## Math 166 - Week in Review #5

## Sections A.1 and A.2 - Propositions, Connectives, and Truth Tables

- A proposition, or statement, is a declarative sentence that can be classified as either true or false, but not both.
- . Prime propositions, or simple propositions, are simple statements expressing a single complete thought.
- We use the lowercase letters p, q, r, etc. to denote prime propositions.
- Propositions that are combinations of two or more prime propositions are called compound propositions. The words used to combine propositions are called logical connectives.
- A <u>conjunction</u> is a statement of the form "p and q" and is represented symbolically by p ∧ q.
   The conjunction p ∧ q is true if both p and q are true; it is false otherwise.
- A <u>disjunction</u> is a statement of the form "p or q" and is represented symbolically by p ∨ q.
   The disjunction p ∨ q is **false** if both p and q are false; it is true in all other cases.
- An <u>exclusive</u> disjunction is a statement of the form "p or q" and is represented symbolically by p \( \times q \).
   The disjunction p \( \times q \) is false if both p and q are false AND it is false if both p and q are true; it is true only when exactly one of p and q is true.
- A <u>negation</u> is a proposition of the form "not p" and is represented symbolically by  $\sim p$ . The proposition  $\sim p$  is true if p is false and vice versa.

## Section 6.1 - Sets

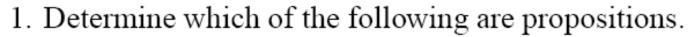
- · A set is a well-defined collection of objects.
- . The objects in a set are called the elements of the set.
- Example of roster notation:  $A = \{a, e, i, o, u\}$
- Example of set-builder notation:  $B = \{x | x \text{ is a student at Texas A&M}\}$
- . Two sets are equal if and only if they have exactly the same elements.
- If every element of a set A is also an element of a set B, then we say that A is a subset of B and write
  A ⊆ B.
- If  $A \subseteq B$  but  $A \neq B$ , then we say A is a proper subset of B and write  $A \subseteq B$ .
- The set that contains no elements is called the empty set and is denoted by 0. (NOTE: {} = 0, but{0} ≠ 0.)
- The union of two sets A and B, written A∪B, is the set of all elements that belong either to A or to B or
  to both
- The intersection of two sets A and B, written  $A \cap B$ , is the set of elements that A and B have in common.
- Two sets A and B are said to be **disjoint** if they have no elements in common, i.e., if  $A \cap B = \emptyset$ .
- If U is a universal set and A is a subset of U, then the set of all elements in U that are not in A is called
  the complement of A and is denoted A<sup>c</sup>.
- De Morgan's Laws Let A and B be sets. Then

 $(A \cup B)^c = A^c \cap B^c$  $(A \cap B)^c = A^c \cup B^c$ 

## ction 6.2 - The Number of Elements in a Finite Set

- The number of elements in a set A is denoted by n(A).
- For any two sets A and B,  $n(A \cup B) = n(A) + n(B) n(A \cap B)$ .
- For any three sets A, B, and C,  $n(A \cup B \cup C) = n(A) + n(B) + n(C) n(A \cap B) n(A \cap C) n(B \cap C) + n(A \cap B \cap C)$ .

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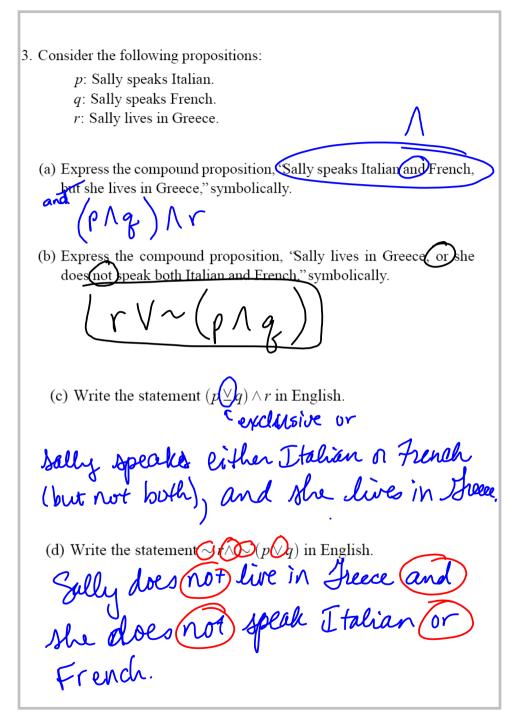
- (a) Do you know when the review starts? Vo. (question)
  (b) What a surprise! Vo (exclamation)
- (c) She wore a black suit to the meeting.
- (c) She wore a black sun to the limit of the sum of the sum of the number 4 is an odd number. He sum of the sentence that cannot be classified as either true or salse.)
  - (f) Some of guests ate cake. Yes
- (g) Please take off your hat before entering the MSC.

  To No (command or request)

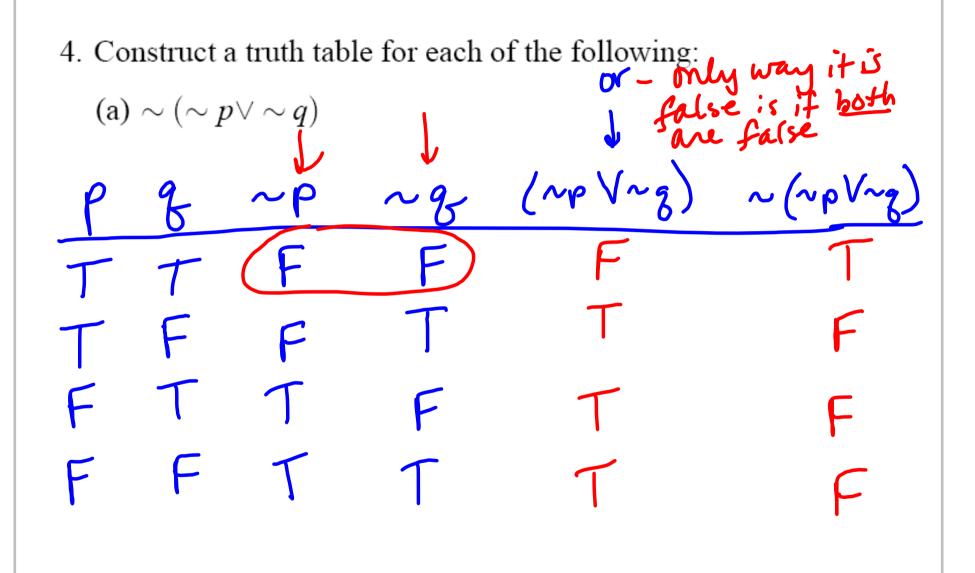
2. Write the negation of the following propositions. (a) Bob will arrive before 8 p.m. Bob will not arrive before 8pm. (Bob will arrive at 8pm or agter) At least one
(b) Some of the committee members missed the meeting. None of the committee members missed the meeting. (c) Some of the kindergartners are not listening to the teacher. all the kindergartners are listening to the teacher (none of the kindergarthers are not Listening ---)
(d) All of the pencils have been sharpened. Not all of the pencils have been sharpened. (both are correct) At least one of the pencils has not been sharpened.

(e) None of the sodas are cold. Some of the sodas are cold. o are cold

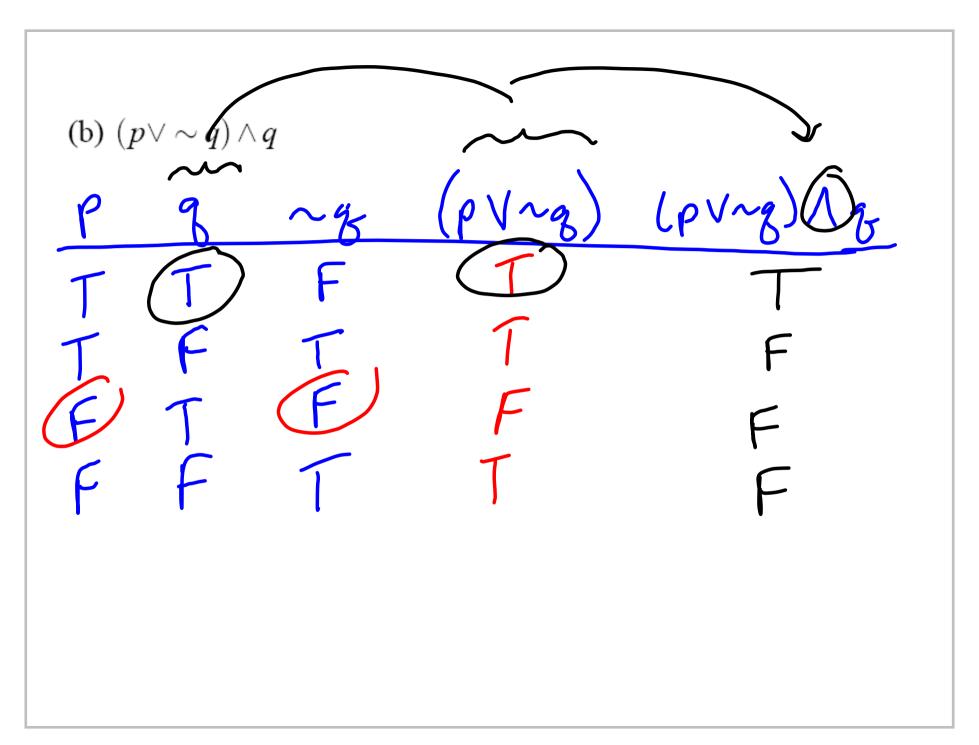
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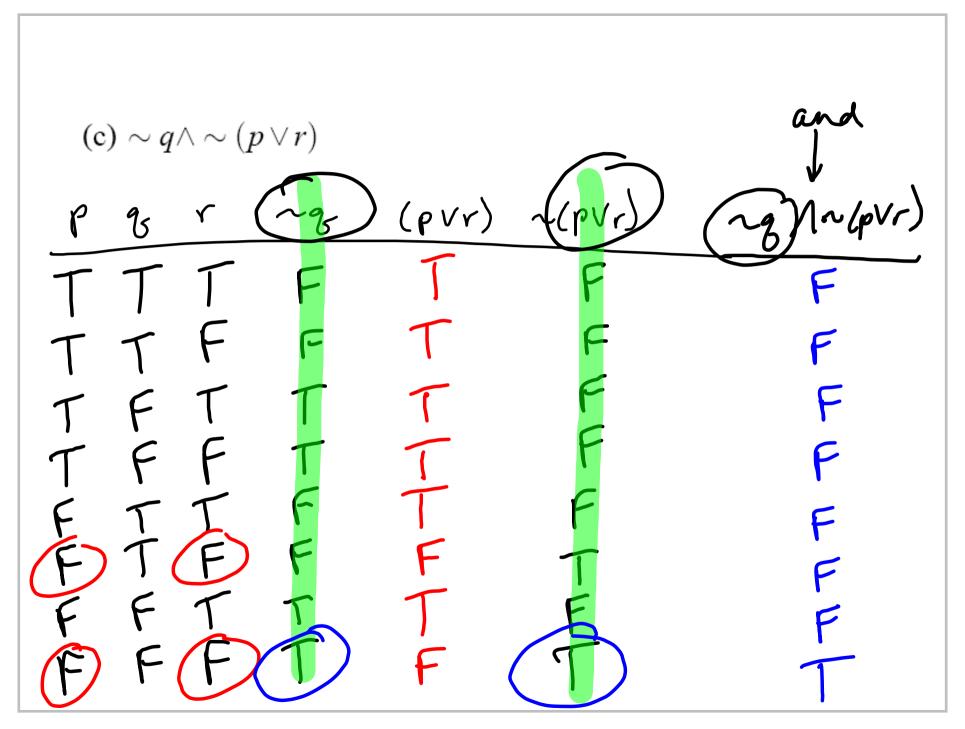
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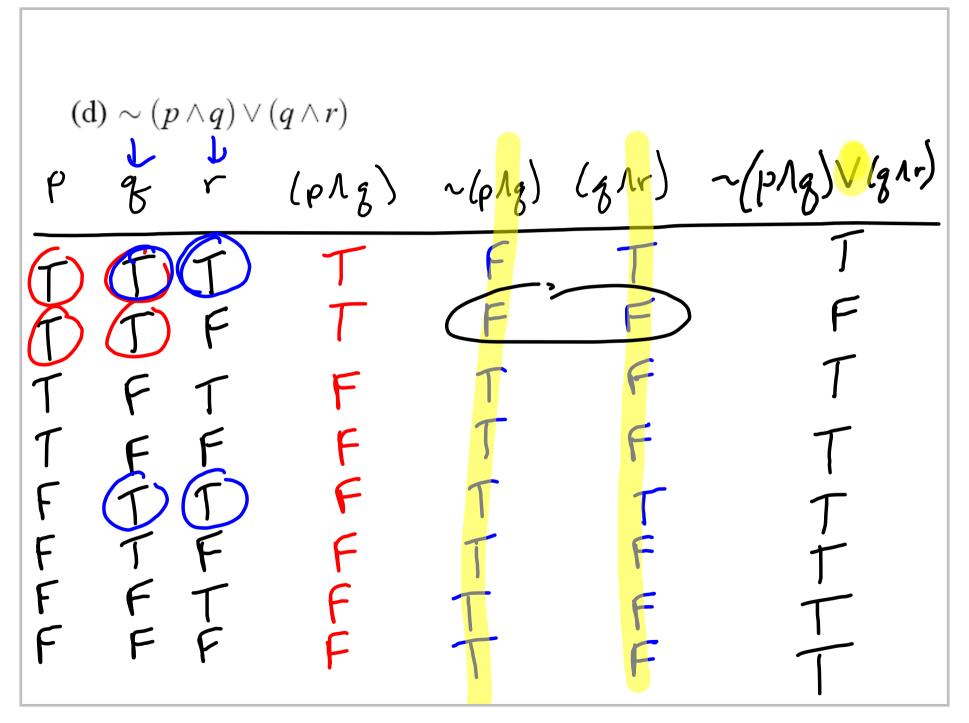


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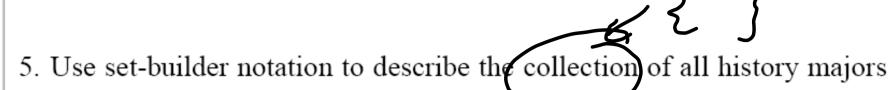


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Title: Oct 9-6:37 PM (9 of 23)



H = 
$$\frac{3}{4}$$
 |  $\chi$  is a history my or at Aim?

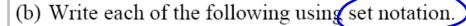
6. Write the set  $\{x|x \text{ is a letter in the word ABRACADABRA}\}$  in roste notation.

$$S = \{a, b, r, c, d\}$$

at Texas A&M University.

7. Le Ube the set of all A&M students. Define $D$ , $A$ , and $C$ as follows: $D = \{x \in U   x \text{ watches Disney movies}\}$
7. Let $U$ be the set of all A&M students. Define $D$ , $A$ , and $C$ as follows:
$D = \{x   U   x \text{ watches Disney movies} \}$
$A = \{x \in U   x \text{ watches action movies} \}$ $C = \{x \in U   x \text{ watches comedy movies} \}$
$C = \{x \in U   x \text{ watches comedy movies}\}$
(a) Describe each of the following sets in words.
i. AOC = The set of all students at Agri
i. $AOC = $ the set of all students at Aim who watch action or comedy movies.
/ inDandinc and not in A
The set of all AEM students who watch Toisney nove and comedy nove and not action moves
watch Bisney move, and comedy movies
(and) not action moves
$ \begin{array}{c}                                     $
<b>↑ ↑</b>
or or
The Det of all AFM Student who watch
Tisney or action or comedy mortes.
(the cet who watch at least
Disney of action or comedy mortes.  iv. $C \cap (D \cup A)$ (the set who watch at least iv. $C \cap (D \cup A)$ one of these 3 types of movies)
11 . 1 0 10 15 m 12 1 1 1 - 1 1 1 2 1 1 1 1 1 1 1 1 1 1
The set of all AEM stridents who
watch come dy and who watch (either) Disney in action movies (or both).
white (or hold)
Brey or across proves.

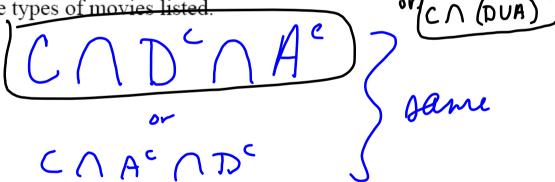
Title: Oct 9-6:37 PM (11 of 23)



i. The set of all A&M students who watch comedy movies but not Disney movies.



three types of movies listed.



iii. The set of all A&M students who watch Disney movies or do not watch action movies.



8. Let 
$$U = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}, A = \{1, 5, 10\}, B = \{1, 3, 5, 7, 9\}, and  $C = \{2, 4, 6, 10\}$ . Find each of the following.$$

(a)  $A \cup B$ 

(b) 
$$B \cap C$$

and  $B \cap C = \emptyset = \{3\}$ 

$$B \cup C = \{(3,5,7,9,2,4,6,0)\}$$

(e)  $(A \cup C)^c \cup B$ 

Title: Oct 9-6:38 PM (13 of 23)

(f) How many subsets does C have?
If S is a set with n elements, then
5 has 2 subsets. (4 1)
Shas 2 <sup>n</sup> subsets. Chas 4 elements so Chas 2 = [16] subsets
(g) How many proper subsets does C have?
16-1 = 15 proper subsets
(h) Are A and C disjoint sets)
7 check AAC
AMC = 2103 Not disjoint because they  (i) Are B and C disjoint sets? have an element in common
(i) Are B and C disjoint sets have an element in common
BNC=P
Since Band Chave no celement in common, they
celements in common, they
are disjoint.

Title: Oct 9-6:38 PM (14 of 23)

9. Let 
$$U = \{a, b, c, d, e, f, g, h, i\}$$
,  $A = \{a, c, h, i\}$ ,  $B = \{b, c, d\}$ ,  $C = \{a, b, c, d, e, i\}$ , and  $D = \{d, b, c\}$ .

- (a) Find n(A).  $\bigcap (A) = 4$
- (b) Find  $n(B \cup C)$ .

$$n(BUC) = n(B) + n(C) - n(BC)$$

$$= 3 + 6 - 3$$

$$= 10$$

(c) Find  $n(A \cap B)$ .

$$\Lambda(A \cap B) = 1$$

subset

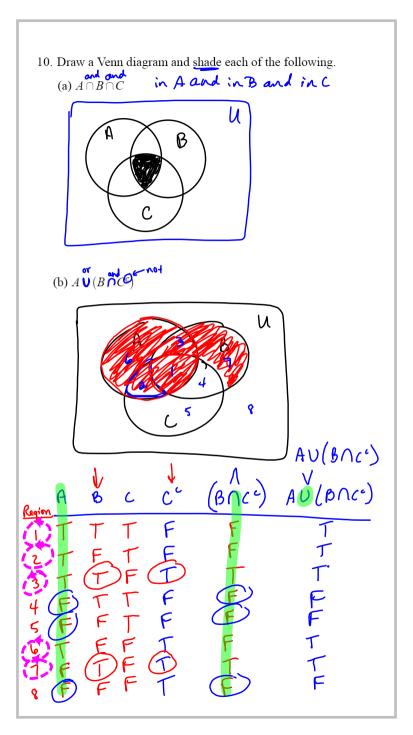
Use the sets above to determine if the following are true of false.

- (d) TRUE (FALSE ) (Is everything in A also in C?)
- TRUE FALSE BOC proper subset
- (f) TRUE FALSE D ⊂ B (B did not have more
- (g) TRUE PALSE 0 ⊆ A Empty set is a subset of every
- (h) TRUE FALSE {c} Q element of
- (i) TRUE FALSE  $d \in C$
- TRUE FALSE  $C \cup C^c = U$
- (k) TRUE (FALSE)  $A \cap A^c = 0$
- (1) TRUE FALSE  $(B \cup B^c)^c = \emptyset$

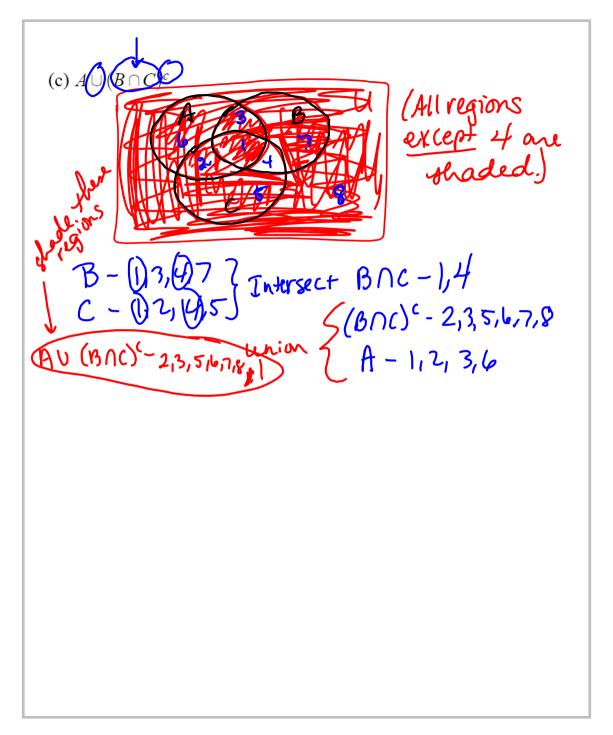
 $(A \cup B)^c = A^c \cap B^c$   $(A \cap B)^c = A^c \cup B^c$ 

element G  $\{c\} \in A$  $\{c\} \subset A$  True  $\{c\} \in A$  False!  $c \in A$  True

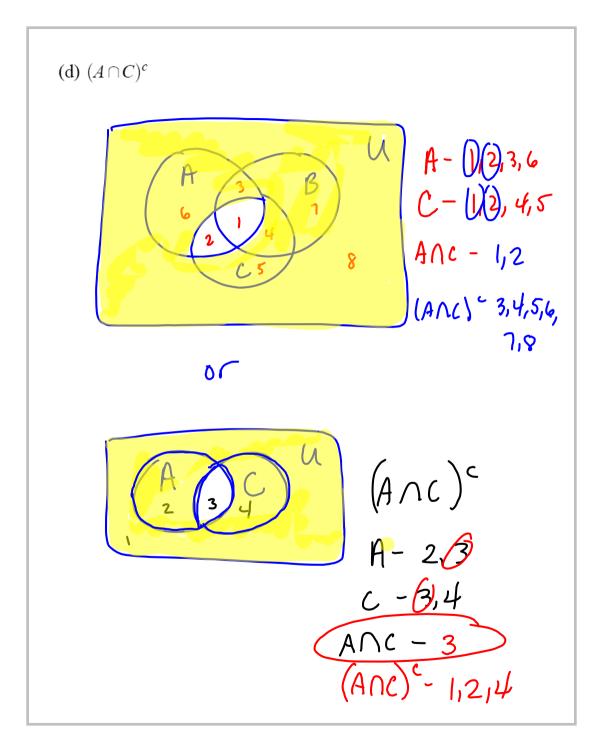
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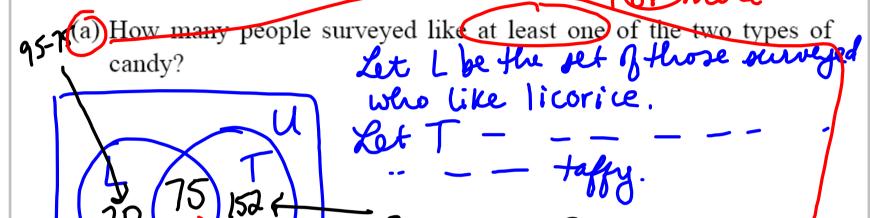


Title: Oct 9-6:41 PM (19 of 23)



Title: Oct 9-9:11 PM (20 of 23)

11. A survey of 300 people found that 95 of those surveyed like licorice, 75 like taffy and licorice, and 53 like neither of these two candies.



300-20-75-53=152 n(LUT)=20+75+152=247

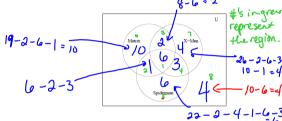
(b) How many people surveyed like exactly one of these two types of candy?

(add the #5 \ regions 244)

- 12. A survey of some college students was conducted to see which of the following three movies they had seen: The Matrix, X-Men, and Spiderman. It was found that
- \ 6 students had seen all three movies.
- 8 students had seen The Matrix and X-Men
- students had seen X-Men and Spiderman but not The Matrix.
- 6 students had seen exactly 2 of the 3 movies.
- 👉 🕩 10 students had seen neither X-Men nor The Matrix. (regions 🦻
  - (19 students had seen The Matrix. 126 students had seen The Matrix or X-Men.

  - 22 students had seen X-Men or Spiderman.

(a) Fill in the Venn Diagram, illustrating the above information.



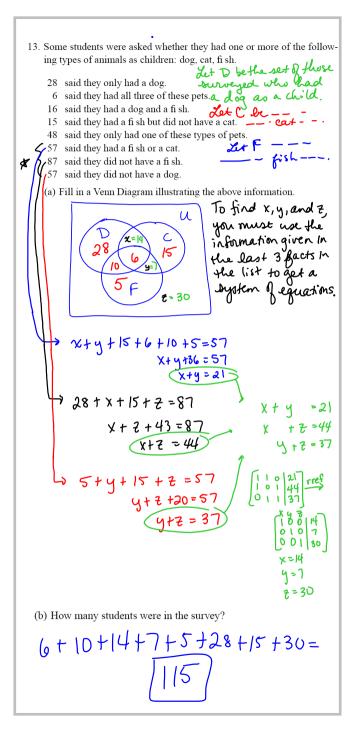
(b) How many students surveyed had seen at least one of the three movies (regions 1-7)

(c) How many students surveyed had seen only Spiderman?

(d) How many students surveyed had seen The Matrix or X-Men but not

(e) How many students surveyed had seen *The Matrix* and *Spiderman*?

Title: Oct 9-6:42 PM (22 of 23)



Title: Oct 9-6:42 PM (23 of 23)