AC(q)$ leads to

$$5 + 4q = 8/q + 5 + 2q.$$

Solving for q , we get:

$$q_{BE} = 2.$$

Thus, at the break-even point, the price is:

$$P = AC(q_{BE}) = 8/2 + 5 + 2 \times 2 = 13.$$

4. What is the lowest price at which the firm would sell its output? If so, what is the output?

The lowest price at which the firm would sell its output is equal to the minimum AVC, which is the shutdown point. The shutdown point is where $P = AVC$. Setting $P = AVC(q)$ and solving for q , we

get:

$$q_{SH} = 0.$$

Thus, the lowest price at which the firm would sell its output is:

$$P = MC(q_{SH}) = 5.$$

Since the output is zero at the shutdown point, there is no output.

8.3 The Short-Run Supply Curve of a Competitive Firm

In a competitive market, a firm's short-run supply curve is determined by its marginal cost (MC) curve and its minimum average variable cost (AVC) level. This is because a competitive firm will only produce output as long as its total revenue ($P \times Q$) covers its total variable cost (TVC) or equivalently $P \geq AVC$, and in the short run, some costs, such as fixed costs (FC), are fixed and cannot be changed.

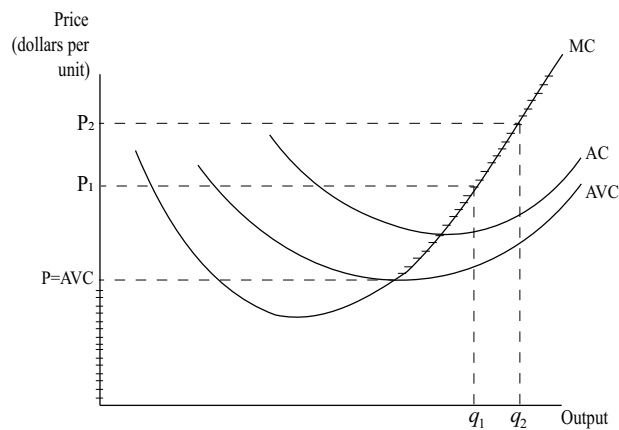


Figure 8.7 Competitive Firm's Short-run Supply Curve

Therefore, *the firm's short-run supply curve is the portion of the MC curve that lies above the minimum AVC level.* When the price is above

the minimum AVC level, the firm will produce the output level where $P=MC$, as long as this output level covers the AVC level. When the price is below the minimum AVC level, the firm will shut down and produce zero output.

Figure 8.7 illustrates the competitive firm's short-run supply curve. The portion of the MC curve above the minimum AVC level is the crosshatched area, which represents the output levels that the firm is willing to produce at different price levels in the short run.

8.4 Output Response to a Change in Input Prices

A change in the price of an input used in production can affect a firm's costs and profit-maximizing level of output. Figure 8.8 illustrates the output response to a reduction in input prices, resulting in a downward shift of the marginal cost curve from MC to MC' . As a result, the profit-maximizing output increases from q_1 to q_2 .

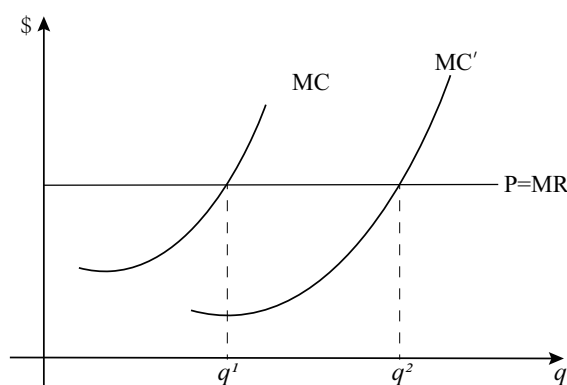


Figure 8.8 Output response to an input price reduction

8.5 Producer Surplus in the Short Run

Producer surplus: Sum of differences between the market price of a good and the marginal cost for all units produced.

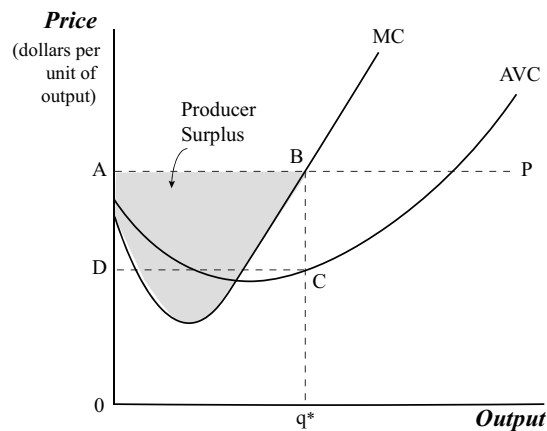


Figure 8.9 Producer surplus for a firm

The producer surplus (PS) for a firm is measured by the shaded area below the market price and above the marginal cost curve, between outputs 0 and q^* , the profit-maximizing output in Figure 8.9

Alternatively, it is equal to rectangle $ABCD$ since the sum of all marginal costs up to q^* is equal to the variable costs of producing q^* , i.e.,

$$PS = TR - TVC.$$

The difference between producer surplus and profit of a firm is then the total fixed cost since

$$PS - \pi = TR - TVC - (TR - TV - TFC) = TFC.$$

8.6 Long-Run Profit Maximization

The same principle used for the short-run setting can apply to the discussion of long-run profit maximization, but now we employ long-run cost curves. The firm maximizes profits in the long run by producing up to where $P = MC$. That is, the long-run output of a profit-maximizing competitive firm is the point at which long-run marginal cost equals the price.

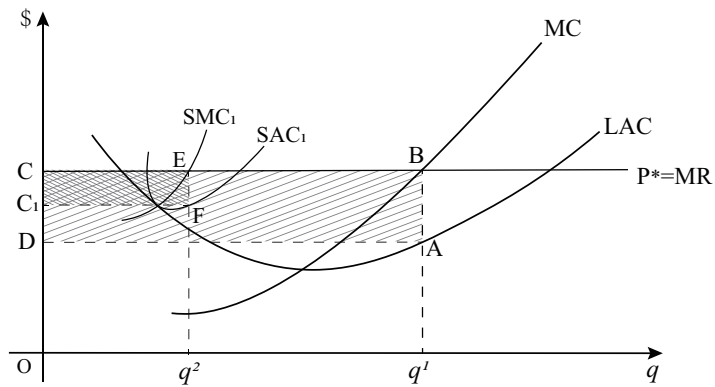


Figure 8.10 The long-run output of a profit-maximizing competitive firm

With P^* , the most profitable output is q^1 in the long run, and the profit is rectangle $ABCD$. In the short run the most profitable output will be q^2 , and rectangle $CEFC_1$ is the profit which is less than the long-run profit.

Conditions for Long-Run Profit Maximization:

- (1): $P \geq AC$ (necessary condition for producing);
- (2): $P = MC$ (how much should be produced).

Chapter 9

Competitive Markets

In this chapter the emphasis shifts from the individual firm to the competitive industry/markets.

Assumptions on Perfect Competitive Markets:

- **A large number of buyers and sellers**, which will normally guarantee that the firms and consumers behave as price takers.
- **Unrestricted mobility of resources**: no barrier to entry into, or exit from the market.
- **Homogeneous products**: the products of all of the firms in an industry are identical to consumers.
- **Possession of all relevant information** to make economic decisions.

Unrestricted mobility implies that there are no special costs that make it difficult for a firm to enter (or exit) an industry. With free entry and exit, buyers can easily switch from one supplier to another, and suppliers can easily enter or exit a market.

The presence of many firms is not sufficient for an industry to approximate perfect competition since firms can implicitly or explicitly collude in setting prices. Conversely, the presence of only a few firms in a market does not rule out competitive behavior.

When Is a Market Highly Competitive? Many markets are highly competitive in the sense that firms face highly elastic demand curves and relatively easy entry and exit, but there is no simple rule of thumb to describe whether a market is close to being perfectly competitive.

9.1 The Short-Run Industry Supply Curve

In the short run, a competitive firm will produce at a point where the marginal cost equals the price, as long as the price is above the minimum point of its average variable cost curve.

How is the short-run industry supply curve determined?

The short-run industry supply curve is derived by horizontally summing the individual firms' marginal cost curves (above their respective average variable cost curves). That is, the industry supply curve is the sum of the quantities produced by each individual firm at each possible price level.

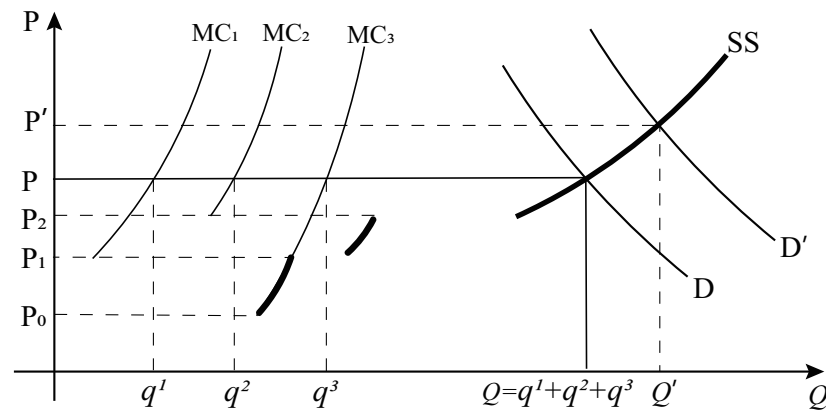


Figure 9.1 The short-run industry supply curve

Note that the short-run supply curve, SS , slopes upward. The upward slope of the industry supply curve reflects the fact that each firm's marginal cost curve slopes upward due to the law of diminishing marginal

returns to variable inputs. Thus, the law of diminishing marginal returns is the underlying determinant of the shape of a competitive industry's short-run supply curve.

Price and Output Determination in the Short Run

The interaction of supply and demand in a market determines the market price and output. In Figure 9.1, the intersection of the demand curve D with the supply curve SS determines the equilibrium price, P , and equilibrium industry output, Q , where Q is the sum of the quantities produced by each individual firm.

In the short run, an increase in market demand leads to a higher price and higher output. When demand increases to D' , the equilibrium price becomes P' , and industry output increases to Q' .

9.2 Long-Run Competitive Equilibrium

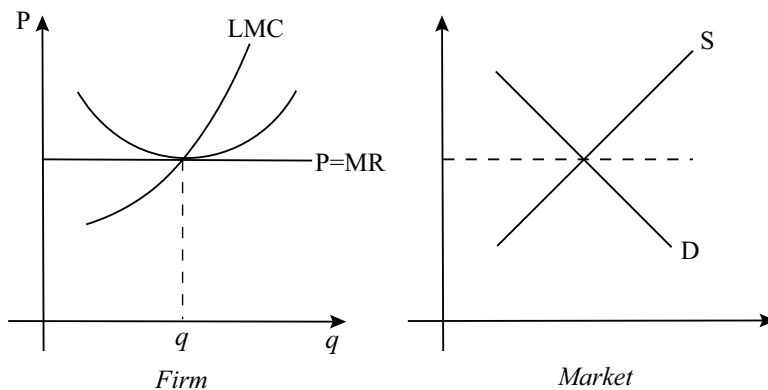


Figure 9.2 The emergence of long-run competitive equilibrium

In the long-run competitive equilibrium, the independent plans of firms and consumers mesh perfectly. Each firm has adjusted its scale of operation in light of the prevailing price and is able to sell as much as it chooses

to sell. Consumers are able to purchase as much as they wish to consume at the prevailing price. There are no incentives for any firm to alter its scale of operation or to exit from the industry and no incentive for outsiders to enter the market. Unless the underlying market conditions change, the price and rate of output will remain stable.

Long-Run Competitive Equilibrium:

- (a) **Profit maximization:** Each firm must be producing the output level such that its profit is maximized at the prevailing market price, that is, $P = LMC$.
- (b) **Zero economic profit made by each firm.** There are no incentives for firms to either enter or exit from the industry.
- (c) **Market quantity supplied equals market quantity demanded:** The combined quantity of outputs of all firms at the prevailing price must equal the total quantity consumers wish to purchase at that price level.

Zero economic profit: A firm is earning a normal return on its investment in a perfectly competitive market — i.e., it is doing as well as it could by investing its money elsewhere.

Remarks: There are instances in which firms earning positive accounting profit may be earning zero economic profit. If a clothing store is located near a large shopping center, the additional flow of customers can increase the store's accounting profit. When the opportunity cost of the land is included, the profitability of the clothing store is no higher than that of its competitors.

Entry and Exit

In a market with entry and exit, a firm enters when it can earn a positive long-run profit and exits when it faces the prospect of a long-run loss.

Entry of Firms Eliminates Profits:

- (i) In Figure 9.3, the representative firm is in long-run equilibrium where P^e is the minimum point of ATC . Normal profits are earned, and hence, economic profit = 0.
- (ii) Suppose demand increases from D^1 to D^2 . Price rises to p_1 and exceeds the minimum point of ATC , leading to positive economic profits.
- (iii) New firms enter the industry, and supply starts to increase from S_1 , causing the price to start falling.
- (iv) Supply continues to increase while economic profits are being made. The increase of supply will not stop until it reaches the new supply curve S_2 , where P^e is the minimum point of ATC again.
- (v) In the long run, a larger quantity is supplied at the same initial price level.

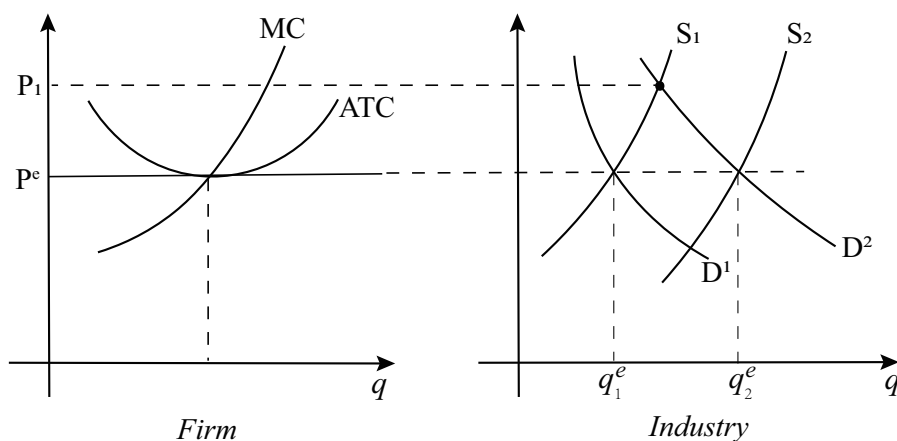


Figure 9.3 Entry of firms eliminates economic profits

Exit of Firms Eliminates Losses:

- (i) In Figure 9.4, the representative firm is in long-run equilibrium where P^e is the minimum point of ATC . Normal profits

are earned, and hence no economic profits could be generated.

- (ii) Suppose demand decreases from D^1 to D^3 . Price falls below the minimum point of ATC to p_2 . Economic profits are negative, i.e., firms suffer from economic losses.
- (iii) Some firms leave the industry, and supply falls from S_1 , causing the price to rise.
- (iv) Supply continues to fall while economic loss is being experienced. The reduction of supply will not stop until it reaches the new supply curve S_3 , where P^e is the minimum point of ATC again.
- (v) In the long run, a smaller quantity is produced and supplied at the same initial price.

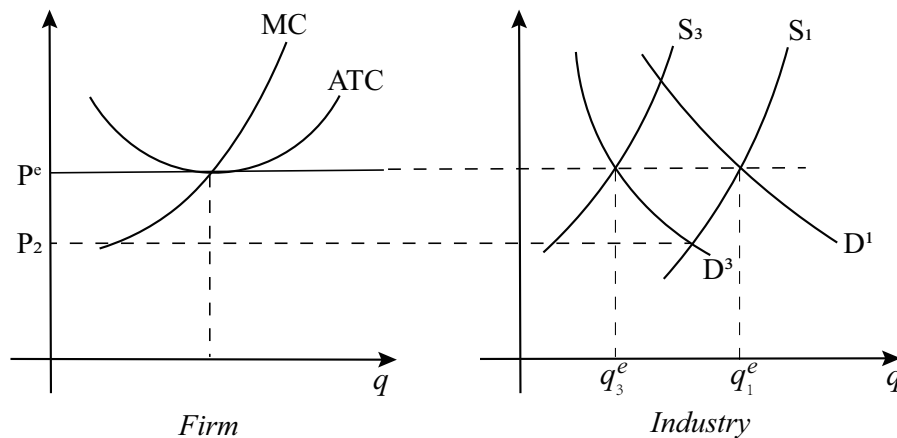


Figure 9.4 Exit of firms eliminates losses

9.3 The Long-Run Supply Curve

Economists distinguish among three different types of competitive industries, constant-cost, increasing-cost, and decreasing-cost. The distinction depends on how a change in industry output affects the prices of inputs.

Constant-Cost Industry: Horizontal LR Supply Curve

Constant-Cost Industry: Expansion of output *does not affect input prices*, and consequently the entry and exit of firm do not cause cost curves to shift. Thus, *the price of output remains constant for all levels of quantity*, and hence LR supply is perfectly elastic. Therefore, *the long-run supply curve for a constant-cost industry is a horizontal line at a price that is equal to the long-run minimum average cost of production.*

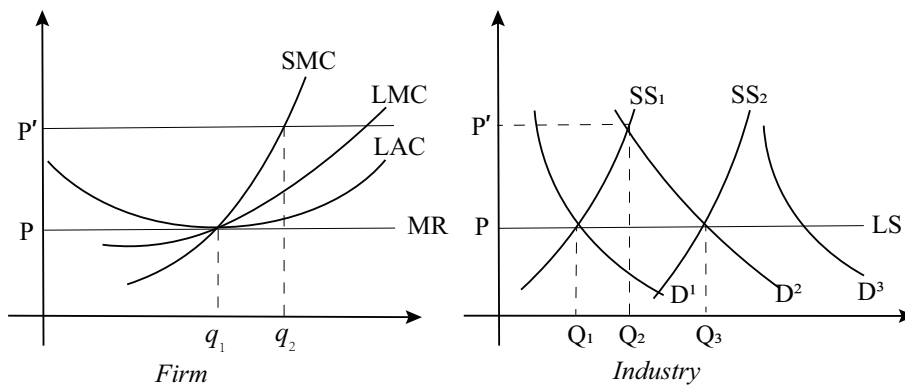


Figure 9.5 The long-run supply curve for a constant-cost industry

Increasing-Cost Industry: Upward-Sloping LR Supply Curve

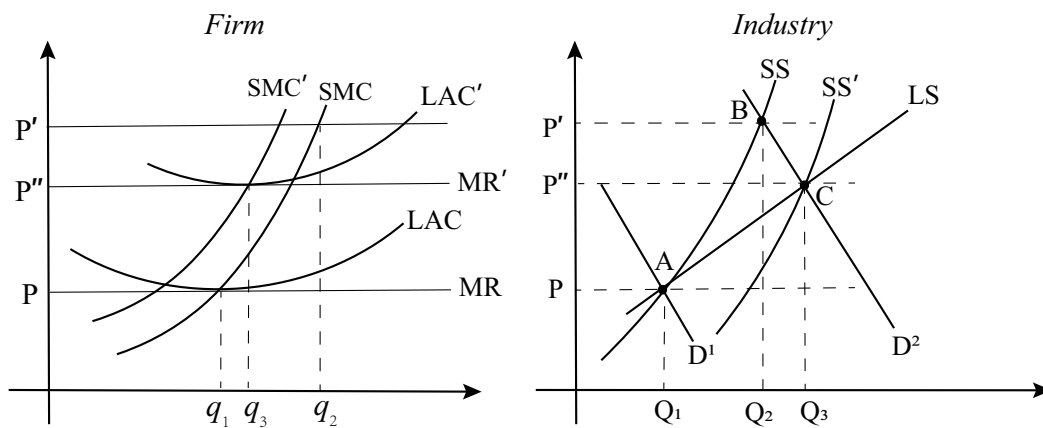


Figure 9.6 The long-run supply curve for an increasing-cost industry

Increasing-Cost Industry: Expansion of output *causes input prices to rise* as demand for them grow, and consequently the entry/exit of firm makes cost curves shift upward/downward. As firms enter the industry, they compete for scarce resources. Thus, *prices of input resources rise as do production costs of firms*. Therefore, cost curves shift upward (*ATC and MC*). Hence, *industry supply curve is upward-sloping*.

Decreasing-Cost Industry: Downward-Sloping LR Supply Curve

Decreasing-Cost Industry: Expansion of output *causes input prices to decrease* as demand for them grow, and consequently the entry/exit of firm makes cost curves shift downward/upward. Hence, a *decreasing-cost industry has a downward-sloping long-run supply curve*. This means the expansion of output by the industry in some way lowers the cost curves of individual firms. The entry of firms may result in lower per unit cost.

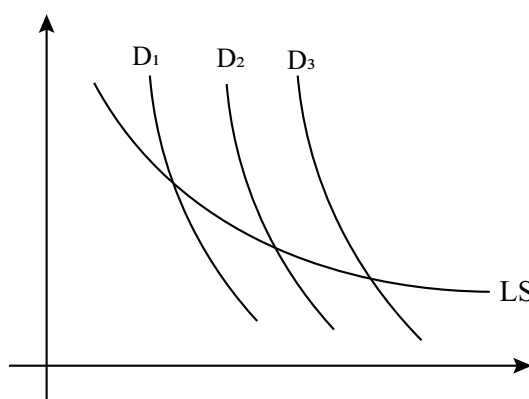


Figure 9.7 The long-run supply curve for a decreasing-cost industry

Example 9.1 We saw that the supply of coffee is extremely elastic in the long run. The reason is that land for growing coffee is widely available and the costs of planting and caring for trees remains constant as the volume grows. Thus, coffee is a constant-cost industry.

The oil industry is an increasing cost industry because there is a limited availability of easily accessible, large-volume oil fields.

Finally, a decreasing-cost industry. In the automobile industry, certain cost advantages arise because inputs can be acquired more cheaply as the volume of production increases.

Long-Run Elasticity of Supply

The long-run elasticity of industry supply is defined in the same way as the short-run elasticity: It is the percentage change in output ($\Delta Q/Q$) that results from a percentage change in price ($\Delta P/P$).

In a constant-cost industry, the long-run supply curve is horizontal, and thus the long-run supply elasticity is infinitely large. (A small increase in price will induce an extremely large increase in output.) In an increasing-cost industry, however, the long-run supply elasticity will be positive but finite.

Because industries can adjust and expand in the long run, we would expect that *long-run elasticities of supply is generally larger than short-run elasticities*. The magnitude of the elasticity will depend on the extent to which input costs increase as the market expands. For example, an industry that depends on inputs that are widely available will have a more elastic long-run supply than will an industry that uses inputs in short supply.

9.4 Gains and Losses from Government Policies

In economics, supply and demand analysis is a tool that can be used to evaluate the impact of various economic policies. This analysis can be applied to a wide variety of problems, including situations in which: a consumer faced with a purchasing decision; a firm faced with a long-range planning problem; a government agency that has to design a policy and evaluate its likely impact. We also use consumer and producer surplus to demonstrate the efficiency of a competitive market.

9.4.1 Consumer and Producer Surplus

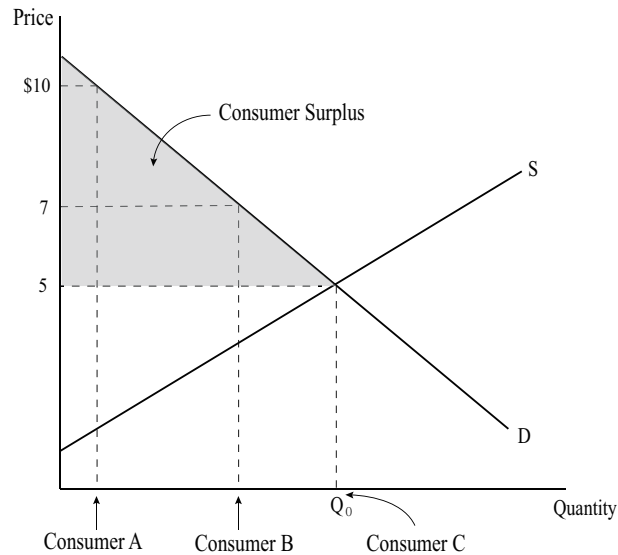


Figure 9.8 Consumer surplus

Consumer surplus for a good measures the total benefit to all consumers, is the shaded area between the demand curve and the market price for the good. It is represented graphically by the shaded area between the demand curve and the market price in Figure 9.8.

Consumer A would pay \$10 for a good whose market price is \$5 and therefore enjoys a benefit of \$5. Consumer B enjoys a benefit of \$2, and Consumer C, who values the good at exactly the market price, enjoys no benefit.

Producer surplus for a good measures the total profits of all producers in the industry, plus rents to factor inputs. It is the benefit that lower-cost producers enjoy by selling the good at the market price, which is the area below the market price and above the market supply curve, between 0 and output q^* as depicted in Figure 9.9.

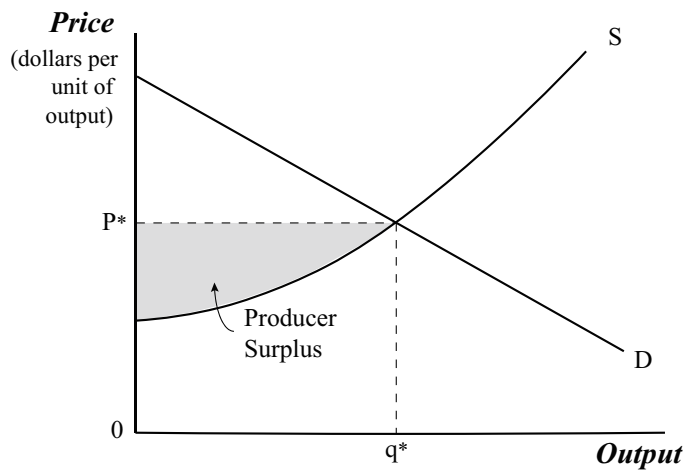


Figure 9.9 Producer surplus for a market

Together, consumer and producer surplus measure the **welfare benefit of a competitive market** as shown in Figure 9.10. When a market is in equilibrium, the total surplus (consumer and producer) is maximized.

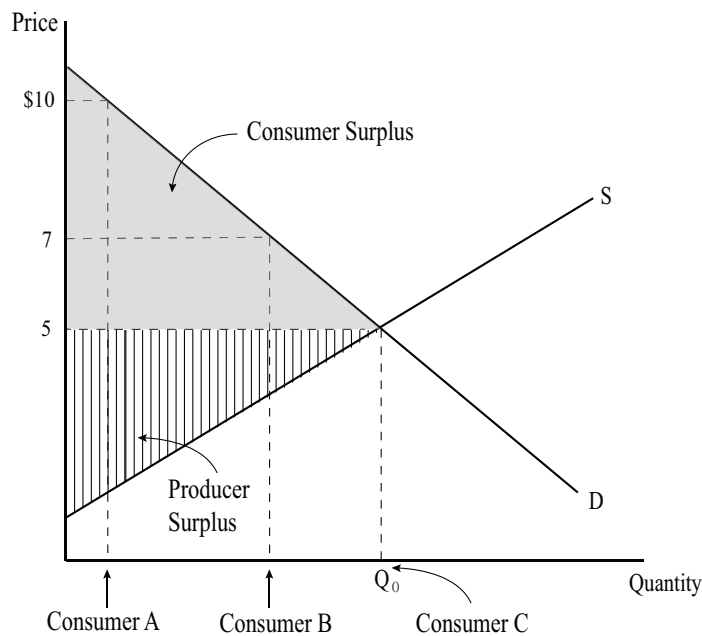


Figure 9.10 Consumer and producer surplus

Deadweight loss refers to net losses of total (consumer plus producer) surplus. This can happen, for example, when a market is not competitive due to government intervention, such as price controls or taxes.

Welfare Effects: Gains and Losses to Consumers and Producers

When the price of a good or service is regulated to be no higher than a ceiling price P_{\max} , which is below the market-clearing price P_0 , the gain to consumers is the difference between rectangle A and triangle B (i.e., the gain = $A - B$). The loss to producers is the sum of rectangle A and triangle C (i.e., the loss = $A + C$). Triangles B and C together measure the deadweight loss from price controls, as shown in Figure 9.11.

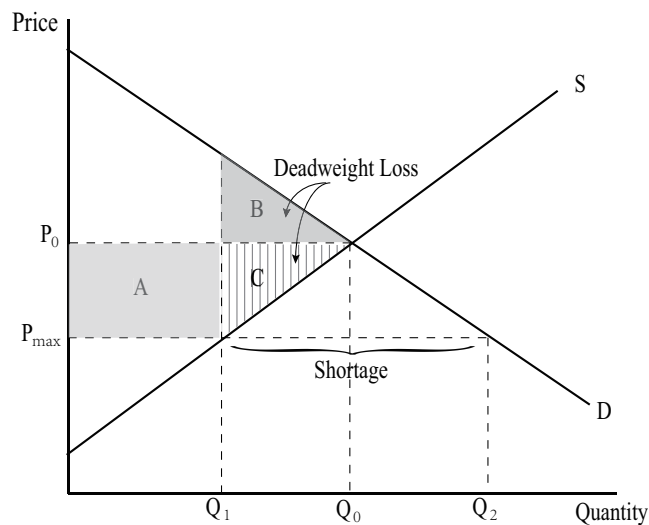


Figure 9.11 Effect of price ceiling

If demand is sufficiently inelastic, triangle B can be larger than rectangle A . In this case, consumers suffer a net loss from price controls as shown in Figure 9.12. The overall effect of a policy on welfare can be evaluated by comparing the gains and losses to consumers and producers, as well as the deadweight loss.

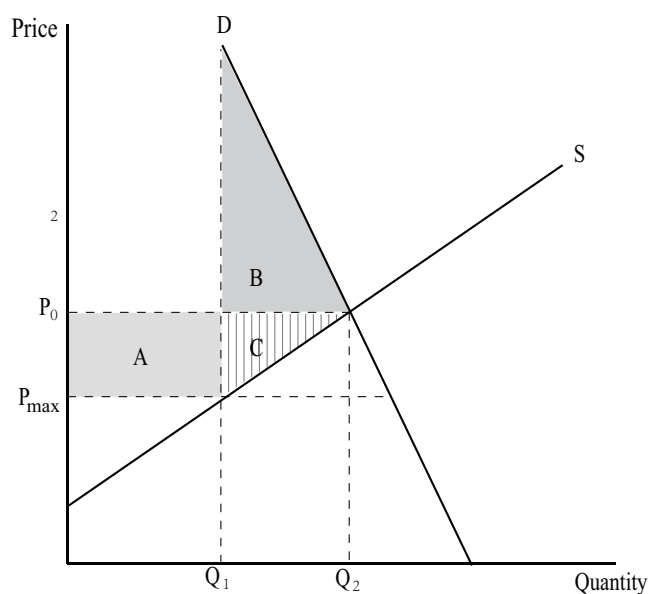


Figure 9.12 Effect of price control when demand is inelastic

9.4.2 The Efficiency of Competitive Markets

Economic efficiency: Maximization of aggregate consumer and producer surplus.

Market failure: Situation in which an unregulated competitive market is inefficient because prices fail to provide proper signals to consumers and producers.

There are two important instances in which market failure can occur:

- Externalities
- Lack of Information

Externality: Action taken by either a producer or a consumer which affects other producers or consumers but is not accounted for by the market price.

Market failure can also occur when consumers lack information about the quality or nature of a product and so cannot make utility-maximizing

purchasing decisions. Government intervention (e.g., requiring “truth in labeling”) may then be desirable.

Welfare Loss When Price is Held Above the Market-Clearing Level

When the price is regulated to be no lower than P_2 , which is the minimum price, only Q_3 will be demanded. If Q_3 is produced, the deadweight loss is given by triangles B and C , as shown in Figure 9.13. However, at price P_2 , producers would like to produce more than Q_3 . If they do, the deadweight loss will be even larger as we will discuss below.

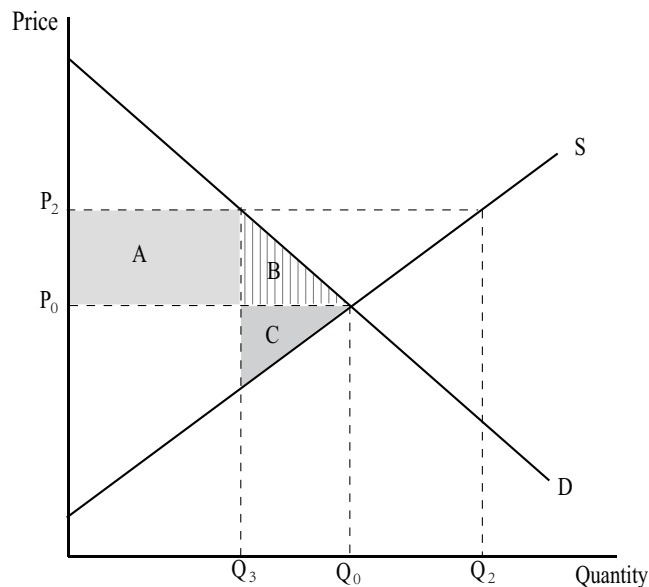


Figure 9.13 Welfare loss when price is held above market-clearing level

9.5 Minimum Price

As shown in 9.13, if producers correctly anticipate that they can sell only the lower quantity Q_3 , the net welfare loss will be given by triangles B and C . What happens if producers think they can sell at thy want at the higher price and produce accordingly?

Suppose that the price is regulated to be no lower than P_{\min} as in Figure 9.14. Producers would like to supply Q_2 , but consumers will buy only Q_3 . Then the amount $Q_2 - Q_3$ will go unsold and thus the change in producer surplus will be $A - C - D$. In this case, producers as a group may be worse off.

The total change in consumer surplus is:

$$\Delta CS = -A - B.$$

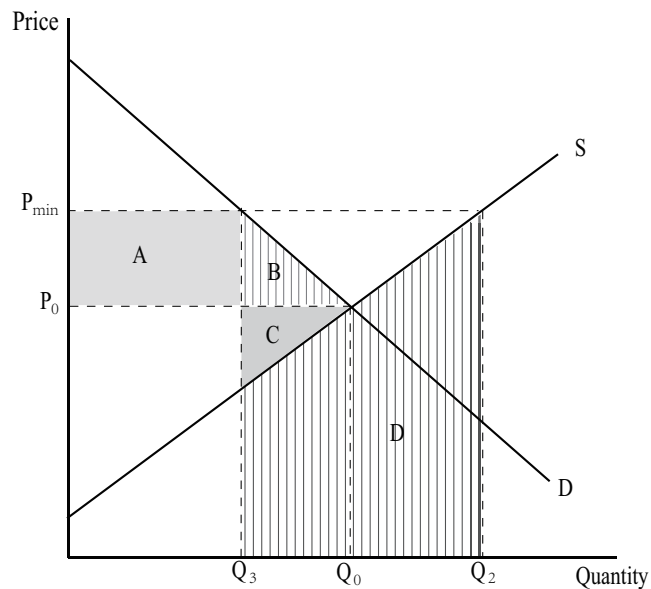


Figure 9.14 Price minimum

The total change in producer surplus is

$$\Delta PS = A - C - D.$$

Therefore, the net welfare loss is $C + B + D$, which is even higher.

Minimum Wage

Although the market-clearing wage is w_0 , firms are not allowed to pay less than w_{\min} .

This results in unemployment of an amount $L_2 - L_1$ and a deadweight loss given by triangles B and C in Figure 9.15.

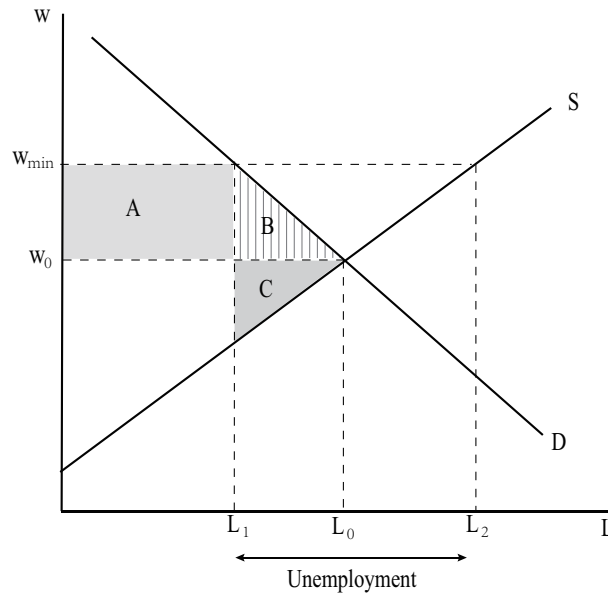


Figure 9.15 Deadweight loss from minimum wage is triangles B and C

Example 9.2 (Airline Regulation) Airline deregulation in 1981 led to major changes in the industry. Some airlines merged or went out of business as new ones entered. Although prices fell considerably (to the benefit of consumers), profits overall did not fall much.

At price P_{\min} , airlines would like to supply Q_2 , well above the quantity Q_1 that consumers will buy.

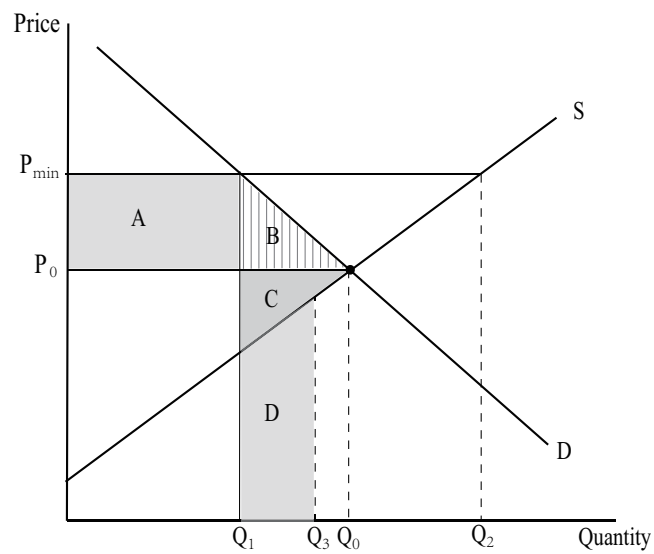


Figure 9.16 Effect of airline regulation by the Civil Aeronautics Board

When they supply Q_3 , trapezoid D is the cost of unsold output. Airline profits may have been lower as a result of regulation because triangle C and trapezoid D can together exceed rectangle A . In addition, consumers lose $A + B$.

Part IV

Market Structure and Competitive Strategy

Part 3 examines a broad range of markets and explains how the pricing, investment, and output decisions of firms depend on market structure and the behavior of competitors.

Chapter 10

Monopoly and Monopsony

Monopoly is the opposite of perfect competition. While perfect competition is characterized by many firms selling in the same market, monopoly is characterized by only one firm selling in a given market. In this chapter, we explain how a monopoly determines price and output, and compare the results with those of the competitive industry. We will then discuss monopsony which is characterized by only one buyer of a good.

10.1 The Nature of Monopoly

Monopoly: A form of market structure in which there is only one seller of some product that has no close substitutes. As a result, the monopoly is the industry because it is the only producer in the market.

Monopoly is the opposite of perfect competition since there is no competition. The monopoly need not be concerned with the possibility that other firms may undercut its price.

Monopsony: Market with only one buyer.

Market power (also known as the **monopoly power** for a seller or **monopsony power** for a buyer): Ability of a seller or buyer to affect the price of a good.

10.2 Sources of Monopoly Power

How does monopoly power come about?

1. **Exclusive ownership of a unique resource:** A firm may hold a monopoly power by owning exclusive rights to a unique resource, such as De Beers Co. of South Africa owning most of the world's diamond mines.
2. **Economies of scale:** When economies of scale are large, a firm's long-run average total cost (LRATC) curve will fall over a suitable range as output is increased. The first firm to enter this industry has a competitive advantage because it can take advantage of low per unit costs at higher levels of output, whereas a new firm would have higher per unit costs producing at low levels of output. Thus, the existing firm could charge a lower price than new firms could afford, and rivals will not enter the market, leading to monopoly power. This kind of monopoly is known as a **natural monopoly**, as seen in public utilities and telephone services.

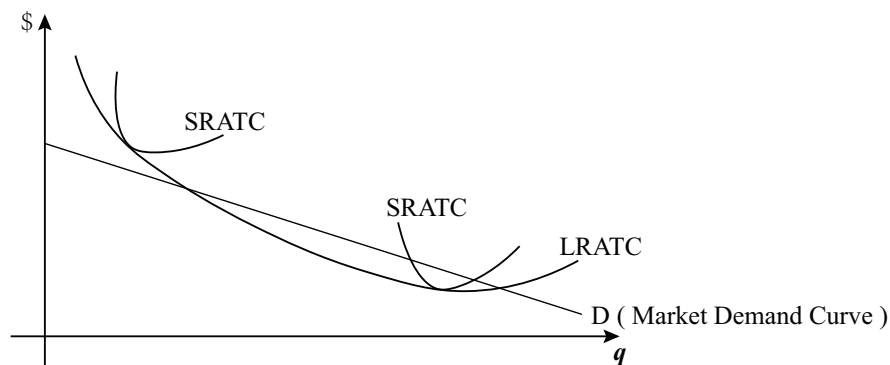


Figure 10.1 LRATC curve under monopoly

3. **Government-granted monopoly:** The government can grant exclusive rights to produce and sell a product or service through patents,

licenses, copyrights, or exclusive franchises.

- **Patents:** Give inventors a monopoly position for the lifetime of the patent (17 years after the patent was granted in the U.S.A.), as seen with companies like IBM and Xerox.
 - **Copyrights:** Give writers and composers exclusive legal controls over the production and reproduction of their work for 70 years after the death of the author.
 - **Licenses:** Limit the number of producers but rarely give monopoly power, such as licenses needed to practice medicine, law, cut hair, or sell liquor.
 - **Public utilities:** Competition is impractical, so industries are given exclusive franchise by the government. If firms share the market, none would be able to take advantage of the large economies of scale. If only one firm supplies the market, it can take advantage of the lower per-unit costs. In return for the granted monopoly position, the government is allowed to regulate the price of the product.
4. **Cooperation/Collusion:** Firms may not compete aggressively when they know competition will significantly reduce their profits. They may even collude (in violation of the antitrust laws), agreeing to limit output and raise prices. Other things being equal, monopoly power will be larger when they cooperate. Collusion can generate substantial monopoly power.

10.3 The Monopoly's Demand and Marginal Revenue Curves

Under perfect competition each firm is a price taker and thus faces a horizontal demand curve. By contrast, the monopolist comprises the entire in-

dustry. Thus, the firm's (monopolist's) demand curve is industry demand curve. Then a monopolist's demand curve is downward sloping—i.e., the firm is a price “maker”.

Recall that

- TR: Total Revenue = $P \times Q$;
- MR: Marginal Revenue = $\frac{\Delta TR}{\Delta Q}$;
- AR: Average Revenue = $\frac{P \times Q}{Q} = P$.

Since the demand curve is always the AR curve (i.e., $P = AR$), which is downward sloping for a monopolist, *marginal revenue must be less than average revenue*, and thus we generally have

$$MR < P.$$

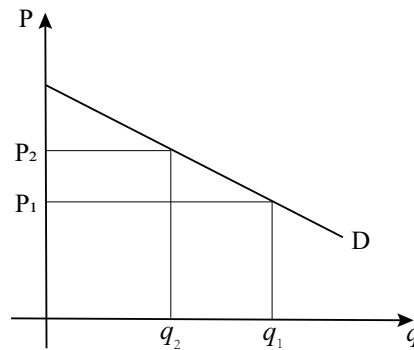


Figure 10.2 Downward-sloping demand curve under monopoly

Indeed, since

$$MR = \frac{\Delta TR}{\Delta Q} = \frac{P\Delta Q + Q\Delta P}{\Delta Q} = P + Q\frac{\Delta P}{\Delta Q}, \quad (10.1)$$

$Q > 0$ and $\frac{\Delta P}{\Delta Q} < 0$, again we have $MR < P$.

Intuitively, the extra revenue from an incremental unit of quantity has two components: (1) producing one extra unit and selling it at P brings

10.3. THE MONOPOLY'S DEMAND AND MARGINAL REVENUE CURVES 195

in revenue P ; and (2) because the firm faces a downward-sloping demand curve, producing and selling this extra unit also results in a small drop in price $\Delta P/\Delta Q$, which reduces the revenue from all units sold (i.e., a change in revenue $q \times \Delta P/\Delta Q$).

Example 10.1 Suppose that the demand curve facing a monopolist is given by

$$P = 11 - Q.$$

Q	$P=AR$	TR	MR
0	\$11	0	—
1	10	10	10
2	9	18	8
3	8	24	6
4	7	28	4
5	6	30	2
6	5	30	0
7	4	28	-2
8	3	24	-4
9	2	18	-6
10	1	10	-8

For a general linear demand function

$$P = a + bq,$$

$TR = P \times q = aq + bq^2$, and then we have

$$MR = \frac{\Delta TR}{\Delta q} = a + 2bq.$$

Therefore, the slope of the MR curve is $2b$, which is exactly twice the slope of the demand function, b .

10.4 Monopolist's Decision

10.4.1 Profit Maximization

The monopolist has control over both price and quantity, making pricing and output policies interdependent. To maximize profit, the monopolist must consider both policies simultaneously.

Conditions for monopolist's profit maximization:

- 1) $P \geq AVC$ (necessary condition for producing);
- 2) $MR = MC$ (how much will it be produced).

Graphically, the monopolist's profit-maximizing output can be illustrated by the point where the MC curve intersects the MR curve, as shown in Figure 10.3.

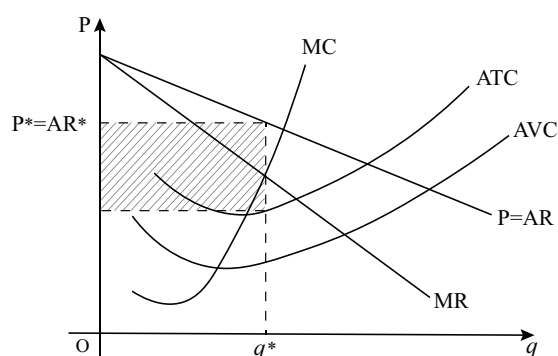


Figure 10.3 Profit maximization for a monopolist

If $P < AVC$, then the firm cannot even cover its variable costs and will shut down in the short run. If $AVC \leq P < ATC$, then the firm produces where $MR = MC$, which maximizes profits. If $P \geq ATC$, then the firm can earn normal profits.

Profit Maximization: $P > ATC > AVC$

1. Use $MR = MC$ to determine q^* .
2. Use q^* and $P = AR$ (= demand) to decide P^* .

3. $TR = AR \times q^* = P^* \times q^*$.
4. Use q^* and ATC to get TC. $TC = ATC \times q^*$.
5. Profit = $TR - TC$.

Loss Minimization: $ATC > P > AVC$

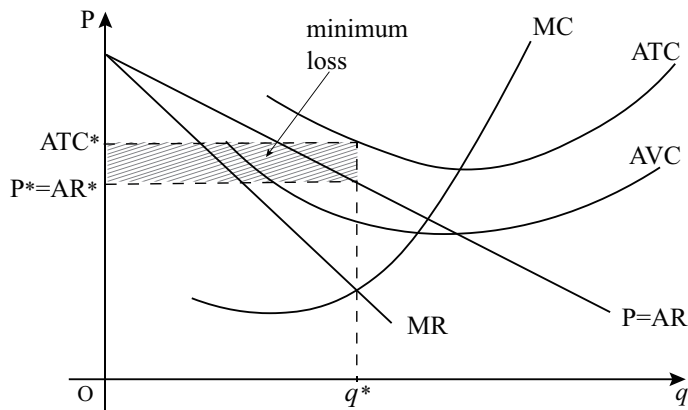


Figure 10.4 Loss minimization for a monopolist

Production Shutdown: $ATC > AVC > P$

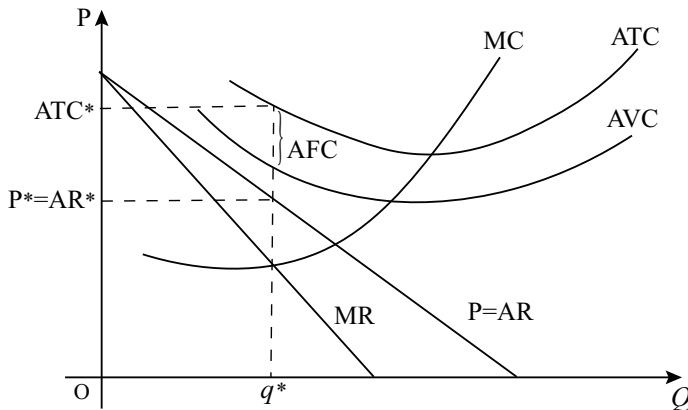


Figure 10.5 Production shutdown for a monopolist

$q^* = 0$ is the loss-minimizing level of output.

Normal Profit: $ATC = P$

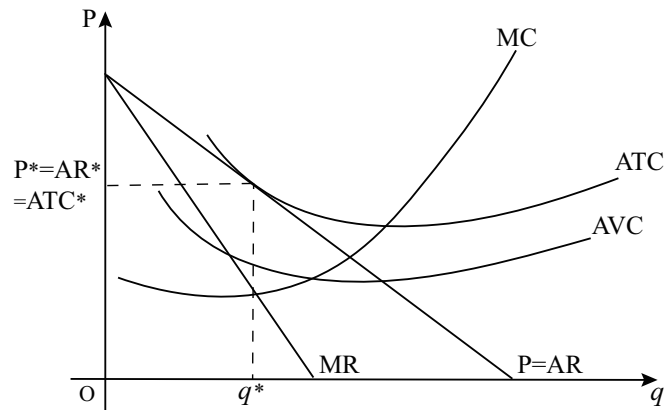


Figure 10.6 Normal profit for a monopolist

$TR = TC \Rightarrow \text{Economic Profit} = 0 \Rightarrow$ a normal profit is earned.

Example 10.2 A monopolist can produce at a constant average (and marginal) cost of

$$AC = MC = 2.$$

It faces a market demand curve given by

$$Q = 10 - P.$$

The revenue for the monopolist is

$$TR = PQ = (10 - Q)Q = 10Q - Q_1^2.$$

Then, the marginal revenue is given by

$$MR = \Delta R / \Delta Q = 10 - 2Q.$$

Setting $MR = MC$ and solving for Q , the monopolist's profit-maximizing quantity, profit, and profit are, respectively, given by

$$Q^* = 4, \tag{10.2}$$

$$P^* = 6, \quad (10.3)$$

and

$$\pi = TR - TC = Q^*(P^* - AC) = 16. \quad (10.4)$$

Long-Run: A monopolist can earn economic profits in the long run, unlike a perfectly competitive firm. This is because the monopolist can restrict output and charge higher prices, leading to higher profits.

10.4.2 The Multiplant Firm

Suppose that a firm has two plants. What should its total output be, and how much of that output should each plant produce? We can find the answer intuitively in two steps.

- **Step 1.** Whatever the total output, it should be divided between the two plants so that marginal cost is the same in each plant. Otherwise, the firm could reduce its costs and increase its profit by reallocating production.
- **Step 2.** We know that total output must be such that marginal revenue equals marginal cost. Otherwise, the firm could increase its profit by raising or lowering total output.

We can derive this result algebraically. Let Q_1 and C_1 be the output and cost of production for Plant 1, Q_2 and C_2 be the output and cost of production for Plant 2, and $Q_T = Q_1 + Q_2$ be total output. Then profit is

$$\Pi = PQ_T = PQ_1 + PQ_2 - c_1(Q_1) - c_2(Q_2),$$

and thus we have

$$MR = MC_1 = MC_2.$$

Therefore, a firm with two plants maximizes profits by choosing output levels Q_1 and Q_2 so that marginal revenue MR (which depends on total

output) equals marginal costs for each plant, MC_1 and MC_2 , as depicted in Figure 10.7.

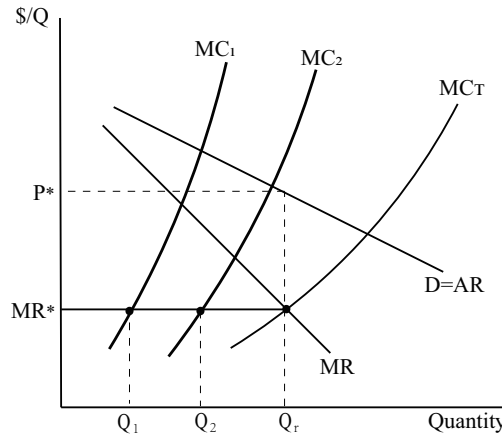


Figure 10.7 Producing with two plants

10.4.3 Relationships between MR, Price, and E_d^P

The relationship between MR, price, and price elasticity of demand (E_d^P) can be expressed as

$$MR = P \left(1 + \frac{1}{E_d^P} \right) \quad (10.5)$$

since

$$MR = P + Q \frac{\Delta P}{\Delta Q} = P \left(1 + \frac{Q}{P} \times \frac{\Delta P}{\Delta Q} \right) = P \left(1 + \frac{1}{E_d^P} \right).$$

Therefore, **the less elastic its demand curve, the more monopoly power a firm has**. The ultimate determinant of monopoly power is, therefore, the firm's elasticity of demand.

By Formula (10.5), we have the following facts:

1. When the elasticity of demand is infinity (a horizontal demand curve), then $MR = P$:

$$MR = P \left(1 - \frac{1}{\infty} \right) = P.$$

2. When demand is unit elastic ($E_d^P = -1$), then $MR = 0$:

$$MR = P \left(1 - \frac{1}{1} \right) = 0.$$

3. When demand is elastic ($|E_d^P| > 1$), then $MR > 0$; e.g., let $E_d^P = -2$:

$$MR = P \left(1 - \frac{1}{2} \right) = \frac{1}{2}P > 0.$$

4. When demand is inelastic ($|E_d^P| < 1$), then $MR < 0$; e.g., let $E_d^P = -\frac{1}{2}$:

$$MR = P \left(1 - \frac{1}{1/2} \right) = P(1 - 2) = -P < 0.$$

Factors affecting the elasticity of demand of a monopolist

- **The elasticity of market demand.** Because the firm's own demand will be at least as elastic as market demand, the elasticity of market demand limits the potential for monopoly power.
- **The number of firms in the market.** If there are many firms, it is unlikely that any one firm will be able to affect the price significantly.
- **The interaction among firms.** Even if there are only a few firms in the market, each firm will be unable to profitably raise the price very much if the rivalry among them is aggressive, with each firm trying to capture as much of the market share as it can.

It is important to distinct the elasticity of market demand and the elasticity of demand of an individual firm which could be much higher.

Example 10.3 (Elasticity of Demand for Soft Drinks) Soft drinks provide a good example of the difference between a market elasticity of demand and a firm's elasticity of demand.

A recent review of statistical studies found that the market elasticity of demand for soft drinks is between -0.8 and -1.0.6. That means that if all

soft drink producers increased the prices of all of their brands by 1 percent, the quantity of soft drinks demanded would fall by 0.8 to 1.06 percent.

The demand for any individual soft drink, however, will be much more elastic, because consumers can readily substitute one drink for another. Although elasticities will differ across different brands, studies have shown that the elasticity of demand for, say, Coca Cola is around -5. In other words, if the price of Coke were increased by 1 percent but the prices of all other soft drinks remained unchanged, the quantity of Coke demanded would fall by about 5 percent.

Students-and business people-sometimes confuse the market elasticity of demand with the firm (or brand) elasticity of demand. Make sure you understand the difference.

10.4.4 A Rule of Thumb for Pricing

With limited knowledge of average and marginal revenue, we can derive a rule of thumb that can be more easily applied in practice. From (10.5), we know that marginal revenue can be expressed as

$$MR = P \left(1 + \frac{1}{1/E_d^P} \right).$$

Setting $MR = MC$ for profit maximization leads to

$$P \left(1 + \frac{1}{1/E_d^P} \right) = MC, \quad (10.6)$$

which can be rearranged to get the so-called **markup equation**:

$$P = \frac{MC}{1 + 1/E_d^P}. \quad (10.7)$$

Since $E_d^P < 0$, in order to ensure that the price is non-negative, the firm must produce *within the range of the elastic demand*. Therefore, we have $[1 + 1/E_d^P] \leq 1$ or equivalently, $\frac{1}{1+1/E_d^P} \geq 1$, which implies that the price is

not less than the marginal cost at profit maximization.

This formula is very useful and provides a basic principle of pricing for any market structure. It reveals that the price equals the marginal cost multiplied by the markup factor $\frac{1}{1+1/E_d^P}$, which is a decreasing function of the price elasticity of demand E_d^P . That is, given a marginal cost, the optimal pricing of the product is inversely proportional to the price elasticity of demand, which means that the smaller the elasticity, the greater the market power and thus the higher the price. When the market is perfectly competitive, E_d^P is infinitely large, and we have $P = MC$.

Example 10.4 (Markup Pricing) Although the elasticity of market demand for food is small (about -1), no single supermarket can raise its prices very much without losing customers to other stores.

The elasticity of demand for any one supermarket is often as large as -10. We then find that by markup equation (10.7),

$$P = MC/(1 - 0.1) = MC/(0.9) = (1.11)MC,$$

which is about 11 percent above marginal cost.

Small convenience stores typically charge higher prices because its customers are generally less price sensitive. Because the elasticity of demand for a convenience store is about -5, the markup equation (10.7) implies that its prices should be about 25 percent above marginal cost. With designer jeans, demand elasticities in the range of -2 to -3 are typical. This means that price should be 50 to 100 percent higher than marginal cost.

Example 10.5 (Astra-Merck Prices Prilosec) In 1995, Prilosec, represented a new generation of antiulcer medication. Prilosec was based on a very different biochemical mechanism and was much more effective than earlier drugs. By 1996, it had become the best-selling drug in the world and faced no major competitor.

Astra-Merck was pricing Prilosec at about \$3.50 per daily dose. The marginal cost of producing Prilosec is only about 30 to 40 cents per dose.

The price elasticity of demand should be in the range of roughly -1.0 to -1.2. Setting the price at a markup exceeding 400 percent over marginal cost is consistent with our rule of thumb for pricing.

10.4.5 Measuring Monopoly Power

The important distinction between a perfectly competitive firm and a firm with monopoly power: For the competitive firm, price equals marginal cost; for the firm with monopoly power, price exceeds marginal cost.

Lerner Index of Monopoly Power: A measure of monopoly power calculated as excess of price over marginal cost as a fraction of price:

$$L = \frac{P - MC}{P},$$

which is also equal to minus the inverse of E_d^p by equation (10.6):

$$L = \frac{P - MC}{P} = -\frac{1}{E_d^p}.$$

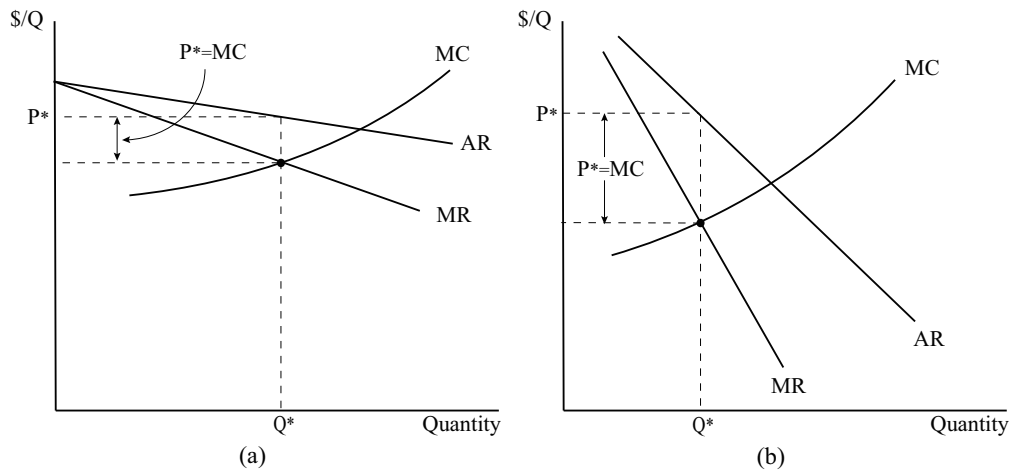


Figure 10.8 Elasticity of demand and price markup

Thus, if the firm's demand is elastic, as in (a) of Figure 10.8, the markup

is small and the firm has little monopoly power. The opposite is true if demand is relatively inelastic, as in (b) of Figure 10.8.

10.5 Further Implications of Monopoly Analysis

Monopoly Has No Supply Curve

Under perfect competition, there is a corresponding quantity of output that a firm is willing to supply at any given price. Conversely, at any specific output level, there is a corresponding price that makes the firm willing to supply that output level. However, this relationship does not exist for a monopolist. *Monopoly has no supply curve* since the quantity supplied at any particular price depends on the monopolist's demand curve.

Consider the two possible demand curves in Figure 10.9: MR_1 and MR_2 intersecting MC at the same point. If the demand curve is D_1 , then the price is P_1 . If the demand curve is D_2 , then the price is P_2 . Thus, there is no one-to-one relationship between price and the quantity produced, and hence the MC curve cannot be a supply curve for a monopolist. Therefore, a monopolist has no supply curve.

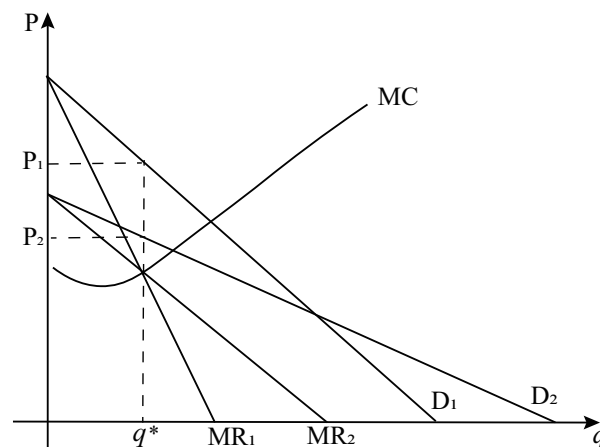


Figure 10.9 No supply curve: A change in demand only changes the price charged

Also, shifts in demand can result in a change in output with no change in price, or changes in both price and output.

10.6 Monopoly versus Perfect Competition

In a perfectly competitive industry, the market is characterized by the equation $S = \sum_i MC_i$, where S represents the supply curve and MC_i represents the marginal cost curve of each firm. The market equilibrium occurs where $S = D$, where D represents the market demand curve, resulting in the equilibrium price P^c and quantity q^c , as shown in Figure 10.10.

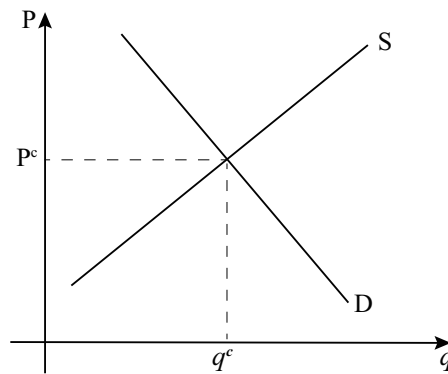


Figure 10.10 Market equilibrium under perfect competition

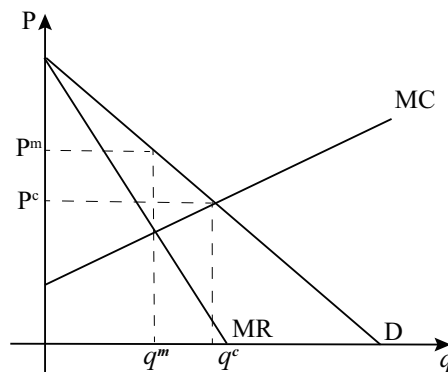


Figure 10.11 Market equilibrium under monopoly

On the other hand, in a monopoly, a single firm takes over all firms in the market. The monopolist sets the price at the point where marginal revenue MR equals marginal cost MC , resulting in the equilibrium price P^m and quantity q^m , as shown in Figure 10.11.

Therefore, when a market is a monopoly, consumers pay a higher price and receive less than they would under perfect competition.

10.7 The Social Cost of Monopoly Power

10.7.1 Income Distribution Problem

When a competitive industry becomes a monopoly, there will be a change in the distribution of real income among members of society. The monopolist gains at the expense of the consumers who pay a higher price, resulting in a redistribution of income from consumers to the owners of the monopoly. This reduces the real purchasing power, or real income, of the consumers. Therefore, the income distribution problem is a social cost of monopoly power.

10.7.2 Inefficient Allocations

Monopoly has another effect that involves a net loss in welfare because it leads to an inefficient allocation. Economists refer to this net loss as a social cost of monopoly.

The shaded rectangle and triangles in Figure 10.12 show changes in consumer and producer surplus when moving from competitive price and quantity, P_c and Q_c , to a monopolist's price and quantity, P_m and Q_m .

Because of the higher price, consumers lose $A + B$ and producer gains $A - C$. The deadweight loss is $B + C$.

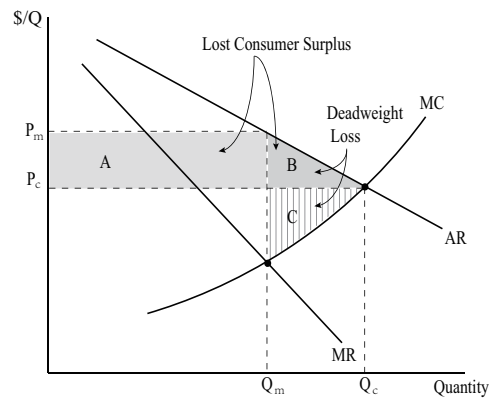


Figure 10.12 Deadweight Loss from Monopoly Power

Price Regulation

How can we solve the inefficiency issue of monopoly? One way is to regulate the price, especially to the competitive price.

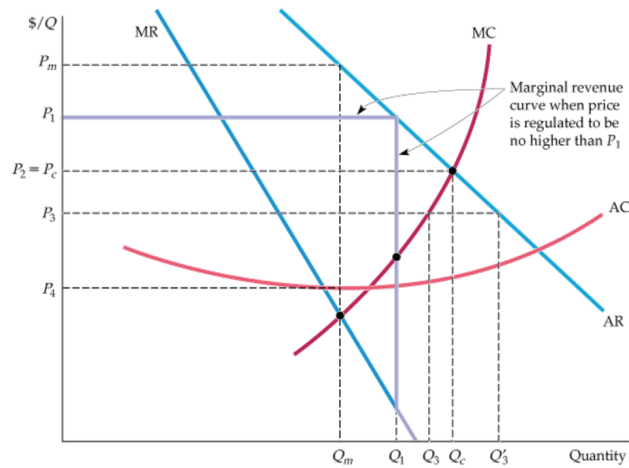


Figure 10.13 Price Regulation

If left alone, a monopolist produces Q_m and charges P_m as shown in 10.13. When the government imposes a price ceiling of P_1 the firm's average and marginal revenue are constant and equal to P_1 for output levels

up to Q_1 . For larger output levels, the original average and marginal revenue curves apply. The new marginal revenue curve is, therefore, the dark purple line, which intersects the marginal cost curve at Q_1 .

When price is lowered to P_c , at the point where marginal cost intersects average revenue, output increases to its maximum Q_c . This is the output that would be produced by a competitive industry.

Lowering price further, to P_3 , reduces output to Q_3 and causes a shortage, $Q'_3 - Q_3$.

10.8 Benefits of Monopoly: Corporate Innovation

Despite the social costs associated with monopoly, it has certain merits, particularly when it comes to incentivizing firms to innovate and develop new products.

Monopoly profits are often the result of corporate innovation. However, these considerable profits also attract other firms to enter the market and compete, leading to decreased profits. This creates a cycle of competition, innovation, monopoly, and competition once again. Through this cycle, market competition leads to market equilibrium, while innovation disrupts it, motivating firms to continuously pursue innovation. This cycle promotes long-term vitality in the market economy, increases social welfare, and encourages economic development. It highlights the unique beauty and power of the market system.

To encourage innovation, governments should enact intellectual property protection laws. However, to prevent fixed or permanent oligopolies and monopolies from arising, anti-monopoly laws and intellectual property rights legislation should only be in effect for a limited time.

Therefore, competition and monopoly are two sides of the same coin, just like supply and demand. Together, they form an awe-inspiring dialectical unity of opposites under market forces, showcasing the beauty and power of the market system.

10.9 Monopsony

Monopsony power: Buyer's ability to affect the price of a good.

Oligopsony: Market with only a few buyers.

Marginal value (MV): Additional benefit derived from purchasing one more unit of a good.

Marginal expenditure (ME): Additional cost of buying one more unit of a good.

Average expenditure (AE): Price paid per unit of a good.

10.9.1 Competitive Buyer Compared to Competitive Seller

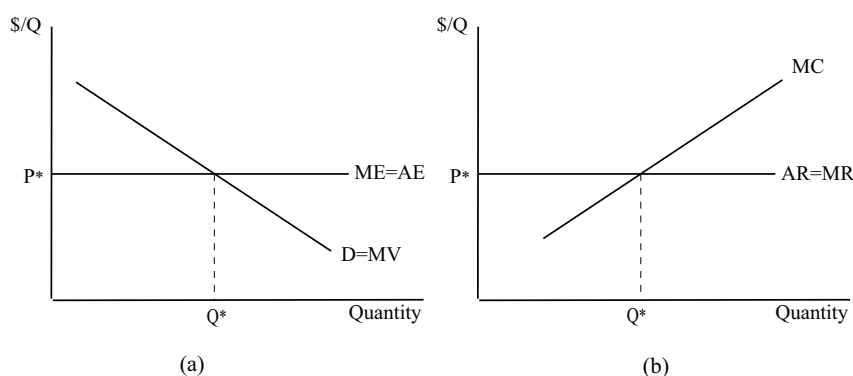


Figure 10.14 Competitive buyer compared to competitive seller

In Figure 10.14.(a), the competitive buyer takes price P^* as given, hence marginal expenditure and average expenditure are constant and equal; quantity purchased is found by price equating marginal value (demand): $ME = AE = P$.

In Figure 10.14.(b), the competitive seller also takes price as given. Marginal revenue and average revenue are constant and equal; quantity sold is found by equating price to marginal cost: $MR = AR = P$

10.9.2 Monopsony Buyer

The market supply curve is the monopsonist's average expenditure curve AE . Because average expenditure is rising, marginal expenditure lies above it.

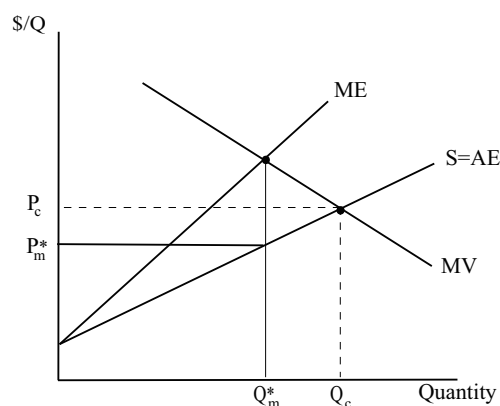


Figure 10.15 Monopsonist buyer

In Figure 10.15, the monopsonist purchases quantity Q_m^* , where marginal expenditure and marginal value (i.e., demand) intersect.

The price paid per unit P_m^* is then found from the average expenditure (i.e., supply) curve. In a competitive market, price and quantity, P_c and Q_c , are both higher. They are found at the point where average expenditure (supply) and marginal value (demand) intersect.

Monopoly and Monopsony

The diagrams in Figure 10.16 illustrate the close analogy between monopoly and monopsony.

1. The monopolist produces at the point where marginal revenue intersects marginal cost. In this situation, average revenue (i.e., demand) is greater than marginal revenue, causing the price to exceed marginal cost.

2. The monopsonist purchases up to the point where marginal expenditure intersects marginal value. In this case, marginal expenditure exceeds average expenditure (i.e., supply), causing marginal value to exceed the price.

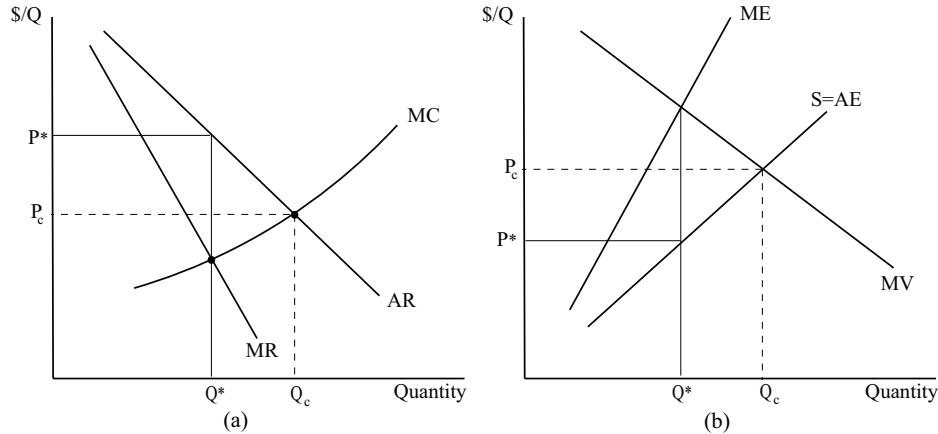


Figure 10.16 Monopoly and Monopsony

In both cases, the market power of the single buyer or seller leads to a distortion of the market outcome, resulting in a price that differs from the competitive price and a quantity that is lower than the competitive quantity.

10.10 Monopsony Power

10.10.1 Monopsony Power: Elastic versus Inelastic Supply

The degree of monopsony power depends on the elasticity of supply. When supply is elastic, as in Figure 10.17.(a), the marginal expenditure and average expenditure do not differ by much, so the price is close to what it would be in a competitive market. However, when supply is inelastic, as in Figure 10.17.(b), the monopsonist can significantly reduce the price and pay less than the marginal cost of production.

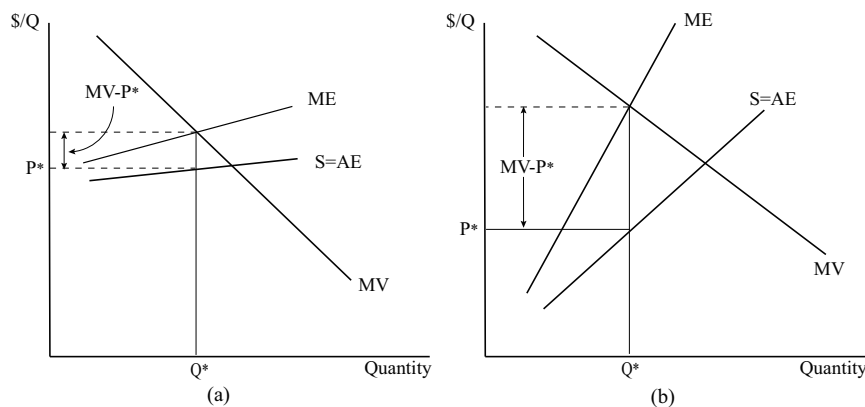


Figure 10.17 Monopsony power: elastic versus inelastic supply.

10.10.2 Sources of Monopsony Power

There are several sources of monopsony power:

- **Elasticity of market supply:** If only one buyer is in the market—a pure monopsonist—its monopsony power is completely determined by the elasticity of market supply. If supply is highly elastic, monopsony power is small, and there is little gain in being the only buyer.
- **Number of buyers:** When the number of buyers is very large, no single buyer can have much influence over price. Thus each buyer faces an extremely elastic supply curve, and the market is almost completely competitive.
- **Interaction among buyers:** If buyers in a market compete aggressively, they will bid up the price close to their marginal value of the product, and will thus have little monopsony power. On the other hand, if those buyers compete less aggressively, or even collude, prices will not be bid up very much, and the degree of monopsony power might be nearly as high as if there were only one buyer.

10.10.3 The Social Costs of Monopsony Power

The shaded rectangle and triangles in Figure 10.18 show changes in buyer and seller surplus when moving from competitive price and quantity, P_c and Q_c , to the monopsonist's price and quantity, P_m and Q_m .

Because both price and quantity are lower, there is an increase in buyer (consumer) surplus given by $A - B$. Producer surplus falls by $A + C$, so there is a deadweight loss given by triangles B and C .

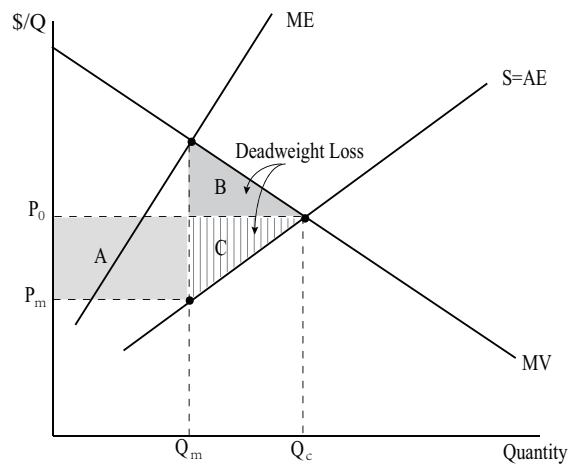


Figure 10.18 Monopsony power: elastic versus inelastic supply

10.10.4 Bilateral Monopsony

Bilateral monopoly is a market structure in which there is only one buyer and one seller. In such a market, both the buyer and the seller have market power and are in a bargaining situation, which makes it difficult to predict the price and quantity of the transaction.

Bilateral monopoly is a rare market structure, but in situations where a buyer or a seller has significant market power, the principle of bilateral monopoly still applies. Monopsony power and monopoly power tend to counteract each other, and the market outcome is somewhere between a perfectly competitive market and a monopoly market.

In general, monopsony power will push the price closer to the marginal cost, and monopoly power will push the price closer to the marginal value. However, the market outcome will depend on the relative strengths of the monopsony and monopoly power.

10.11 Limiting Market Power: The Antitrust Laws

Excessive market power can harm potential purchasers, reduce output, and lead to a deadweight loss. To address these issues, antitrust laws are designed to promote competition by prohibiting actions that restrain, or are likely to restrain, competition.

In theory, a firm's excess profits could be taxed away, but redistribution of the firm's profits is often impractical. To limit the market power of a natural monopoly, such as an electric utility company, direct price regulation is the answer.

Antitrust laws: Rules and regulations prohibiting certain practices that limit competition, such as collusion with other firms, price-fixing, predatory pricing, and exclusive dealing.

It is important to stress that, at the outset, while there are limitations (such as colluding with other firms), in general, it is not illegal to be a monopolist or to have market power. On the contrary, we have seen that patent and copyright laws protect the monopoly positions of firms that have developed unique innovations.

In cases where a firm has too much market power, antitrust authorities may also consider breaking up the firm or imposing price regulation to limit its market power.

Enforcement of Antitrust Laws

Antitrust laws are enforced through three methods:

- The Antitrust Division of the Department of Justice enforces antitrust

laws.

- The Federal Trade Commission administers antitrust laws through its administrative procedures.
- Antitrust laws can also be enforced through private proceedings.

Example 10.6 (Microsoft) Microsoft dominated the software market for personal computers, with over a 90 percent market share for operating systems and office suites. In 1998, the Antitrust Division of the U.S. Department of Justice filed a lawsuit alleging that Microsoft had illegally bundled its Internet browser with its operating system to maintain its monopoly. The court found Microsoft had illegally maintained its monopoly in violation of Section 2 of the Sherman Act.

In 2004, the European Commission accused Microsoft of monopolizing the media player market by bundling the Windows Media Player with its operating system. In 2012, the case was closed after Microsoft agreed to offer customers a choice of browsers during the initial boot-up of their new operating system.

Today, competition has shifted to the smartphone industry where Microsoft faces strong competition from Google's (Android) and Apple's (iOS) operating systems.

Chapter 11

Pricing with Market Power

11.1 Capturing Consumer Surplus

In the previous chapter, we discussed the pricing of a monopoly using a uniform price. However, in reality, firms commonly adopt differential pricing. The premise of differential pricing is that the purchase of the demander will generate consumer surplus. A monopolist may obtain some or even all of the consumer surplus through price discrimination.

Price discrimination is the practice of selling the same good or service at different prices to different buyers.

Monopolists use price discrimination to realize greater profits because they are the only supplier of a good. For example, movie theaters charge different prices for children and adults, utility companies charge different rates for businesses and residences, and senior citizens pay a lower fare for bus rides.

Conditions that aid price discrimination include:

- Resale is not possible.
- The market can be segmented by classifying buyers into separate, identifiable groups (for example, by showing identification).
- The monopolist has control over the market.

- There are different demand elasticities, such as A's demand being less elastic than B's demand. Monopolists can increase total revenue by increasing the price for A while decreasing the price for B.

There are many broadly adopted forms of price discrimination in practice. In the following, we will discuss seven of them.

11.2 First-Degree Price Discrimination

Reservation price is the maximum price that a customer is willing to pay for a good.

First-degree price discrimination is the practice of charging each customer their reservation price.

11.2.1 Capturing Consumer Surplus by Perfect Price Discrimination

Assume $MC = ATC$ is constant.

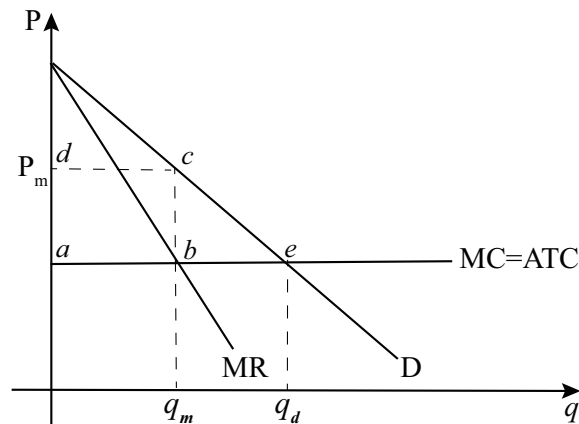


Figure 11.1 Market equilibrium under perfect price discrimination

If the same price is charged for all goods, then profit is maximized at q_m sold at p_m , and the profit is equal to the area $abcd$.

However, if the monopolist uses perfect price discrimination to charge the maximum price buyers are willing to pay for each additional unit, then the profit expands to the area between the demand curve and the marginal cost curve.

Since the demand curve is the same as the MR curve, profits are maximized where $D = MC$; that is, at q_d . Profit is now given by area $aecd$. Clearly, area $aecd > area abcd$.

11.2.2 Capturing Consumer Surplus by Imperfect Price Discrimination

Firms usually do not know the reservation price of every consumer, but sometimes reservation prices can be roughly identified. In Figure 11.2, six different prices are charged. The firm earns higher profits, but some consumers may also benefit. With a single price P_4^* , there are fewer consumers. The consumers who now pay P_5 or P_6 enjoy a surplus.

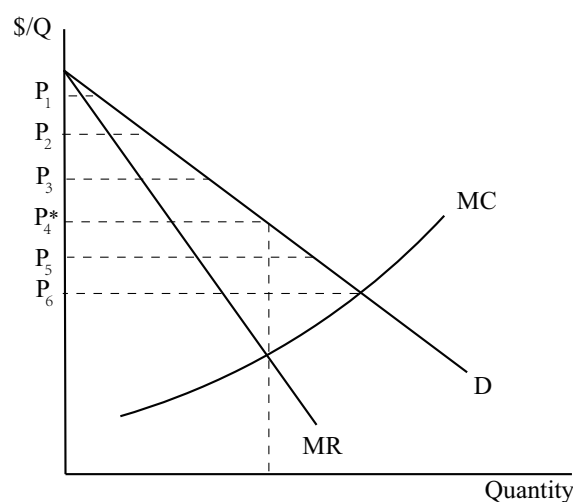


Figure 11.2 First-degree price discrimination in practice

11.3 Second-Degree Price Discrimination

Second-degree price discrimination is the practice of charging different prices per unit for different quantities of the same good or service.

Block pricing is the practice of charging different prices for different quantities or "blocks" of a good.

Different prices are charged for different quantities, or "blocks," of the same good. In Figure 11.3, there are three blocks with corresponding prices P_1 , P_2 , and P_3 .

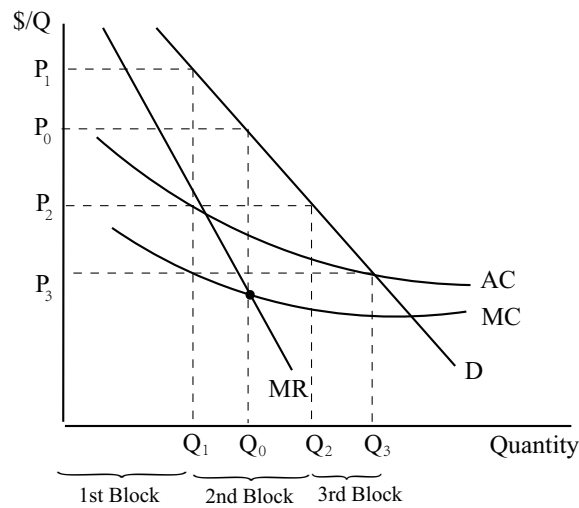


Figure 11.3 Second-degree price discrimination

There are also economies of scale, and average and marginal costs are declining. Second-degree price discrimination can then make consumers better off by expanding output and lowering cost.

11.4 Third-Degree Price Discrimination

Third-degree price discrimination is the practice of dividing consumers into two or more groups with separate demand curves and charging different prices to each group.

Creating Consumer Groups

If third-degree price discrimination is feasible, how should the firm decide what price to charge each group of consumers?

Let P_1 be the price charged to the first group of consumers, P_2 the price charged to the second group, and $C(Q_T)$ the total cost of producing output $Q_T = Q_1 + Q_2$. The total profit is then

$$\Pi = P_1Q_1 + P_2Q_2 - C(Q_T).$$

Thus, we need to ensure that

$$MR_1 = MR_2 = MC,$$

which means that the marginal revenue for each group is the same and equal to the marginal cost of production.

Therefore, using the formula

$$MR = P(1 + 1/E_d^p),$$

the relative prices are given by

$$\frac{P_1}{P_2} = \frac{(1 + 1/E_2)}{(1 + 1/E_1)}.$$

Consider Figure 11.4. Consumers are divided into two groups, with separate demand curves for each group. The optimal prices and quantities are such that the marginal revenue from each group is the same and equal to marginal cost.

Here group 1, with demand curve D_1 , is charged P_1 , and group 2, with the more elastic demand curve D_2 , is charged the lower price P_2 . Marginal cost depends on the total quantity produced Q_T . Note that Q_1 and Q_2 are chosen so that $MR_1 = MR_2 = MC$.

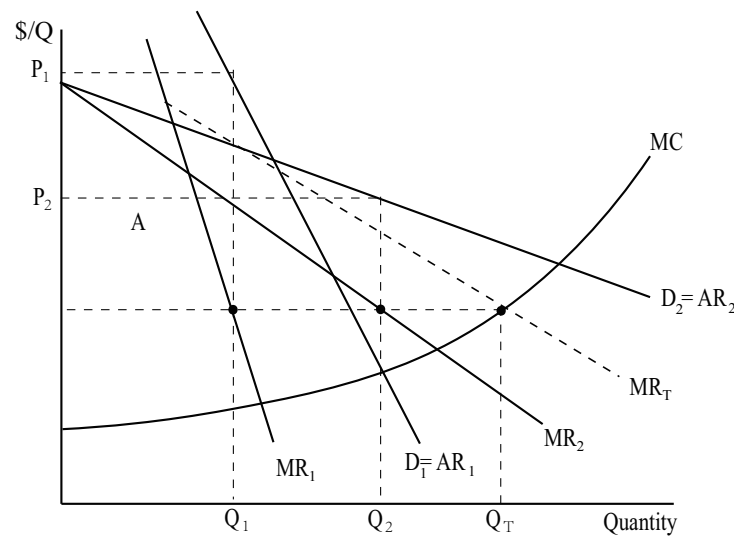


Figure 11.4 Third-degree price discrimination

Example 11.1 (Airline Fares) Travelers are often amazed at the variety of fares available for round-trip flights.

	Fare Category	Fare Category	Fare Category
Elasticity	First Class	Unrestricted Coach	Discounted
Price	-0.3	-0.4	-0.9
Income	1.2	1.2	1.8

Table 11.1: Elasticities of demand for air travel

Recently, for example, the first-class fare for round-trip flights from New York to Los Angeles was above \$2000; the regular (unrestricted) economy fare was about \$1000, and special discount fares (often requiring the purchase of a ticket two weeks in advance and/or a Saturday night stay over) could be bought for as little as \$200. These fares provide a profitable form of price discrimination. The gains from discriminating are large because different types of customers, with very different elasticities of demand, purchase these different types of tickets. Airline price discrimination has become increasingly sophisticated. A wide variety of fares is available.

Example 11.2 (The Economics of Coupons and Rebates) Coupons provide a means of price discrimination. For example, Table 11.2 shows the price elasticity of demand for users versus non-users of coupons for various products.

Product	Price Elasticity	Price Elasticity
	Nonusers	Users
Toilet	-0.60	-0.66
Stuffing/dressing	-0.71	-0.96
Shampoo	-0.84	-1.04
Cooking/salad oil	-1.22	-1.32
Dry mix dinners	-0.88	-1.09
Cake mix	-0.21	-0.43
Cat food	-0.49	-1.13
Frozen entrees	-0.60	-0.95
Gelatin	-0.97	-1.25
Spaghetti sauce	-1.65	-1.81
Creame rinse/conditioner	-0.82	-1.12
Soups	-1.05	-1.22
Hot dogs	-0.59	-0.77

Table 11.2: Price elasticity of demand for users versus nonusers of coupons

11.5 The Two-Part Tariff

A **two-part tariff** is a pricing strategy in which consumers are charged both an entry fee and a usage fee. This strategy is commonly used in practice, especially in industries where firms face high fixed costs and low variable costs.

11.5.1 Two-Part Tariff with a Single Consumer

Consider a market with a single consumer whose demand curve is represented by D in Figure 11.5. The firm can maximize profit by setting the usage fee P equal to the marginal cost and setting the entry fee T^* equal

to the entire surplus of the consumer. The resulting profit is the area of rectangle $ABCD$ in Figure 11.5.

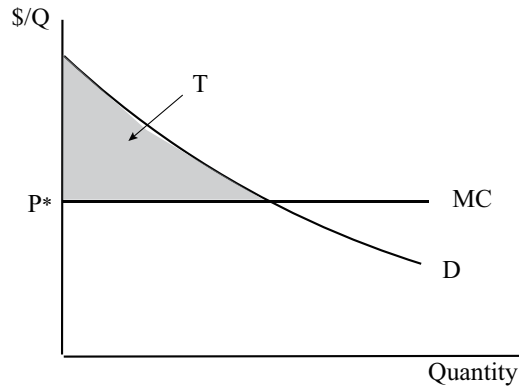


Figure 11.5 Two-Part Tariff with a Single Consumer

11.5.2 Two-Part Tariff with Two Consumers

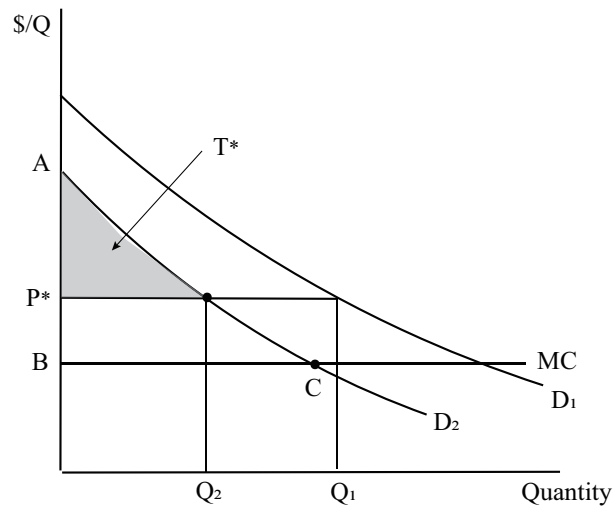


Figure 11.6 Two-Part Tariff with Two Consumers

In a market with two consumers whose demand curves are represented by D_1 and D_2 in Figure 11.6, the firm can maximize profit by *setting the usage fee P^* above the marginal cost and setting the entry fee T^* equal to the*

surplus of the consumer with the smaller demand. The resulting profit is $2T^* + (P^* - MC)(Q_1 + Q_2)$, which is larger than twice the area of triangle ABC in Figure 11.6.

Example 11.3 (Pricing Cellular Phone Service)

Data Usage	Monthly Price	Monthly Access Charge	Overage Fee
A. Verizon	A. Verizon	A. Verizon	A. Verizon
1 GB	\$30	\$ 20	\$ 15/GB
3GB	\$45	\$ 20	\$ 15/GB
6GB	\$60	\$ 20	\$ 15/GB
12GB	\$80	\$ 20	\$ 15/GB
18GB	\$100	\$ 20	\$ 15/GB
B. Sprint	B. Sprint	B. Sprint	B. Sprint
1GB	\$20	\$ 45	\$ none
3GB	\$30	\$ 45	\$ none
6GB	\$45	\$ 45	\$ none
12GB	\$60	\$ 45	\$ none
24GB	\$80	\$ 45	\$ none
C. AT&T	C. AT&T	C. AT&T	C. AT&T
2GB	\$30	\$ 25	\$ 15/GB
5GB	\$50	\$ 25	\$ 15/GB
15GB	\$100	\$ 15	\$ 15/GB
20GB	\$140	\$ 15	\$ 15/GB
25GB	\$175	\$ 15	\$ 15/GB
30GB	\$225	\$ 15	\$ 15/GB

Table 11.3: Cellular data plans (2016)

Cellular phone service providers often use a two-part tariff pricing strategy. This typically involves a monthly access fee, which includes a certain number of free minutes, and a per-minute charge for additional minutes used. Offering different plans allowed companies to combine third-degree price discrimination with the two-part tariff.

In recent years, many consumers use their phones for a variety of purposes beyond just making calls. As a result, cellular providers have begun offering different plans based on expected data usage. By combining price discrimination with a two-part tariff, cellular providers are able to increase

their profits while offering consumers more options.

11.6 Intertemporal Price Discrimination and Peak-Load Pricing

Intertemporal price discrimination is the practice of separating consumers with different demand functions into different groups by charging different prices at different points in time. This strategy allows firms to capture surplus from consumers who are willing to pay a higher price and to later reduce the price to appeal to the mass market.

Example 11.4 (How to Price a Best-selling Novel) Publishing both hardbound and paperback editions of a book allows publishers to price discriminate.

Some consumers want to buy a new bestseller as soon as it is released, even if the price is \$25. Other consumers, however, will wait a year until the book is available in paperback for \$10.

The key is to divide consumers into two groups, so that those who are willing to pay a high price do so and only those unwilling to pay a high price wait and buy the paperback.

It is clear, however, that those consumers willing to wait for the paperback edition have demands that are far more elastic than those of bibliophiles. It is not surprising, then, that paperback editions sell for so much less than hardbacks.

Peak-load pricing is the practice of charging higher prices during peak periods when capacity constraints cause marginal costs to be high. This strategy is more profitable for the firm than charging a single price at all times and is also more efficient because marginal cost is higher during peak periods.

11.7 Bundling

Bundling is the practice of selling two or more products as a package. By bundling, a firm can take advantage of customer heterogeneity and capture more value than by selling the products separately.

For example, a film company may sell two films as a package to two different theaters and that their reservation prices for the two films are as follows:

	Gone with the Wind	Getting Gertie's Garter
Theater A	\$12,000	\$3,000
Theater B	\$10,000	\$4,000

Table 11.4: Selling two films as a package

If the films are rented separately, the maximum price that could be charged for Wind is \$10,000 because charging more would exclude Theater B. Similarly, the maximum price that could be charged for Gertie is \$3000. The total revenue is \$26,000.

But suppose the films are bundled. Theater A values the pair of films at \$15,000 (\$12,000 + \$3000), and Theater B values the pair at \$14,000 (\$10,000 + \$4000). Therefore, the film company can charge each theater \$14,000 for the pair of films and earn a total revenue of \$28,000.

Why is bundling more profitable than selling the films separately? Because the relative valuations of the two films are reversed. The demands are negatively correlated-the customer willing to pay the most for Wind is willing to pay the least for Gertie.

Suppose demands were positively correlated-that is, Theater A would pay more for both films:

If we bundled the films, the maximum price that could be charged for the package is \$13,000, yielding a total revenue of \$26,000, the same as by renting the films separately.

Chapter 12

Monopolistic Competition and Oligopoly

Competition and monopoly are at opposite ends of the market spectrum. While competition is characterized by many firms, unrestricted entry, and homogeneous products, a monopoly is the sole producer of a product with no close substitutes. Falling between competition and monopoly are two other types of market structures: monopolistic competition and oligopoly, which describe the majority of remaining firms.

Monopolistic competition is closer to competition, as it has many firms and unrestricted entry or exit, like the competitive model, but its products are differentiated. Oligopoly, on the other hand, is more like a monopoly, as it is characterized by a small number of large firms producing either a homogeneous product like steel, or differentiated products like automobiles, and acting in relation to each other in their actions. In the following, we will examine some of these models, noting the similarities as well as the differences between these models.

12.1 Monopolistic Competition

The Characteristics of Monopolistic Competition

- Many firms.
- Firms compete by selling differentiated products that are highly substitutable for one another but not perfect substitutes; in other words, each firm's product is slightly different from other firms in the industry so that the cross-price elasticities of demand are large but not infinite. It has only limited market power.
- Free entry and exit: it is relatively easy for new firms to enter the market with their own brands and for existing firms to leave if their products become unprofitable.
- Firms engage in nonprice competition - advertising is important.

Examples: Soft drinks; Wine; Chinese restaurants in NYC.

12.1.1 Short-Run Equilibrium

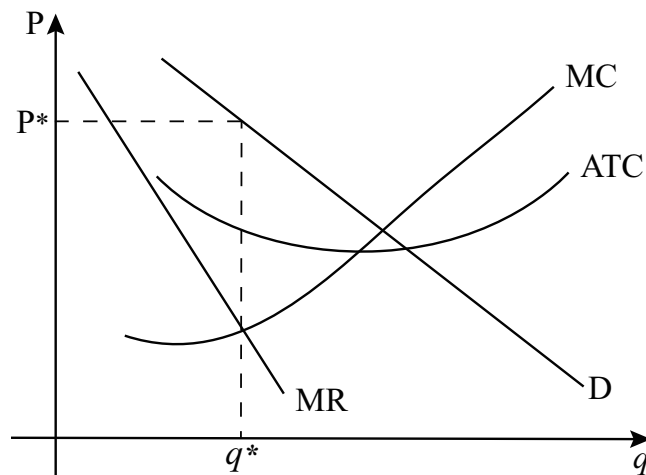


Figure 12.1 Short-run profit maximization under monopolistic competition

Similarly to a monopolist, a monopolistically competitive firm faces a downward-sloping demand curve since it is the only producer of its differentiated product. As a result, the firm has some market power and can set its price above its marginal cost to maximize profit, as shown in Figure 12.1. Therefore, the pricing and output decisions of a monopolistically competitive firm are made in the same way as those of a monopolist.

12.1.2 Long-Run Equilibrium

Recall that a monopolist can earn positive economic profits in the long run due to the barriers to entry. However, this does not hold for a monopolistically competitive firm as there are no such barriers.

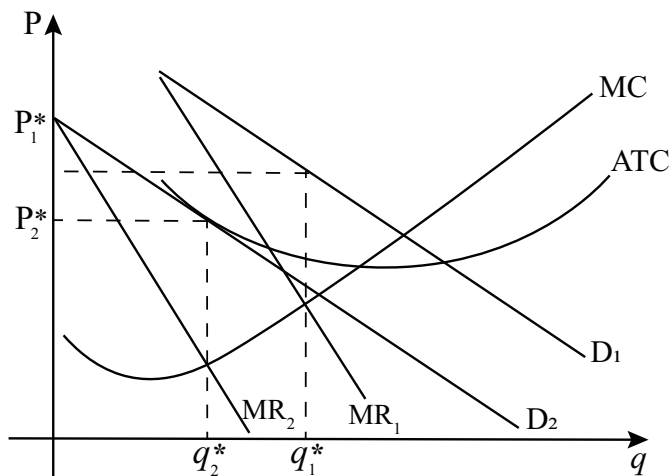


Figure 12.2 Entry eliminates profits under monopolistic competition

Entry Eliminates Profits:

In the long run, new firms will enter the industry since there are no restrictions on entry. As a result, the industry demand must be divided among more firms, leading to a decrease in the demand for each individual firm's output. This shift in demand leads to lower prices and lower profits for each firm, as depicted in Figure 12.2. The process continues until each firm earns only normal profits in the long-run equilibrium (p_2^*, q_2^*) ,

i.e., until $P = AC = D(q)$.

Exit Eliminates Losses:

Conversely, if some firms in the industry are making losses, they will exit the industry, reducing the supply and increasing the demand for each remaining firm's output. This shift in demand leads to higher prices and profits for each firm, as depicted in Figure 12.3. The process continues until each remaining firm earns only normal profits in the long-run equilibrium, i.e., until $P = AC = D(q)$.

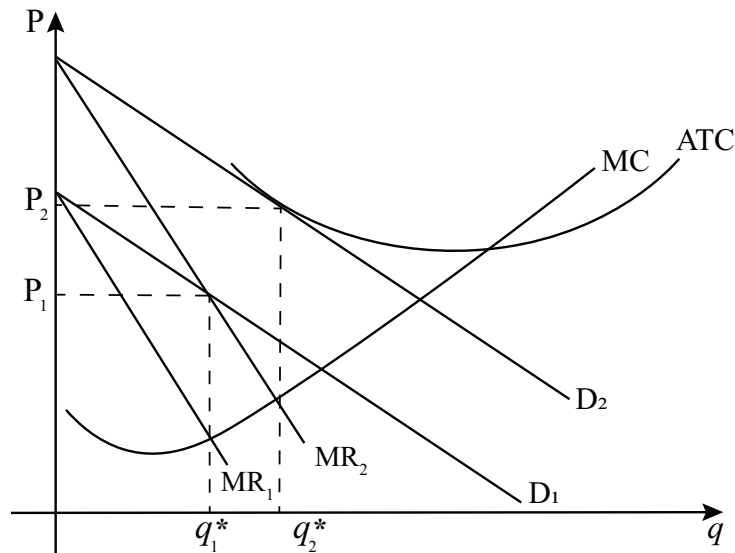


Figure 12.3 Exit eliminates losses under monopolistic competition

12.1.3 Monopolistic Competition and Economic Efficiency

Under perfect competition, price equals marginal cost. The demand curve facing the firm is horizontal, so **the zero-profit point occurs at the point of minimum average cost.**

However, under monopolistic competition, the demand curve is downward-sloping, so **the zero-profit point is to the left of the point of minimum average cost.** As a result, price exceeds marginal cost, leading to a dead-weight loss, which is similar to a monopoly.

Is monopolistic competition a socially undesirable market structure that should be regulated? The answer is probably no for two reasons:

1. In most monopolistically competitive markets, **monopoly power is small**. There are usually enough firms competing, with brands that are sufficiently substitutable, so that no single firm has significant monopoly power. Any resulting deadweight loss is likely to be small. Moreover, because firms' demand curves are relatively elastic, average cost will be close to the minimum.
2. Any inefficiency must be balanced against an important benefit from monopolistic competition: **product diversity**. Most consumers value the ability to choose among a wide variety of competing products and brands that differ in various ways. The gains from product diversity can be large and may easily outweigh the inefficiency costs resulting from downward-sloping demand curves.

Example 12.1 (Monopolistic Competition for Soft Drinks and Coffee) The markets for soft drinks and coffee illustrate the characteristics of monopolistic competition. Each market has a variety of brands that differ slightly but are close substitutes for one another.

Brand	Elasticity of Demand
Colas:	
RC Cola	-2.4
Coke	-5.2 to -5.7
Grand Coffee:	
Folgers	-6.4
Maxell house	-8.2
Chock Full o' Nuts	-3.6

Table 12.1: Elasticity of demand for Colas and Coffee

With the exception of RC Cola and Chock Full o' Nuts, all the colas and coffees are quite price elastic. With elasticities on the order of -4 to -8, each

brand has only limited monopoly power. This is typical of monopolistic competition.

12.2 Oligopoly

Oligopoly is an industry characterized by a few large firms producing most or all of the output of some product, and *reacting to each other in pricing and output decisions*.

Characteristics of Oligopoly:

- a) **Economies of scale:** It only takes a few firms of size q to supply the whole market. Scale economies may make it unprofitable for more than a few firms to coexist in the market; patents or access to a technology may exclude potential competitors; and the need to spend money for name recognition and market reputation may discourage entry by new firms. These are “natural” entry barriers — they are basic to the structure of the particular market. In addition, incumbent firms may take strategic actions to deter entry. Managing an oligopolistic firm is complicated because pricing, output, advertising, and investment decisions involve important strategic considerations, which can be highly complex.

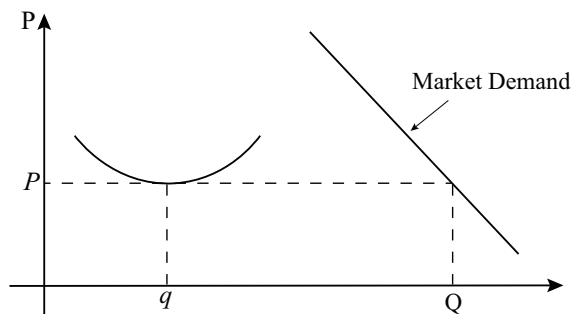


Figure 12.4 Downward-sloping demand curve under oligopoly

- b) **Mutual interdependence among firms** - since there are only a few firms in the market, each firm must react to the actions of other firms.
- c) **Nonprice competition and price rigidity.** Price war is a last resort due to the fear of lowering profits. Competition relies on advertising and product differentiation.
- d) **Temptation for firms to collude in setting prices.** Firms may want to maximize collective profits, but this is illegal in the U.S.
- e) **Incentive for firms to merge.** There is "perfect collusion" when the industry becomes a monopoly.
- f) **Substantial barriers to entry** - such as

(i) **economies of scale**

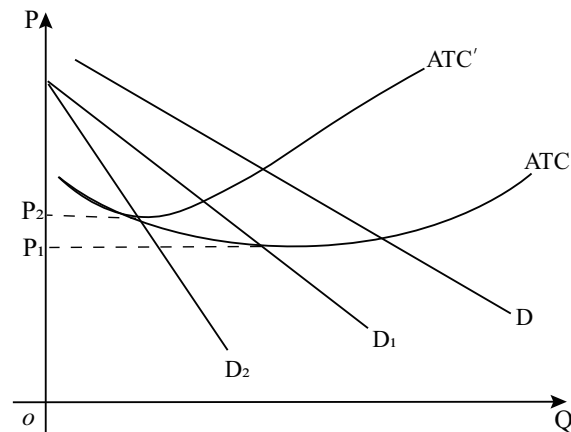


Figure 12.5 Individual demand and market demand under oligopoly

- D : demand faced by the first firm with no competitors.
- D_1 : demand faced by the first firm with one competitor.

- D_2 : demand faced by the competitor ($D = D_1 + D_2$).
- ATC : the same for both firms, with economies of scale.

Strategy for firm 1:

Charge a price below P_2 and above P_1 . The potential loss of firm 2 will prevent it from entering the market. **Note:** $ATC' \Rightarrow$ the 1st firm cannot use price to keep the 2nd firm out of the market.

(ii) **cost structure**

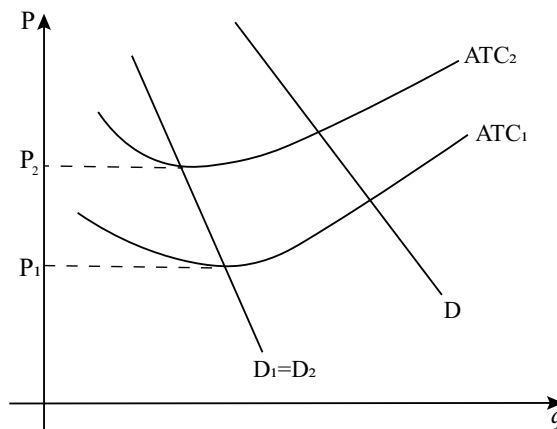


Figure 12.6 Oligopolistic firms with heterogeneous cost structures

Assume:

- firm 2 steals half of the market.
- costs for new firms are higher ($ATC_2 > ATC_1$).

Strategy for firm 1:

The first firm can keep the 2nd firm out by choosing a price between P_1 and P_2 . P_2 is referred

to as the limit price because any price greater than this will induce entry.

Therefore, in oligopolistic markets, the products may or may not be differentiated. What matters is that a few firms account for most or all of the total production. This results in some or all firms earning substantial profits over the long run due to barriers to entry that make it difficult or impossible for new firms to enter. Oligopoly is a prevalent market structure, and examples of oligopolistic industries include automobiles, steel, aluminum, petrochemicals, electrical equipment, and computers.

Understanding Strategic Interactions in Oligopolistic Markets

Oligopolistic markets are characterized by firms setting prices, output or other actions (such as advertising) based on strategic considerations regarding the behavior of their competitors. Game theory is a very useful tool for analyzing such behavior.

Game theory is a framework that analyzes strategic interactions among players who make decisions based on each other's actions and responses. It helps understand the interdependence among rival firms and the role of uncertainty in pricing and output decisions.

A game is described by the number of players, the set of strategies or actions, the payoffs of players, the form of the game (static or dynamic), and the information available to the players (complete or incomplete).

Payoff is the value associated with a possible outcome, and a **strategy** is a rule or plan of action for playing a game. An **optimal strategy** is one that maximizes a player's expected payoff.

To succeed in strategic interactions, it is essential to understand the opponent's perspective and deduce their likely responses to your actions.

The most commonly used solution concept in game theory is Nash equilibrium, introduced by Nobel Laureate John Nash, who inspired the movie "A Beautiful Mind."

Nash equilibrium is a profile of strategies or actions in which each firm does the best it can given its competitors' actions. At a Nash equilibrium, no firm has an incentive to deviate from its strategy.

As a result, at a Nash equilibrium, each firm will no longer adjust its own strategy given its rational expectation of the opponents' strategy profile. An important feature of Nash equilibrium is the consistency between belief and choice, meaning a choice based on a belief is optimal, and the belief supporting this choice is correct.

A much stronger solution concept is **dominant strategy equilibrium**, where each firm does the best regardless of its competitors' actions. That is, it is strategy-proof (no strategy will be played).

A **duopoly** is a market in which two firms compete with each other.

In the following discussion, we will examine models that deal with oligopolistic behavior and keep in mind how different assumptions about rival behavior can change the outcome.

12.3 Quantity Competition

12.3.1 Cournot Model

Cournot model is an oligopoly model introduced by the French economist Cournot in 1838, in which firms produce a homogeneous product, each firm treats the output of its competitors as fixed, and all firms decide simultaneously how much to produce.

The model is on quantity competition with homogeneous products, and shows how uncoordinated output decisions between rival firms could interact to produce an outcome that lies between the competitive and monopolistic equilibria.

Although the Cournot equilibrium is often considered a steady-state solution, it can also be viewed as a dynamic adjustment process that leads to the equilibrium of static quantity competition.

To see this, consider a scenario where there are two firms that produce identical products with zero marginal costs. Each firm believes that its rival is insensitive to its own output. The market demand curve is linear and is known to both sellers.

Initially, firm A views D_T as its demand curve and produces $Q_1 = \frac{T}{2}$ where MC equals MR_T . Firm B enters the market and assumes firm A will continue to produce $Q_1 = \frac{T}{2}$ units so it sees D_B as its demand curve and produces $Q_2 = \frac{T-Q_1}{2}$. Firm A then readjusts its output to $Q_3 = \frac{T-Q_2}{2}$. This adjustment process continues until an equilibrium is reached with *each producing* $1/3$ of T .

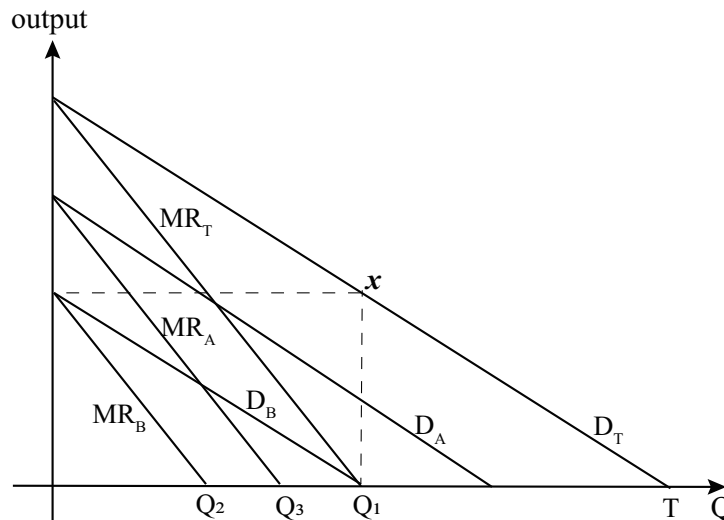


Figure 12.7 Market equilibrium under Cournot competition

Note that D_B is a residual demand curve, which is obtained by subtracting the amount sold by firm A at all prices from the market $Q_2 = \frac{T-Q_1}{2}$. Firm A will readjust its output and will view D_A as its new demand curve. D_A is also a residual demand curve and is obtained by subtracting firm B 's output from D_T .

Thus, in the Cournot model, uncoordinated rival behavior produces a determinate equilibrium that is greater than the monopoly output ($Q_1 = \frac{T}{2}$) and two-thirds of the competitive equilibrium output. The following

algebraic solution of the Cournot equilibrium also supports this conclusion.

Reaction Curves and Cournot Equilibrium

In the Cournot model, firms make output decisions based on their expectations about their competitors' output decisions. The relationship between a firm's profit-maximizing output and the amount it thinks its competitor will produce is called the **reaction curve**.

Firm 1's reaction curve shows how much it will produce as a function of how much it thinks Firm 2 will produce, and Firm 2's reaction curve shows its output as a function of how much it thinks Firm 1 will produce. Figure 12.8 shows the reaction curves for two firms in the Cournot model.

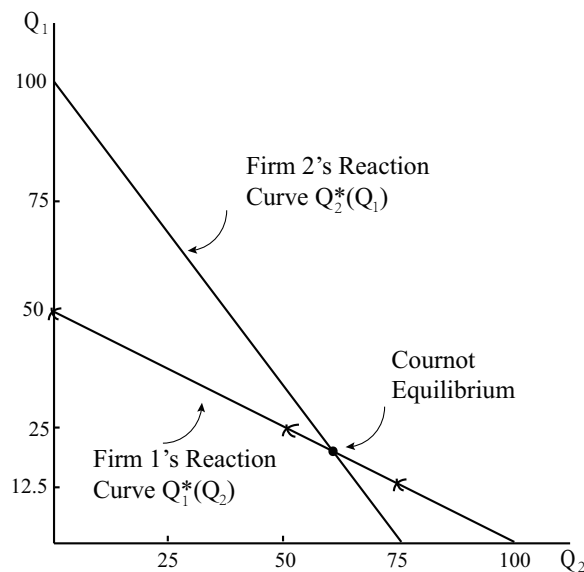


Figure 12.8 Reaction Curves and Cournot Equilibrium

In the **Cournot equilibrium**, each firm *correctly assumes* how much its competitor will produce and sets its own production level accordingly. Cournot equilibrium is an example of a Nash equilibrium, where no firm would individually want to change its behavior given what its competitors

are doing.

Algebraically, suppose that the market demand function is $P(q_1 + q_2)$. Firm 1 wishes to find q_1^* which maximizes profits by taking firm 2's level of output as fixed.

$$\max_{q_1} P(q_1 + \bar{q}_2)q_1 - c_1(q_1).$$

Similarly, firm 2's problem is to find q_2^* .

$$\max_{q_2} P(\bar{q}_1 + q_2)q_2 - c_2(q_2).$$

At equilibrium, the actions of two firms will be consistent when the choice each firm makes is compatible with the other firm's expectations. In other words, the choice based on a belief is rational (optimal), and the belief supporting this choice is correct, i.e., $\bar{q}_1 = q_1^*$ and $\bar{q}_2 = q_2^*$.

Example 12.2 (The Linear Demand Curve) Two identical firms face the following market demand curve:

$$P = 45 - Q,$$

where $Q = Q_1 + Q_2$. Also,

$$MC_1 = MC_2 = 3.$$

Total revenue for the two firms:

$$R_1 = PQ_1 = (45 - Q)Q_1 = 45Q_1 - Q_1^2 - Q_2Q_1,$$

and

$$R_2 = PQ_2 = (45 - Q)Q_2 = 45Q_2 - Q_1Q_2 - Q_2^2.$$

Then,

$$MR_1 = 45 - 2Q_1 - Q_2,$$

$$MR_2 = 45 - Q_1 - 2Q_2.$$

Setting $MR_1 = MC_1$ and solving for Q_1 , we obtain Firm 1's reaction curve:

$$Q_1 = 21 - \frac{1}{2}Q_2. \quad (12.1)$$

By the same calculation, we can get firm 2's reaction curve:

$$Q_2 = 21 - \frac{1}{2}Q_1. \quad (12.2)$$

Cournot equilibrium is:

$$Q_1 = Q_2 = 14.$$

Total quantity produce is

$$Q = Q_1 + Q_2 = 28.$$

If the two firms collude (like a monopolist), then the total profit-maximizing quantity is obtained as follows:

Total revenue for the two firms is given by:

$$R = PQ = (45 - Q)Q = 45Q - Q^2,$$

then

$$MR = \Delta R / \Delta Q = 45 - 2Q$$

Setting $MR = MC$, we find that total profit is maximized at $Q = 21$. Then, $Q_1 + Q_2 = 21$ is the collusion curve.

If the firms agree to share profits equally, each will produce half of the total output:

$$Q_1 = Q_2 = 10.5,$$

which is less than the output produced as an oligopolistic firm.

12.3.2 The Stackelberg Model—First Mover Advantage

Stackelberg model is an oligopoly model introduced by Stackelberg in 1934, in which one firm sets its output before other firms do.

There is an advantage to moving first. To see this, let us reconsider Example 12.2.

Example 12.3 (The Linear Demand Curve (continued)) Suppose Firm 1 sets its output first, and then Firm 2, after observing Firm 1's output, makes its output decision. In setting output, Firm 1 must, therefore, consider how Firm 2 will react.

$$P = 42 - Q$$

and

$$MC_1 = MC_2 = 3.$$

Firm 2's reaction curve:

$$Q_2 = 21 - \frac{1}{2}Q_1. \quad (12.3)$$

Firm 1's total revenue is then given by

$$\begin{aligned} R_1 &= PQ_1 = (45 - Q)Q_1 \\ &= 45Q_1 - Q_1^2 - Q_1Q_2, \\ &= 45Q_1 - Q_1^2 - Q_1\left(21 - \frac{1}{2}Q_1\right) \\ &= 24Q_1 - Q_1^2 - \frac{1}{2}Q_1 \end{aligned} \quad (12.4)$$

$$MR_1 = 24 - Q_1.$$

Setting $MR_1 = MC_1$ gives $Q_1 = 21$, and $Q_2 = 10.5$.

We conclude that Firm 1 produces twice as much as Firm 2 and makes twice as much profit. Going first gives Firm 1 an advantage.

12.4 Price Competition

12.4.1 Price Competition with Homogeneous Products—The Bertrand Model

The Bertrand Model is about price competition with homogeneous products.

Bertrand model is an oligopoly model proposed by the French economist Joseph Bertrand in 1883, in which firms produce a homogeneous good, each firm treats the price of its competitors as given, and all firms decide simultaneously what price to charge.

This model results in the same outcome as perfect competition even if there are just two firms.

Let's return to the duopoly example.

$$P = 30 - Q,$$

where $Q = Q_1 + Q_2$, and

$$MC_1 = MC_2 = 3.$$

At Cournot equilibrium, $Q_1 = Q_2 = 9$, and the market price is \$12, so that each firm makes a profit of \$81.

Now suppose that these two duopolists compete by simultaneously choosing a price instead of a quantity.

The only possible Nash equilibrium in the Bertrand model results in both firms setting price equal to marginal cost: $P_1 = P_2 = \$3$ because no firm can obtain higher profit by unilaterally changing its pricing strategy. The industry output is 27 units. So each firm produces 13.5 units, and both firms earn zero profit.

In the Cournot model, because each firm produces only 9 units, the market price is \$12. Now the market price is \$3. In the Cournot model,

each firm made a profit; in the Bertrand model, the firms price at marginal cost and make no profit.

12.4.2 Price Competition with Differentiated Products

Now suppose that each of two duopolists has fixed costs of \$20 but zero variable costs, and that they face the same demand curves:

$$Q_1 = 12 - 2P_1 + P_2,$$

$$Q_2 = 12 - 2P_2 + P_1.$$

Firm 1's profit is:

$$\begin{aligned}\Pi_1 &= P_1Q_1 - 20 = P_1(12 - 2P_1 + P_2) - 20 \\ &= 12P_1 - 2P_1^2 + P_1P_2 - 20.\end{aligned}$$

Similarly, we can figure out that firm 2's profit is given by

$$\Pi_2 = P_2Q_2 - 20 = 12P_2 - 2P_2^2 + P_1P_2 - 20.$$

The two firms's profit maximizing prices are

$$\Delta\Pi_1/\Delta P_1 = 12 - 4P_1 + P_2 = 0, \quad (12.5)$$

$$\Delta\Pi_2/\Delta P_2 = 12 - 4P_2 + P_1 = 0. \quad (12.6)$$

Solving the above two equations, we obtain the Nash equilibrium:

$$P_1 = P_2 = 4.$$

Firm 1's reaction curve:

$$P_1 = 3 + \frac{1}{4}P_2.$$

Firm 2's reaction curve:

$$P_2 = 3 + \frac{1}{4}P_1.$$

The intersection of these two curves gives the above Nash equilibrium.

12.5 Kinked Demand Curve Model

In oligopolistic industries, firms are aware that any price change they make will affect the sales of other firms in the industry. Therefore, the demand and marginal revenue (MR) curves of each firm must take into account the reactions of rivals.

The **kinked demand curve model** is an oligopoly model in which each firm faces a demand curve that is kinked at the currently prevailing price: at higher prices, demand is more elastic, whereas at lower prices, it is less elastic. To have a kinked demand curve, it is assumed that oligopolists expect that *rivals would match price cuts but not price hikes*.

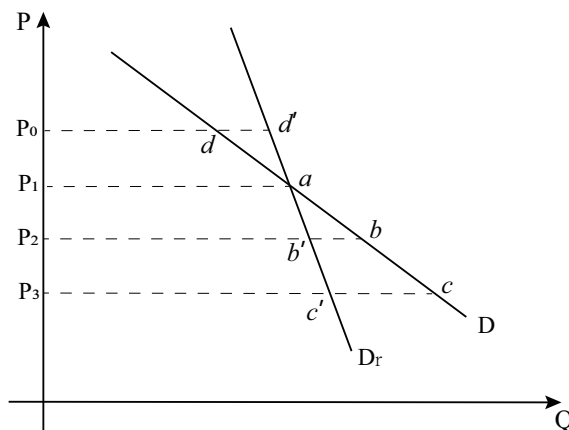


Figure 12.9 Demand curve which takes into account the reaction of rivals

Figure 12.9 shows the demand curve which takes into account the reaction of rivals, where D represents the firm's demand curve when rivals do not react to price changes and D_r represents the firm's demand curve when rivals match any price cut. Along D , as P decreases, Q increases

due to substitutability of this product for similar products in other industries and purchases by customers who switch away from other firms in this industry. Along D_r , as P decreases, Q increases, but not by as much as that along D because purchases by customers who switch away from other firms in this industry will no longer be true.

We arrive at a kinked demand curve, as shown in Figure 12.10, where at higher prices, demand is very elastic, whereas at lower prices, it is inelastic. To find MR in this model, we need to identify q_K , draw MR for D until q_K is reached, and extend D_r to the vertical axis and draw MR beginning at q_K .

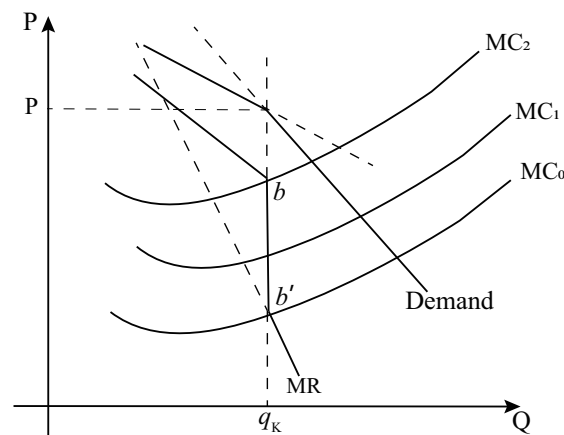


Figure 12.10 A kinked demand curve

In the vertical segment b to b' , the profit-maximizing rule $MR = MC$ yields the same (p, q) for any marginal cost ($MC_2 \geq MC_1 \geq MC_0$). This leads to **price rigidity**, a characteristic of oligopolistic markets by which firms are reluctant to change prices even if costs or demands change.

12.6 Prisoners' Dilemma: Competition vs Collusion

The prisoners' dilemma is a game-theoretical model that has implications for the behavior of oligopolists. It demonstrates how competitors could act to their mutual disadvantage. Suppose there are two firms in the same industry, A and B. If they collude and fix prices, they can share the market and earn high profits. But if one firm cheats and lowers its prices, it can capture a larger market share and earn even higher profits while the other firm loses market share and profits. If both firms cheat, they will end up in a price war, which will lower profits for both.

We can represent this situation in a payoff matrix, as shown in Table 12.3.

		Person B	
		confesses	doesn't confess
Person A	confesses	<u>5</u> , <u>5</u>)	(<u>1</u> , 10)
	doesn't confess	(10, <u>1</u>)	(2, 2)

Table 12.2: Prisoners' Dilemma for Two Suspects.

Note that "player" must individually choose a strategy (confess or not confess), but the outcome of that choice depends on what the other firm does.

In this setting, it is quite likely that both players will cheat and end up in the (**confess, confess**) strategy profile, which is a dominant strategy equilibrium. Confessing makes sense since each prisoner is attempting to make the best "of the worst" outcomes. However, both prisoners would be better off if they did confess.

It may be remarked that we can figure out an equilibrium for two-person games conveniently and quickly by using the following method. Consider the strategy of player 1, and for each strategy of player 2, find out the best responses of player 1. Draw a underline under its corresponding payoff. Similarly, find out the best responses of player 2 and underlines it.

The strategy profile with both underlines is (**confess, confess**), which is a unique Nash equilibrium. The corresponding equilibrium payoff profile is (5, 5).

The prisoners' dilemma highlights the tension between individual incentives and collective welfare. In oligopoly theory, the dilemma suggests that collusion is difficult to sustain, as each firm has an incentive to cheat and gain a larger market share. However, if all firms collude and maintain high prices, they can earn higher profits collectively. This tension between competition and collusion is a central issue in antitrust policy and regulation.

To see the relevance of the prisoners' dilemma to oligopoly theory, let us suppose that player A and player B are the firms in the same industry. The matrix in Table 12.3 identifies the payoffs about profits from an agreement to fix prices and share the market or from cheating on the collusive agreement. By the same reasoning as before, both are likely to cheat despite the fact that both will be worse off by cheating.

		player B	
		cheats	doesn't cheat
player A	cheats	(10, 10)	(20, 5)
	doesn't cheat	(5, 20)	(15, 15)

Table 12.3: Cooperation game of two oligopolistic firms. The cheating is a Nash equilibrium.

Example 12.4 (Price Competition (continued)) Consider the same example of duopoly: there are two firms, each of which has fixed costs of \$20 and zero variable costs. They face the same demand curves:

$$Q_1 = 12 - 2P_1 + P_2,$$

$$Q_2 = 12 - 2P_2 + P_1.$$

We found that in Nash equilibrium each firm will charge a price of \$4 and earn a profit of \$12, whereas if the firms collude, they will charge a price of \$6 and earn a profit of \$16, and whereas if Firm 1 keeps the colluding price \$6 and firm 2 cheats by setting price at \$4, their profits are

$$\Pi_1 = P_1Q_1 - 20 = (6)[12 - (2)(6) + 4] - 20 = \$4$$

$$\Pi_2 = P_2Q_2 - 20 = (4)[12 - (2)(4) + 6] - 20 = \$20,$$

respectively.

		Firm 2	
		charge \$4	charge \$6
Firm 1	charge \$4	(\$12, \$12)	(\$20, \$4)
	charge \$6	(\$4, \$20)	(\$16, \$16)

Table 12.4: **Payoff matrix:** Profits (or payoffs) to each firm given its decision and the decision of its competitor. The collusion is not a Nash equilibrium.

So if Firm 1 charges \$6 and Firm 2 charges only \$4, Firm 2's profit will increase to \$20. And it will do so at the expense of Firm 1's profit, which will fall to \$4.

Example 12.5 (Procter & Gamble in a Prisoner's Dilemma) The Procter & Gamble Company (P&G) is an American multinational consumer goods corporation headquartered in Cincinnati, Ohio, founded in 1837 by William Procter and James Gamble. In 2014, P&G recorded \$83.1 billion in sales. It was renamed it as Procter & Gamble Health Limited in May 2019 after completing the acquisition of the consumer health division of Merck Groupin.

Candle maker William Procter, born in England, and soap maker James Gamble, born in Ireland, both emigrated to the US from the United Kingdom. They settled in Cincinnati, Ohio, initially and met when they married sisters Olivia and Elizabeth Norris. Alexander Norris, their father-in-

law, persuaded them to become business partners, and in 1837 Procter & Gamble was created.

We argued that P&G should expect its competitors to charge a price of \$1.40 and should do the same. But P&G would be better off if it and its competitors all charged a price of \$1.50.

		Unilever and Kao	
		charge \$1.40	charge \$1.50
P& G	charge \$1.40	(<u>\$12</u> , <u>\$12</u>)	(<u>\$29</u> , \$11)
	charge \$1.50	(\$3, <u>\$21</u>)	(\$20, <u>\$20</u>)

Table 12.5: Payoff matrix for Pricing Problem.

Since these firms are in a prisoners' dilemma, it doesn't matter what Unilever and Kao do. P&G makes more money by charging \$1.40.

Advertising. Another way to illustrate the usefulness of the game-theoretical approach is to examine the interdependence of advertising decisions. Suppose that two firms are considering their advertising budgets. They have two strategies, a large budget or small budget. The payoff matrix is the profits they get under different strategies. The resulting equilibrium strategy profile is (**large budget, large budget**).

		B	
		Small Budget	Large budget
A	Small Budget	(10, 10)	(5, <u>18</u>)
	Large budget	(<u>18</u> , 5)	(8, <u>8</u>)

Table 12.6: Payoff matrix for advertising game.

Unfortunately, not every game has a dominant strategy for each player

		B	
		Small Budget	Large budget
A	Small Budget	(<u>10</u> , <u>8</u>)	(6, 5)
	Large budget	(4, 2)	(8, <u>6</u>)

Table 12.7: Modified advertising game.

Now Firm A has no dominant strategy since its optimal decision depends on what Firm B does. If Firm B chooses a small budget for advertising, Firm A does best by also choosing a small budget for advertising; but if Firm B chooses a large budget for advertising, Firm A does best by also choosing a large budget for advertising. Notice that although it does not have a dominant strategy equilibrium, it has two Nash equilibria: (**small budget, small budget**) and (**large budget, large budget**).

Furthermore, does the prisoners' dilemma doom oligopolistic firms to aggressive competition and low profits? Not necessarily. Although our imaginary prisoners have only one opportunity to confess, most firms set output and price over and over again, continually observing their competitors' behavior and adjusting their own accordingly. This allows firms to develop reputations from which trust can arise. As a result, oligopolistic coordination and cooperation can sometimes prevail.

12.7 Dominant Firm Price Leadership Model

Price leadership is a pricing strategy in which one firm regularly announces price changes that other (smaller) firms then match. This strategy is used to resolve the uncertainty of rivals' reactions to price changes. If one firm in the industry initiates a price change, and the rest of the firms traditionally follow the leader, there is no uncertainty about rival behavior.

In the **dominant firm price leadership model**, a dominant firm is a firm with a large share of total sales that sets the price to maximize its profit, taking into account the supply response of many smaller firms.

Price leadership by the dominant firm occurs when the dominant firm in the industry sets a price that maximizes its profit and allows its smaller rivals to sell as much as they want at the price so set.

In some industries, a large firm might naturally emerge as a leader, with the other firms deciding that they are best off just matching the leader's prices, rather than trying to undercut the leader or each other. For example, we may consider the OPEC (Organization Petroleum Exporting Countries) as a dominant firm, and non-OPEC ones as smaller firms.

Figure 12.11 shows the equilibrium price and quantity under price leadership. Suppose the industry demand curve is DD . Since the other smaller firms in the industry will follow any price change initiated by the dominant firm, they become price takers, and adjust output until price equals their marginal cost. The residual demand curve confronting the dominant firm is obtained by subtracting the quantity the other smaller firms will produce shown by S_D from the market demand, yielding P_1AD . The dominant firm produces q_D , where $MC_D = MR_D$, and charges P_3 . Smaller firms produce q_0 .

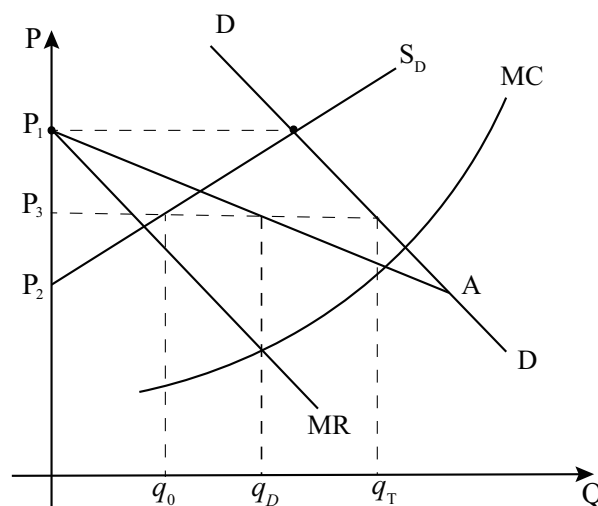


Figure 12.11 Equilibrium price and quantity under price leadership

12.8 Cartels and Collusion

Cartel: Producers explicitly agree to cooperate in setting prices and output levels.

In all models discussed so far, the firms were assumed to behave independently. Each firm makes a specific conjecture regarding how other firms will respond to its actions without any concern for how this affects the profits of the other firms. That is, there is no cooperation among firms.

The most important cooperative model of oligopoly is the cartel model. A **cartel** is an explicit agreement among independent producers to coordinate their decisions so that each of them will earn monopoly profits. If producers adhere to the cartel's agreements and market demand is sufficiently inelastic, the cartel may drive prices well above competitive levels.

Cartels are often international. While U.S. antitrust laws prohibit American companies from colluding, those of other countries are much weaker and are sometimes poorly enforced. Furthermore, nothing prevents countries, or companies owned or controlled by foreign governments, from forming cartels. For example, the OPEC cartel which was formed in 1960 is an international agreement among oil-producing countries which has succeeded in raising world oil prices above competitive levels.

12.8.1 Cartelization of a Competitive Industry

Let us examine how a group of firms can earn monopoly profits by coordinating their activities in a competitive market. Initially, we assume that the industry is in a long-run equilibrium. We will identify the short-run adjustments that the industry's firms can make with existing plants to reap monopoly profits for themselves. Figure 12.12 illustrates this possibility.

For instance, let us consider an industry consisting of 20 firms operating in a competitive market. In this scenario, the industry's output is Q , and the price is P . However, if the firms in the industry collude and form a cartel, they can restrict the output to Q_1 and charge the monopoly price

P_1 . Each firm produces q_1 and earns a profit at the price of P_1 .

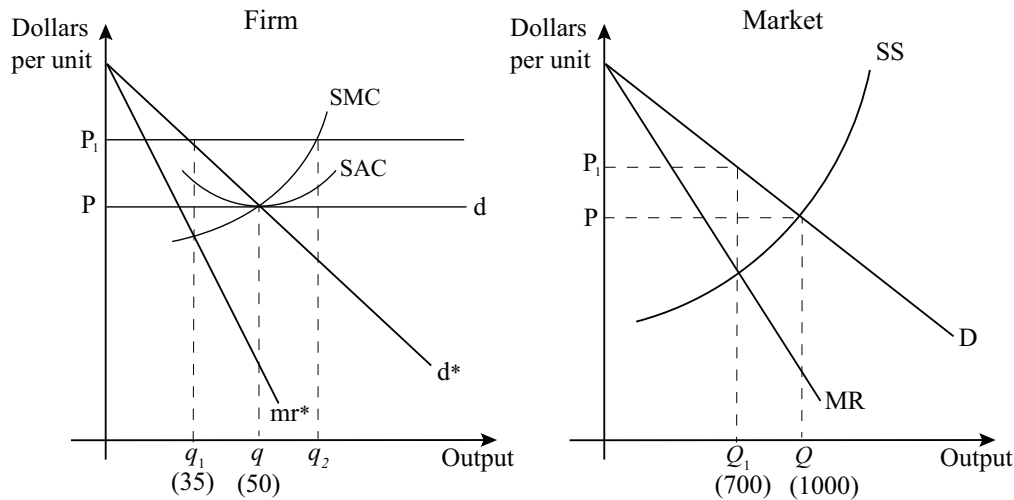


Figure 12.12 The emergence of cartels in a competitive market

The firms in the industry can always make more profits by colluding rather than by competing. While competitive firms acting independently are unable to raise the price by restricting output, they can increase the price by acting jointly to limit the amount supplied. We can analyze cartel pricing by using the dominant firm model, as shown in Figure 12.11.

There are two conditions for cartel success:

- First, a stable cartel organization must be formed whose members agree on price and output levels and then adhere to that agreement.
- The second condition, and perhaps the most important, is the potential for monopoly power. Even if a cartel can solve its organizational problems, there will be little room to raise the price if it faces a highly elastic demand curve.

Why Do Cartels Fail?

Despite the potential benefits of a successful cartel, they often fail due to several reasons, including:

Incentives to Cheat: Each firm in the cartel has a strong incentive to cheat on the cartel agreement, as shown in the prisoners' dilemma. If one firm increases its output and lowers its price, it can earn a higher profit. However, if many firms do this, industry output will increase significantly, and price will fall below the monopoly level. It is in each firm's interest to have other firms restrict their output while it increases its own output.

Disagreement Among Members: Members of the cartel may disagree over the appropriate cartel policy regarding prices, output, market shares, and profit sharing. This is especially true when cost, technology, and size of firms are different.

Potential Entry: The profits of the cartel members will encourage entry into the industry. If the cartel achieves economic profit by raising the price, new firms have an incentive to enter the market. If the cartel cannot block the entry of new firms, the price will be driven back down to the competitive level as production from the "outsiders" reaches the market.

Chapter 14

Employment and Pricing of Inputs

The emphasis now shifts from product markets to input (or factor) markets, which are markets where firms purchase the inputs they need to produce goods and services. We will explore the factors that determine the level of employment and the prices of inputs used in the production process. Firms are suppliers in product markets and demanders in input markets, while households and individuals are the demanders in product markets and suppliers in input markets.

In this chapter, we will discuss the basic principles common to all input-market analyses, regardless of whether the input refers to labor, capital, or raw materials.

14.1 The Input Demand of a Competitive Firm

14.1.1 One Variable Input

We begin by introducing two important concepts:

- **Derived input demand** is the demand for an input that depends on both the firm's level of output and the cost of inputs, *derived from*

profit maximization.

- **Marginal revenue product (MRP)** of an input is the additional value resulting from the sale of output created by the use of one additional unit of an input.

Suppose that only one input (labor) is allowed to vary, while the others are fixed. In this short-run setting, labor is the only variable input. By the law of diminishing marginal returns, the marginal product of labor (MP_L) curve slopes downward beyond some point.

The **marginal revenue product of labor** (MRP_L) is defined as:

$$MRP_L = MR \times MP_L, \quad (14.1)$$

where MR is the marginal revenue earned by the firm for each additional unit of output sold, whether or not the output market is competitive.

However, in a competitive output market, $MR = P$, and then MRP_L reduces to the **marginal value product of labor** (MVP_L):

$$MVP_L = P \times MP_L, \quad (14.2)$$

which is downward sloping because the marginal product of labor falls as the hours of work increase.

The profit-maximizing level of labor is that firm will hire workers up to the point where the marginal value product of labor is equal to its wage rate, i.e.,

$$w = MVP_L,$$

which gives us the **input demand curve for labor** of a competitive firm.

Suppose that the daily wage rate is \$30 dollars per worker. Then, the profit-maximizing labor input units are $L^* = 20$. Therefore, factor markets are similar to output markets in many ways.

Figure 14.1 shows the input demand curve with only labor input variable, given by $MVP_L = MP_L \times P_x$.

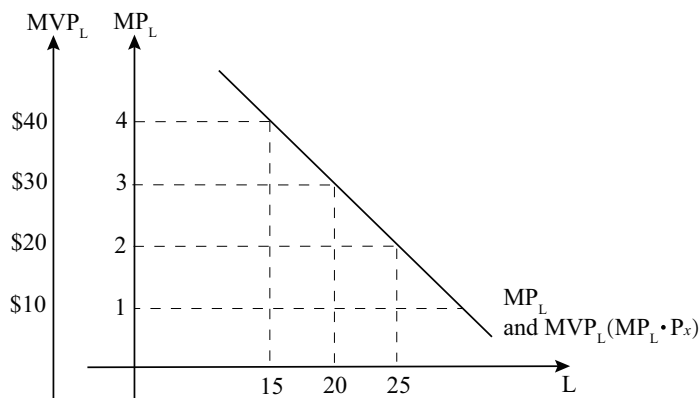


Figure 14.1 The input demand curve with only labor input variable, which is given by $MVP_L = MP_L \times P_x$ with $P_x = \$10$ for product x .

The profit-maximizing condition in the factor market, $w = MVP_L$, is actually equivalent to the condition for profit maximization in terms of output, which is $MC = P$. To see why, we can use the fact that $MC = w/MP_L$ and substitute it into $MC = P$. This gives us:

$$\frac{w}{MP_L} = P,$$

which can be rearranged to get:

$$w = P \times MP_L = MVP_L.$$

Therefore, the two conditions are equivalent.

14.1.2 Firm's Input Demand: All Inputs Variable

In general, a change in an input price will lead the firm to alter the demand for other inputs. What is the input demand curve when all inputs are variable?

Suppose that at initial equilibrium, the hourly wage rate is \$30 and $L = 20$. The firm is operating at point A on MVP_L where $K = 10$. Now, suppose the wage rate decreases to \$20. If K remains constant ($K = 10$),

the firm will increase the employment of labor to $L = 25$. If capital increases to $K = 12$ (as more workers require more tools), the entire MVP_L curve shifts upward. This adjustment leads to a further increase in labor to point C . Connecting points A and C , we get the firm's input demand curve, shown in Figure 14.2.

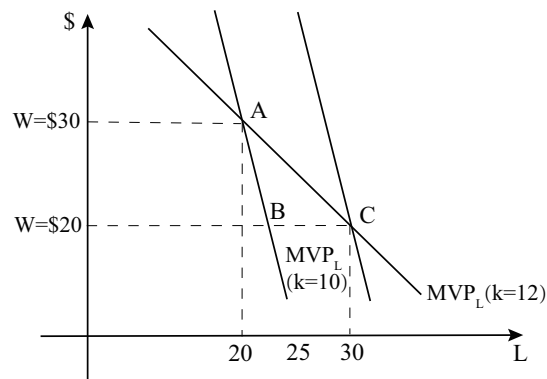


Figure 14.2 The input demand curve with all inputs variable.

14.2 Input Demand in a Competitive Industry

In a competitive industry, the total quantity of an input hired by all firms is the sum of the quantities employed by each firm. To obtain the industry input demand curve, we must aggregate the input demand of all firms.

However, when deriving a firm's input demand curve, we assume a constant product price. This assumption does not hold for an industry because when all firms increase their output simultaneously, they sell more output only at a lower price. Therefore, we must consider the effect of changes in output price on the input demand of the industry, as illustrated in Figure 14.3.

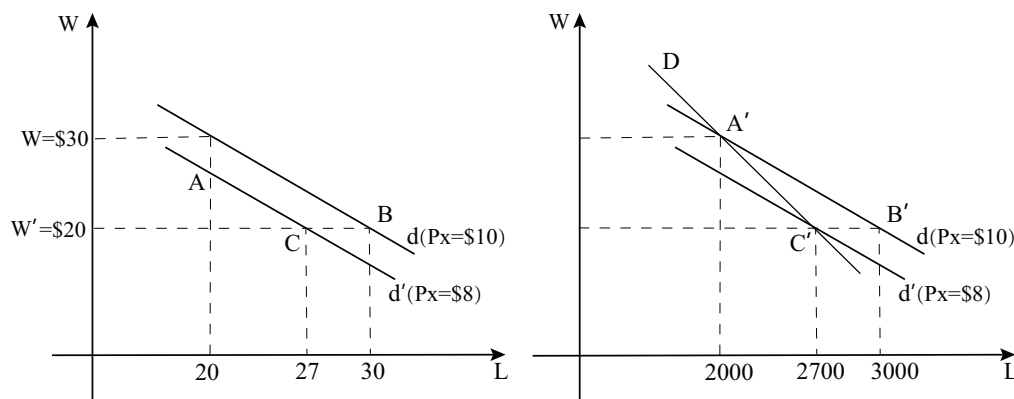


Figure 14.3 The industry demand curve in a competitive industry

14.3 The Input Demand of Monopoly

A monopoly is a firm that is the sole seller of a product. However, having monopoly power in the output market does not necessarily mean having market power in the input markets.

Like a competitive firm, a monopoly aims to maximize profits by using inputs until the marginal cost equals the marginal revenue. This results in the profit-maximizing level of output q , which can be expressed as the following equation:

$$MC = MR_q$$

Since $MC = \frac{w}{MP_L}$, we can rewrite the equation as:

$$w = MP_L \times MR_q \equiv MRP_L.$$

This equation is known as the **monopolist's input demand curve**, where MRP_L is the marginal revenue product of labor.

Notice that the *monopolist's input demand curve* lies below the *marginal value product of labor (MVP_L) curve*, which is the demand curve for a perfectly competitive firm. This is because the marginal revenue of a monopoly is lower than the price of output q at each level of output and employment

of labor, i.e., $MR_q < P$.

Figure 14.4 illustrates the relationship between MRP_L and MVP_L curves under monopoly.

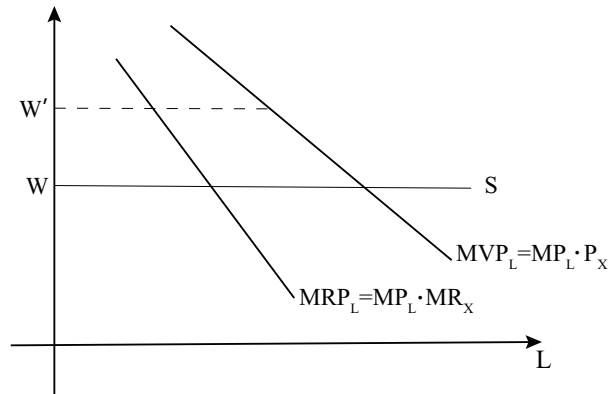


Figure 14.4 The relationship between MRP and MVP curves under monopoly

It is also important to note that a monopoly tends to employ less labor, or any other input, than a perfectly competitive industry. This is because a monopoly produces less output than a competitive industry, resulting in a lower demand for inputs.

14.4 The Supply of Inputs

The supply side of input markets deals with the quantities of inputs available at alternative prices.

Average expenditure curve (AV) is the *supply curve* representing the price per unit that a firm pays for a good.

Marginal expenditure curve (ME) is the curve describing the additional cost of purchasing one additional unit of a good.

Profit maximization requires that marginal revenue product be equal

to marginal expenditure of an input:

$$MRP = ME. \quad (14.3)$$

In the competitive input market, since the price of the input equals marginal expenditure ($ME = w$), (14.3) reduces to

$$MRP = w. \quad (14.4)$$

The supply curve of inputs to **all industries** in the economy is almost vertical. For example, the total amount of labor can increase only if workers decide to work longer hours or if more people enter the labor force. Such responses to a higher wage rate may be so small that the supply curve appears almost vertical.

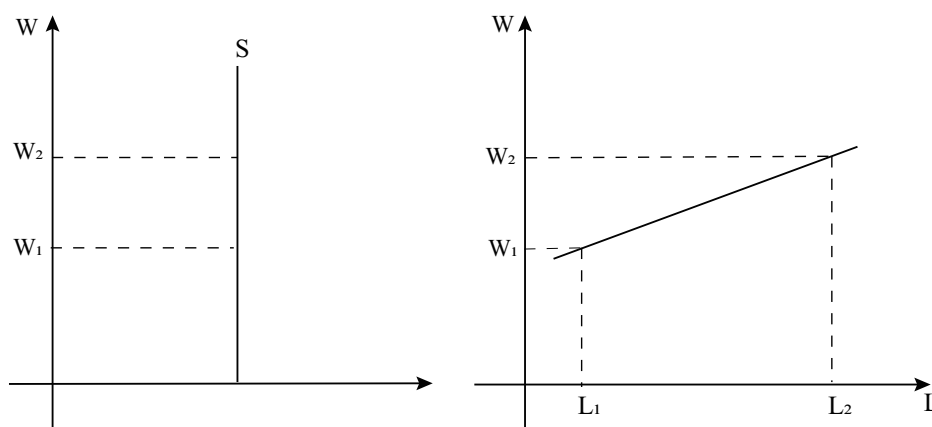


Figure 14.5 The diagram on the left is the supply curve for all industries, and the diagram on the right is the supply of an industry for labor input.

However, the supply curve confronting any particular industry may not be vertical. The amount employed in a particular industry is subject to great variation. For example, if the wage rate paid to workers in the shoe industry should increase, workers in other industries would leave their jobs to go to work making shoes. As a result, the supply curve for labor

in the shoe industry, which is only a small part of the entire labor market, will be more elastic than the supply curve of labor for the entire economy. In fact, the supply curves of most inputs to most industries are likely to be either perfectly horizontal or slightly upward-sloping, as shown in Figure 14.5.

14.5 Labor Supply

Since consumers are suppliers of labor, we can use consumer theory to derive the labor supply curve.

14.5.1 The Income-Leisure Choice of a Worker

In our previous discussion of a consumer's choice, the consumer's income was assumed to be fixed. However, most people's income is not fixed but depends instead on, among other things, the decision about how much time the person will work. To investigate, we assume that labor income is the only source of a worker's income, and the wage rate is fixed. Let:

- I = the weekly income;
- L = the weekly leisure time;
- H = the weekly working hours;
- w = the wage rate per hour.

Then, the income the worker earns is $I = wH$. Since a week has $24 \times 7 = 168$ hours and $H + L = 168$, we have $I = w(168 - L)$, and thus,

$$I + wL = 168w,$$

which is the worker's budget constraint. The worker's problem is to choose a combination of (I, L) such that they have the highest utility.

Suppose the worker's indifference curves are strictly convex over (I, L) . We can find the optimal bundle by either graphical or mathematical approach. As usual, the equilibrium is the point of tangency between the budget line and an indifference curve.

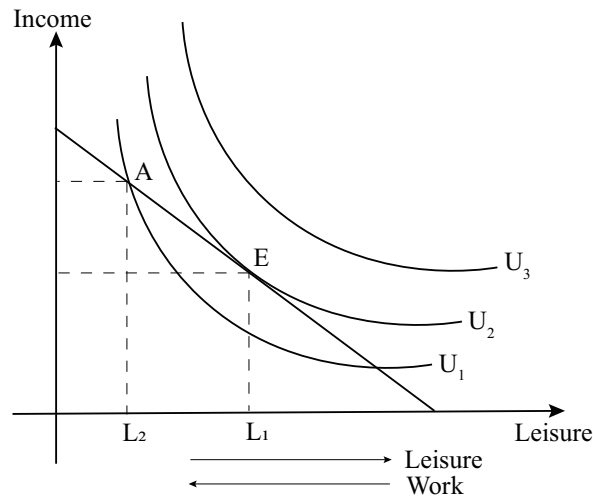


Figure 14.6 The income-leisure choice of a worker.

14.5.2 The Supply of Working Hours

The previous analysis assumed a fixed wage rate. However, what happens when the wage rate changes? Will workers work longer hours at a higher wage rate? The answer depends on the consumer's preferences.

The Substitution Effect Dominating the Income Effect Leads to More Working Hours

Suppose the initial wage rate is $w_0 = \$10$, and the optimal bundle is E . If the wage rate increases to $w_1 = \$15$, the new optimal bundle is E' . The substitution effect $= L_3 - L_1 < 0$. A higher wage rate's substitution effect is to encourage a worker to have less leisure time or supply more hours of labor. The income effect $= L_2 - L_3 > 0$, meaning the higher wage rate encourages the consumer to have more leisure time or supply fewer

hours of labor, as both leisure and income are normal goods. The total effect of the higher wage rate is the sum of the income and substitution effects. Although these effects operate in opposite directions, in this case, the substitution effect is large, so the total effect is an increase in working hours from NL_1 to NL_2 .

Figure 14.8 shows a graphical representation of the consumer choice when the substitution effect dominates the income effect.

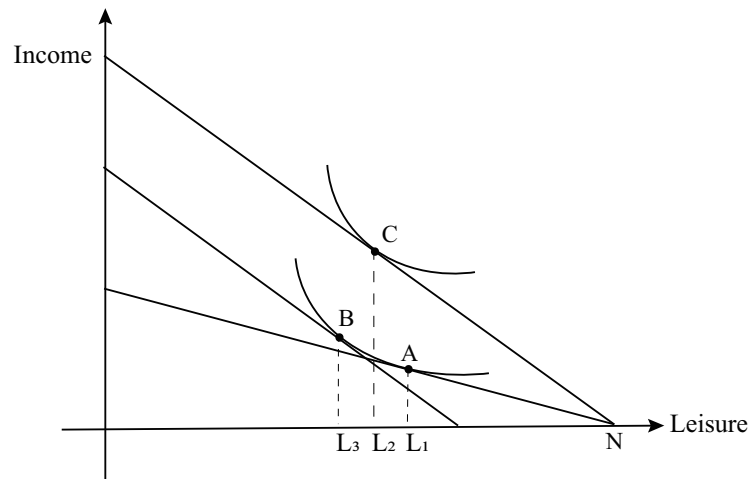


Figure 14.7 Consumer choice when substitution effect dominates income effect

The Dominance of Income Effect Leads to Less Working Hours

When the income effect dominates over the substitution effect, the conclusion is different from the above. In this case, the higher wage rate leads to a decrease in the hours worked. For instance, if the wage rate further increases to $w = 20$, the total effect $= (L^2 - L^3) + (L^3 - L^1) = L^2 - L^1 > 0$, indicating that the consumer will increase leisure time and decrease working hours.

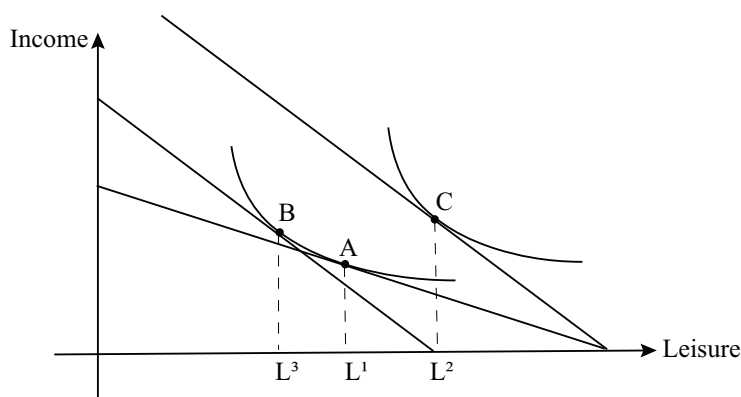


Figure 14.8 Consumer choice when income effect dominates substitution effect

Figure 14.8 shows a graphical representation of the consumer choice when income effect dominates substitution effect.

14.5.3 Backward-bending Labor Supply Curve

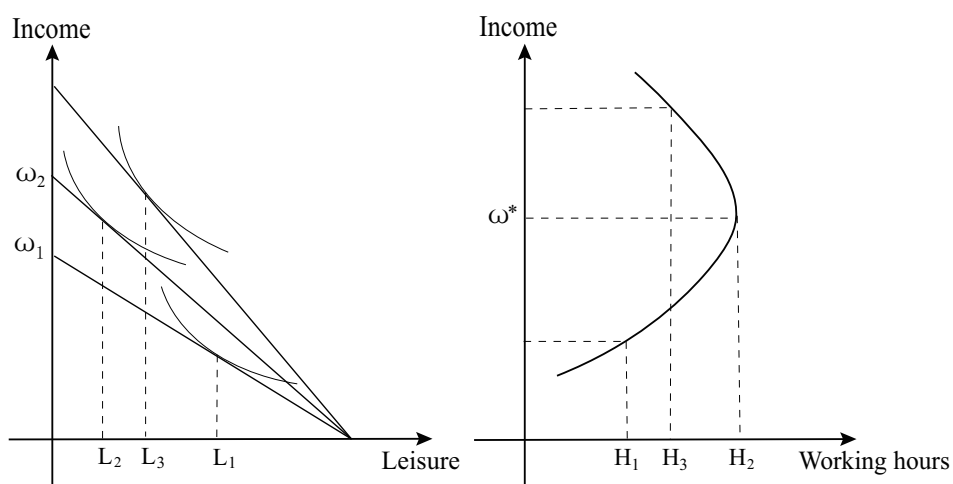


Figure 14.9 The emergence of a backward-bending labor supply curve

Drawing on the preceding discussion, we can conclude that the labor supply curve exhibits different slopes depending on the dominance of substi-

tution and income effects. At low wage rates, the curve slopes upward due to the dominance of the substitution effect over the income effect, which motivates individuals to supply more work hours. However, at higher wage rates beyond a certain threshold represented by w^* , the labor supply curve slopes downward because the income effect dominates the substitution effect. This encourages individuals to choose leisure time over work, resulting in a decrease in the number of work hours supplied. These opposing effects produce a backward-bending labor supply curve, as illustrated in Figure 14.9.

The labor supply curve can also be a vertical line.

Example 14.1 Suppose that $U = L^\alpha I^\beta$, where $\alpha > 0$, $\beta > 0$, and $\alpha + \beta = 1$. The consumer's choice of I and L can be determined by $MRS_{LI} = \frac{w}{1}$, which yields $\frac{\alpha I}{\beta L} = w$. Therefore, $I = \beta w L / \alpha$. Substituting $I = \beta w L / \alpha$ into the budget constraint $I + wL = 168w$, we obtain $(\frac{\beta}{\alpha} + 1)wL = 168w$, and thus $L^* = 168\alpha$. The consumer works 24α hours a day, which is independent of the wage rate w .

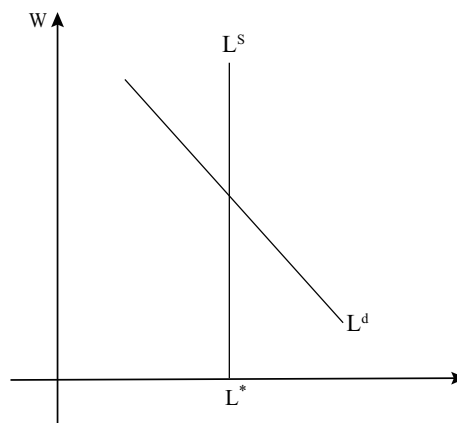


Figure 14.10 A vertical labor supply curve

The Market Labor Supply Curve

To obtain the market labor supply curve, we horizontally add the individual supply curves of all workers competing in a given labor market. This

curve can slope upward, bend backward, or be a vertical line.

14.5.4 The General Level of Wage Rate

To analyze the level of wage rate, we use the principles of supply and demand. The supply curve of labor for this problem represents the total quantity of labor that will be supplied by all individuals at various wage levels. The appropriate supply curve is the aggregate supply curve of hours of work discussed earlier.

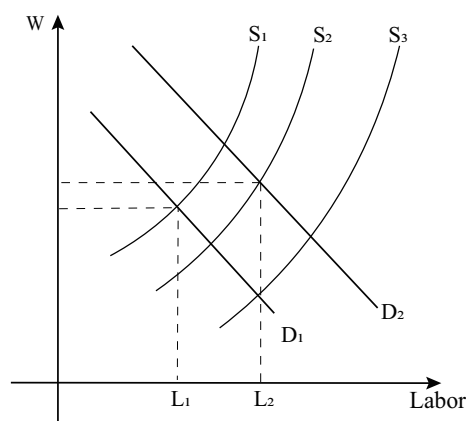


Figure 14.11 The demand and supply analysis of equilibrium wage rate

The aggregate demand curve for labor represents the marginal productivity of labor to the economy as a whole. The intersection of the aggregate demand and supply curves determines the general level of wage rates. If demand increases faster than supply, wage rates tend to rise over time.

The productivity of labor is a primary factor that influences the level of wages. This explains why real wage rates are typically higher in developed countries than in less developed ones. Marginal productivity is higher due to factors that determine the position of the demand curve, such as capital, technology, and skill.

14.5.5 Why Wages Differ?

Under the assumptions of identical workers and job evaluations based solely on monetary wage rates, there is a tendency for wage rates among firms or industries to equalize. However, dropping these assumptions leads to the conclusion that wage rates can differ among jobs and people employed in the same line of work. Why is the wage rate for engineers higher than the wage rate for clerks? These differences are in full equilibrium with no tendency for the wage rates to equalize.

Factors leading to equilibrium wage differences:

- **Equalizing wage differentials:** Workers currently employed in less desirable jobs may prefer their current jobs despite lower pay. Monetary considerations are not always the only, or most important, factors that influence job selection. The wage differential that arises due to job preference is known as the **equalizing wage differential**, as the less attractive jobs must pay more to equalize the real advantages of employment among different jobs.

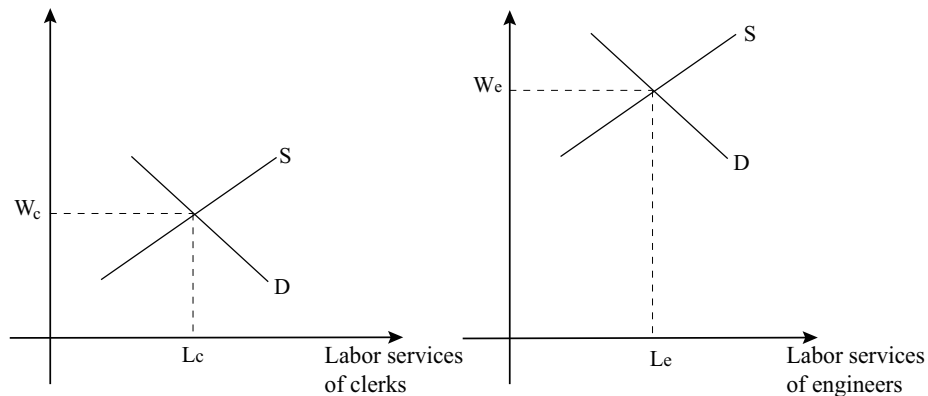


Figure 14.12 Wage rate gap between engineers and clerks

- **Differences in human capital investment:** Acquiring the skills to become an engineer may involve significant costs. The wage for en-

gineers may not be high enough to compensate clerks for the training costs they would have to bear to become engineers.

- **Differences in ability:** Even if there were no training costs, clerks may not have the necessary aptitude for science and mathematics required to work as engineers.

14.6 Industry Determination of Price and Employment of Inputs

14.6.1 The market equilibrium for labor input

As usual, the market equilibrium of an input for a particular industry will be established when the quantity demanded equals the quantity supplied. Graphically, the equilibrium is shown by the intersection of the industry demand and supply curves. The position of a firm in equilibrium can be similarly determined.

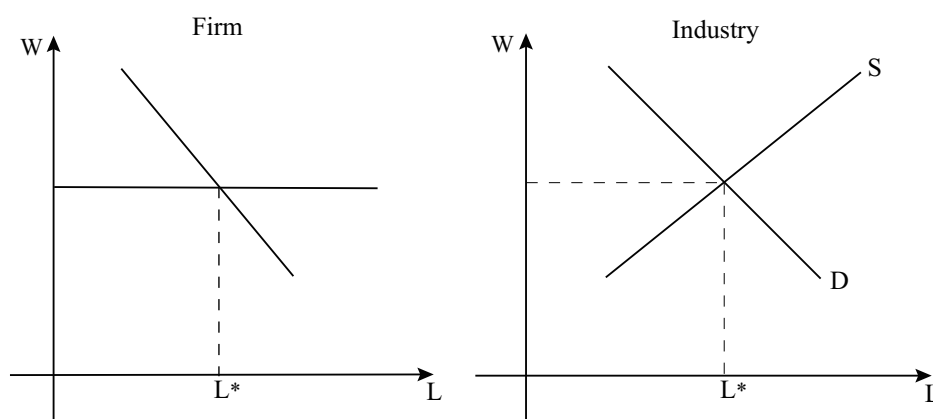


Figure 14.13 The market equilibrium for labor input

Note that each firm is in the position of employing the quantity of the input at which the marginal value product equals the price.

Process of Input Price Equalization across Industries

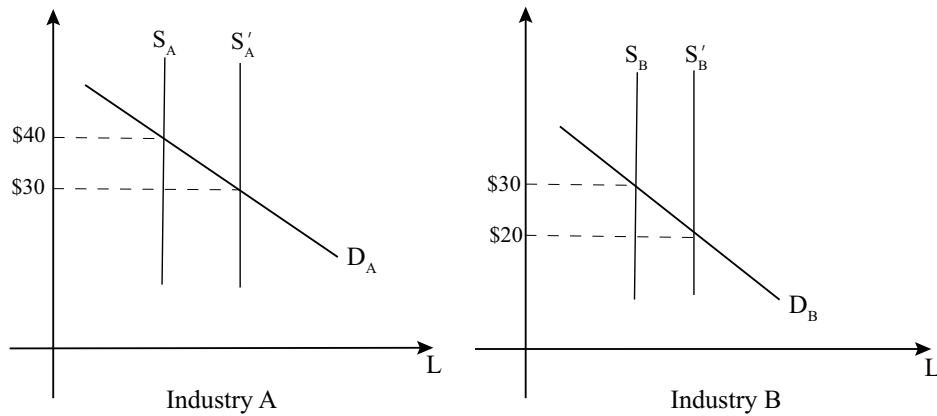


Figure 14.14 Wage rate equalization across two industries

When several industries employ the same input, the input tends to be allocated among industries so that its price is the same in every industry. If this were not true—if workers were receiving \$40 in industry A and \$30 in industry B—input owner would have incentive to shift inputs to industries where pay is higher, and this process tends to equalize input prices.

14.6.2 Economic Rent

Rent refers to payments made to lease the services of land, apartments, equipment, or other durable assets.

Economic Rent is the difference between the payments made to a factor of production and the minimum amount that must be spent to obtain the use of that factor.

In other words, economic rent is the portion of the payment to the supplier of an input that is in excess of the minimum amount necessary to retain the input in its present use.

Economic Rent with an Upward-sloping Supply Curve

In cases where the supply curve of an input, such as the supply of college professors, slopes upward, part of the payment to input owners represents economic rent. Individuals A , B , C , and D receive rents equal to areas A_2 , B_2 , C_2 , and D_2 , respectively, as illustrated in Figure 14.15.

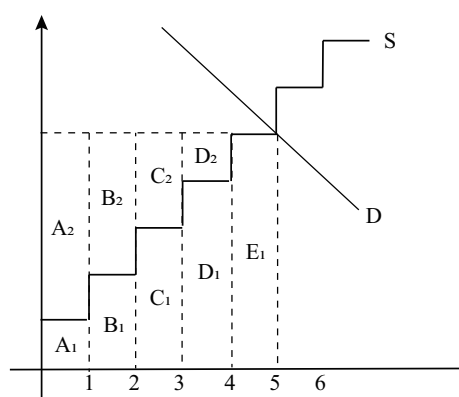


Figure 14.15 Economic rent with an upward-sloping supply curve

The fraction of total payments that represents economic rent increases as the supply curve becomes more inelastic. Economic rents represent the net benefits received by input owners from their current employment, and they measure the gains from voluntary exchange.

There are two limiting cases to consider:

Economic Rent with a Vertical Supply Curve

When the supply curve of an input is vertical, it is infinitely inelastic. In this case, *the entire remuneration of the input represents economic rent* because the same quantity would be available even at a zero price. The vertical curve intersects with the demand curve for the input's services to determine its price. The price and quantity are specified to indicate that we are not concerned with the sale price of the input but with the price for the services yielded by the use of the input.

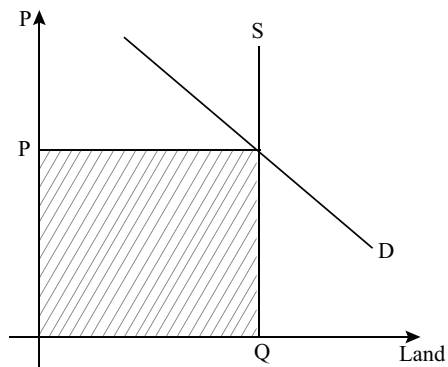


Figure 14.16 Economic rent under a vertical supply curve of land

Figure 14.16 illustrates economic rent under a vertical supply curve of land.

Economic Rent with a Horizontal Supply Curve

When the supply curve of an input is horizontal, it is infinitely elastic. In this case, *the economic rent earned by a factor of production will always be zero.*

14.7 Factor Markets with Monopsony Power

In some factor markets, buyers have **monopsony power**, which allows them to affect the prices they pay for inputs. This often happens when a single firm is the only purchaser of a particular input, or when there are only a few buyers, each of whom has some monopsony power. The **pure monopsony** here means a single firm that is the sole purchaser of some type of input.

Firms with monopsony power can negotiate lower prices for inputs than smaller purchasers. They frequently face the upward-sloping market supply curve for inputs, which means that the marginal cost of hiring another worker (ME) is not equal to the wage rate the firm must pay to all workers ($ME > w$), and so ME lies above S .

The profit-maximizing level of employment of a monopsony is then given by

$$MVP_L = ME > w$$

if the firm is a competitor in its output market, and

$$MRP_L = ME > w$$

if the firm is a monopoly in its output market.

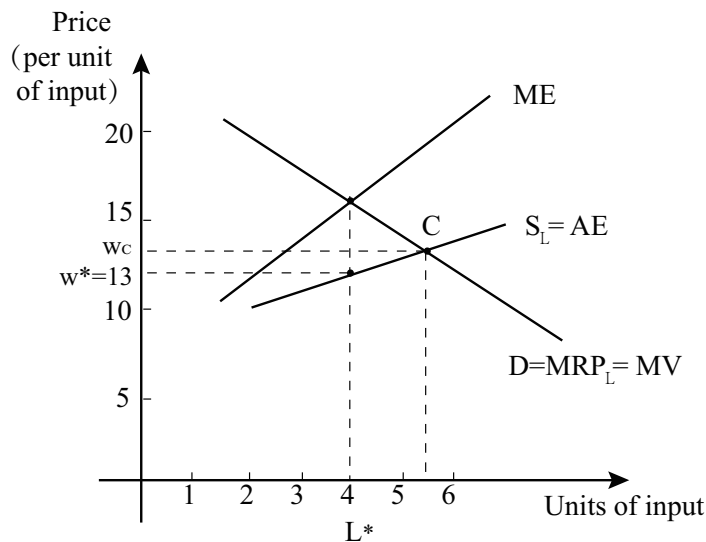


Figure 14.17 Marginal and average expenditure

Thus, compared to competitive input markets, monopsony markets result in lower employment and lower wage rates. A similarity between monopsony and monopoly is apparently true from this conclusion: *a monopoly restricts output to set a higher price, while a monopsony restricts output to pay a lower wage rate.* A monopoly is able to charge a higher price because it faces a downward-sloping demand curve, whereas a monopsony is able to pay a lower wage rate because it faces an upward-sloping supply curve.

When the buyer of an input has monopsony power, the marginal ex-

penditure curve lies above the average expenditure curve, as shown in Figure 14.17. The number of units of input purchased is given by L^* at the intersection of the marginal revenue product and marginal expenditure curves, and the corresponding wage rate w^* is lower than the competitive wage w_c due to the monopsony power of the buyer.

14.8 Conclusion

In conclusion, this chapter presents the profit-maximizing level of employment and wage rate in different types of input markets with product markets. Figure 14.18 illustrates the diagram depicting the main results, which can be summarized as follows:

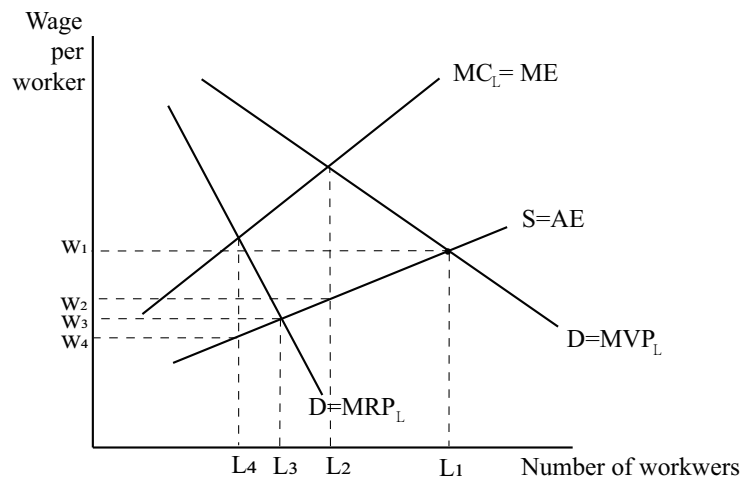


Figure 14.18 The profit-maximizing level of employment in various types of markets

1. In perfectly competitive markets for both labor and product, the profit-maximizing level of labor occurs where the marginal value product of labor equals the wage rate, i.e., $MVP_L = w$. The number of units of input purchased is given by L_1 , and the corresponding wage rate is w_1 .

2. When the market for labor has monopsony power and the market for product is perfectly competitive, the profit-maximizing level of labor occurs where $MVP_L = ME > w$. The number of units of input purchased is L_2 , which is lower than L_1 , and the corresponding wage rate w_2 is lower than the competitive wage w_1 .
3. When the market for labor is perfectly competitive and the market for product has monopoly power, the profit-maximizing level of labor occurs where $MRP_L = w$. The number of units of input purchased is L_3 , which is lower than L_1 , and the corresponding wage rate w_3 is lower than the competitive wage w_1 .
4. When the market for labor has monopsony power and the market for product has monopoly power, the profit-maximizing level of labor occurs where $MVP_L = ME > w$. The number of units of input purchased is L_4 , which is lower than L_2 , and the corresponding wage rate w_2 is lower than the competitive wage w_3 .

Thank you for completing this course!