

10-21. Show that $g_n(\lambda)$ defined by Eq. (10-47) obeys the following recursion formula:

$$g_{n-1} = \frac{\partial g_n}{\partial(\ln \lambda)}$$

Also show that for λ close to unity, that

$$g_{5/2}(\lambda) = 2.363(-\ln \lambda)^{3/2} + 1.342 + 2.612 \ln \lambda - 0.730 (\ln \lambda)^2 + \dots$$

From these two results, show that the discontinuity of $(\partial C_V / \partial T)$ at $T = T_c$ for an ideal Bose-Einstein gas is

$$\left(\frac{\partial C_V}{\partial T}\right)_{T \rightarrow T_c + \epsilon} - \left(\frac{\partial C_V}{\partial T}\right)_{T \rightarrow T_c - \epsilon} = \frac{3.66 Nk}{T_c}$$