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Math 166 - Week in Review #7

Section 7.2 - Definition of Probability

- The probability of an event is a number between 0 and 1 inclusive that indicates the likelihood of that event occurring. The closer the probability is to 1, the more likely the event is to occur.
- <u>Probability Distribution</u> a table that lists all of the simple events of an experiment and their corresponding probabilities.

NOTE: The sum of all probabilities in a probability distribution is always 1.

- Uniform Sample Space a sample space in which all outcomes are equally likely.
- If $E = \{s_1, s_2, \dots, s_k\}$ is an event of an experiment with sample space S, then $P(E) = P(s_1) + P(s_2) + \dots + P(s_k)$.

Section 7.3 - Rules of Probability

Let S be a sample space of an experiment and suppose E and F are events of the experiment. Then

- 1. $0 \le P(E) \le 1$ for any E.
- 2. P(S) = 1
- 3. If *E* and *F* are mutually exclusive, then $P(E \cup F) = P(E) + P(F)$.
- 4. If E and F are any two events of an experiment, then $P(E \cup F) = P(E) + P(F) P(E \cap F)$.
- 5. $P(E^c) = 1 P(E)$ (Rule of Complements)

NOTE: When calculating probabilities, Venn Diagrams can sometimes be useful. De Morgan's Laws may also come in handy from time to time: $(E \cap F)^c = E^c \cup F^c$ and $(E \cup F)^c = E^c \cap F^c$.

Section 7.4 - Use of Counting Techniques in Probability

• <u>Computing the Probability of an Event in a Uniform Sample Space</u> - Let *S* be a uniform sample space and let *E* be any event. Then

$$P(E) = \frac{number\ of\ favorable\ outcomes\ in\ E}{number\ of\ possible\ outcomes\ in\ S} = \frac{n(E)}{n(S)}$$

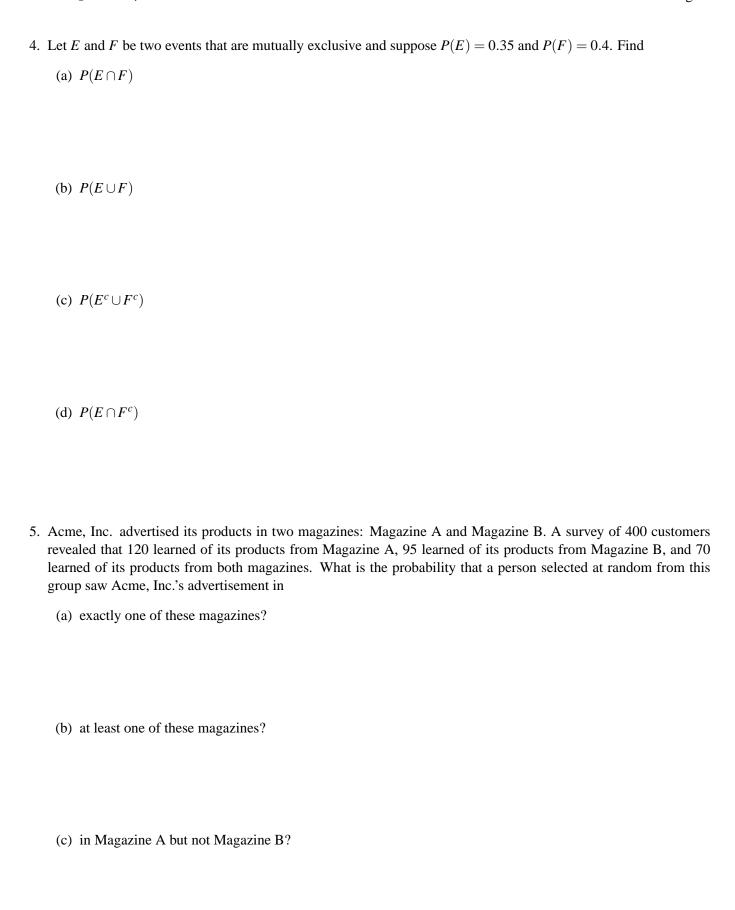
1.	Two	fair four-sided dice are cast and the numbers that land up on the first and second dice are recorded.
	(a)	What is the sample space of this experiment?
	(b)	Is this a uniform sample space? Why or why not?
	(c)	Write the event that the sum of the dice is 6.
	. •	
	(d)	What is the probability that the first die is a 2 and the second die is even?
	(e)	What is the probability that the sum of the numbers shown on the dice is less than 4 or at least one die shows
		a 1?
	_	
2.		fair four-sided dice are cast and the sum of the numbers landing up is recorded.
	(a)	What is the sample space of this experiment?
	(b)	Find the probability distribution for this experiment.
	(c)	Is this a uniform sample space? Why or why not?
	(d)	Write the event that the sum of the dice is 6.

3. Let $S = \{s_1, s_2, s_3, s_4, s_5, s_6\}$ be the sample space of an experiment with the following probability distribution:

Outcome	s_1	s_2	<i>s</i> ₃	s_4	S 5	s_6
Probability	$\frac{3}{40}$	$\frac{4}{40}$	$\frac{7}{40}$	$\frac{14}{40}$		

Let $A = \{s_1, s_3, s_5\}$, $B = \{s_3, s_4, s_6\}$, and $C = \{s_2, s_4\}$ be events of the experiment and suppose $P(B) = \frac{24}{40}$.

- (a) Fill in the missing probabilities in the probability distribution above.
- (b) Is this a uniform sample space? Why or why not?
- (c) Find each of the following:
 - i. P(A)
 - ii. *P*(*C*)
 - iii. $P(B^c)$
 - iv. $P(A \cap B)$
 - v. $P(A \cup B)$
- (d) Are the events A and C mutually exclusive? Why or why not?

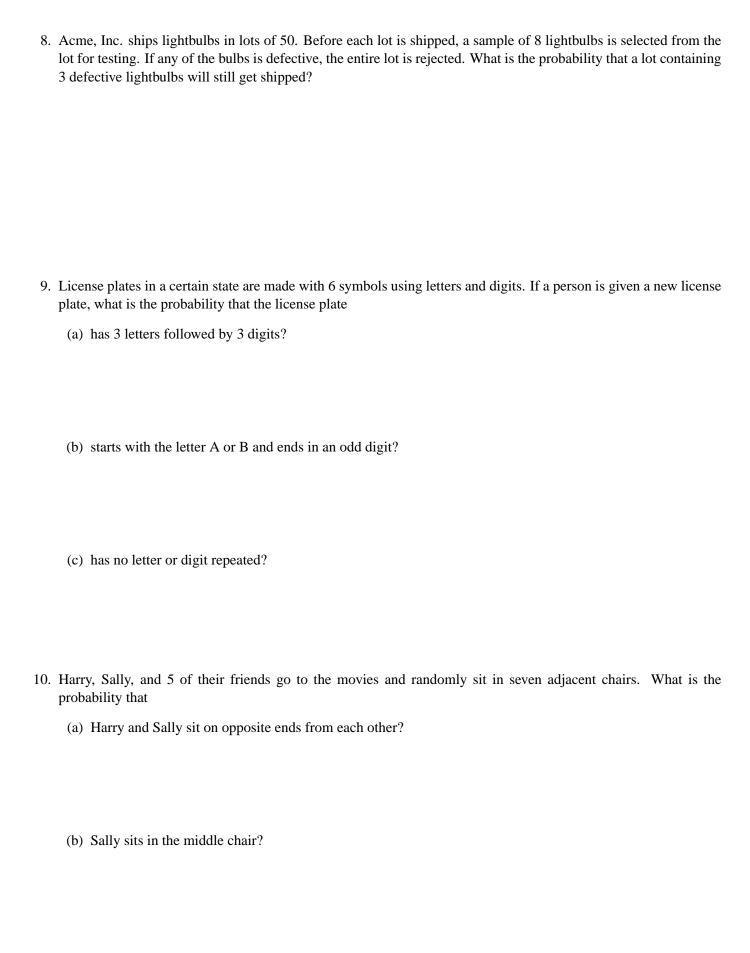


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Information about a Standard Deck of 52 Cards

- There are 4 suits: hearts, diamonds, clubs, and spades.
- Hearts and diamonds are red; clubs and spades are black.
- There are 13 cards in each suit: Ace, 2, 3, 4, 5, 6, 7, 8, 9, 10, Jack, Queen, and King.
- Jacks, Queens, and Kings are called face cards, so there are 12 face cards in a standard deck of 52 cards.

6.	One card is drawn at random from a standard deck of 52 playing cards. What is the probability that the card is (a) a club?
	(b) a face card?
	(c) a club or a face card?
	(d) neither a club nor a face card?
7.	A box contains 2 red marbles, 8 yellow marbles, 6 red gumballs, 5 yellow gumballs, and 3 blue jawbreakers. If a sample of 5 objects is randomly chosen from the box (without replacement), what is the probability that (a) exactly 3 yellow marbles are chosen?
	(b) exactly 3 red gumballs and exactly 2 yellow objects are chosen?
	(c) exactly 4 yellow marbles or exactly 1 blue jawbreaker is chosen?
	(d) at least 1 yellow marble is chosen?



	(c) Harry and Sally sit together?
	(d) Harry and Sally do not sit together?
11.	Three married couples go to the movies. If these 6 people randomly sit in 6 adjacent chairs, what is the probability that each person sits next to his or her spouse (i.e., married couples sit together)?
12.	A student studying for a vocabulary test knows the meanings of 12 words from a list of 21 words. If the test contains 10 word from the study list, what is the probability that at least 6 of the words on the test are words that the student knows?
13.	Find the probability that in a group of 6 people that at least two of them were born in November. Assume that all months are equally likely.