

7.4.2) Write down an integral formula for the flux of an electric field through the can in the previous example. Consider the unspecified field $E(\vec{r})$.

$$\text{Flux} = \iint_S \vec{E}(\vec{r}) \cdot d\vec{S} = \iint_S (\vec{E}(\vec{r}) \cdot \hat{n}) dS$$

$$\text{Where } \hat{n} = \frac{\vec{r}}{\|\vec{r}\|} = \hat{r}$$

And we know that for a cylinder of radius R, $dS = R d\theta dz$, therefore:

$$\text{Flux} = 4 \int_0^{15} \int_0^{2\pi} \vec{E}(\vec{r}) \cdot \hat{r} d\theta dz + \int_0^4 \int_0^{2\pi} \vec{E}(\vec{r}) \cdot \hat{k} d\theta dr + \int_0^4 \int_0^{2\pi} \vec{E}(\vec{r}) \cdot -\hat{k} d\theta dr$$

The last two integrals account for the top and bottom of the cylinder. $E(r)$ in these two needs to be evaluated at the points of $z = 0$ (for \hat{k}) and $z = 15$ (for $-\hat{k}$).