

Basics of Probability

When we toss a fair coin the two outcomes in the sample space $S = \{H, T\}$ are equally likely, so the probability of each outcome is $1/2$.

This is a THEORETICAL PROBABILITY based on the sample space having equally likely outcomes.

In general, this is the way we will find probability, by using a sample space of EQUALLY LIKELY OUTCOMES.

The probability of an event, $P(E)$ is a number between 0 and 1,

We can also calculate the EMPIRICAL PROBABILITY of an event by doing an experiment many times.

For example, you could toss a coin and note how many times it comes up heads (shown in book)

or you could roll a die and count how many times a 1 is rolled.

number of tosses (m)	number of 1's rolled (n)	relative frequency (n/m)

(SUBJECTIVE PROBABILITY)

UNIFORM SAMPLE SPACE $S=\{s_1,s_2, \dots,s_n\}$,

$\{s_1\}, \{s_2\} \dots \{s_n\}$ are called SIMPLE events

Notice these simple events are MUTUALLY EXCLUSIVE as only one can occur.

PROBABILITY DISTRIBUTION TABLE:

Event	probability

Properties of probability distribution tables:

Toss a coin three times. There are 8 equally likely outcomes:

Event	Probability
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Find the probability distribution table for the number of heads when a coin is tossed 3 times.

$S = \{HHH, HHT, HTH, HTT, THH, THT, TTH, TTT\}$

What is the probability of 2 or more heads?

What is the probability of rolling a sum 2 or a sum of 12 using two fair die?

1~1	2~1	3~1	4~1	5~1	6~1
1~2	2~2	3~2	4~2	5~2	6~2
1~3	2~3	3~3	4~3	5~3	6~3
1~4	2~4	3~4	4~4	5~4	6~4
1~5	2~5	3~5	4~5	5~5	6~5
1~6	2~6	3~6	4~6	5~6	6~6

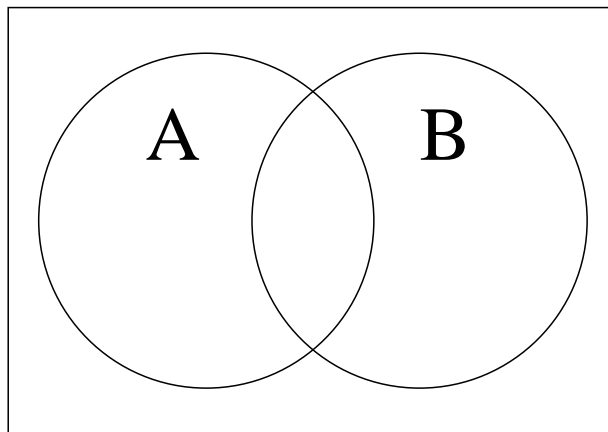
What is the probability of rolling a sum of 7?

1~1	2~1	3~1	4~1	5~1	6~1
1~2	2~2	3~2	4~2	5~2	6~2
1~3	2~3	3~3	4~3	5~3	6~3
1~4	2~4	3~4	4~4	5~4	6~4
1~5	2~5	3~5	4~5	5~5	6~5
1~6	2~6	3~6	4~6	5~6	6~6

Rules for Probability

If event A and event B are mutually exclusive then

In general, A and B have some outcomes in common so we have the union rule for probability:



Example: Let

$E = \{x \mid x \text{ is a sum of } 7\} =$

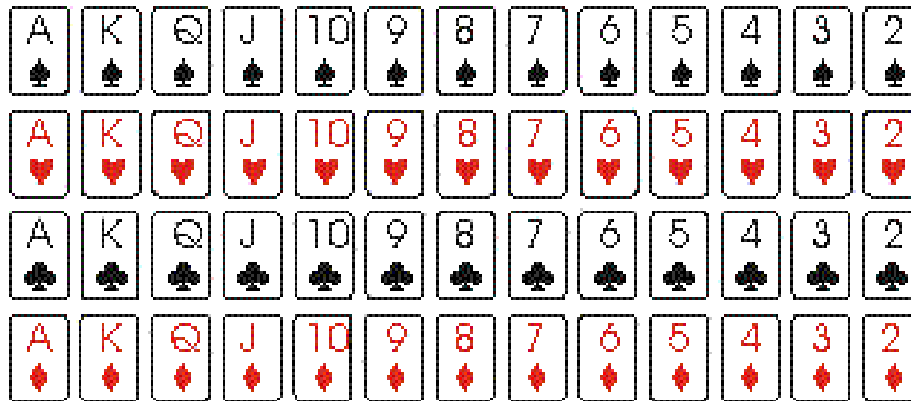
and

$F = \{x \mid x \text{ is a } 6 \text{ on the green die}\} =$

1~1	2~1	3~1	4~1	5~1	6~1
1~2	2~2	3~2	4~2	5~2	6~2
1~3	2~3	3~3	4~3	5~3	6~3
1~4	2~4	3~4	4~4	5~4	6~4
1~5	2~5	3~5	4~5	5~5	6~5
1~6	2~6	3~6	4~6	5~6	6~6

What is the probability that you have a sum of 7 OR a 6 on the green die?

A standard deck of 52 cards has 4 suits, each with 13 cards. The suits are spades, ♠, hearts, ♥, clubs, ♣, and diamonds, ♦. The cards in each suit are numbered from Ace, King, Queen, Jack, ten down to 2.



Example - If a single card is drawn from a standard deck of cards, what are the probabilities of

a) a 9 or a 10? Let

b) a black card or a 3?

Example - a survey gave the following results: 45% of the people surveyed drank diet drinks (D) and 25% drank diet drinks and exercised ($D \cap E$) and 24% did not exercise and did not drink diet drinks ($D^c \cap E^c$). Find the probability that:

- a) a person does not drink diet drinks (D^c).
- b) does not exercise and drinks diet drinks ($E^c \cap D$).
- c) exercises and does not drink diet drinks ($E \cap D^c$).

Draw the diagram.