

Week in Review # 11

1. (a)
$$\begin{matrix} & \text{Red 6} & \text{Black 7} & \text{Black 8} \\ \text{Red 2} & 4 & -2 & -2 \\ \text{Black 10} & -6 & 3 & 2 \end{matrix}$$

(b) Row 1

(c) Column 3

2. (a) option 1: R-1 and C-4
option 2: R-3 and C-1

(b) R-3 and C-4

3. (a) yes it is strictly determined.
optimal strategy:
row player: row 2
column player: column 2
value of the game = 4

(b) not strictly determined.

- (c) yes it is strictly determined.
optimal strategy:
row player: row 2 or row 4
column player: column 2
value of the game = 2

4.
$$A = \begin{matrix} & \text{Red 6} & \text{Black 7} & \text{Black 8} \\ \text{red 2} & 4 & -2 & -2 \\ \text{black 10} & -6 & 3 & 2 \end{matrix}$$

(a)
$$Q = \begin{bmatrix} 0.25 \\ 0.30 \\ 0.45 \end{bmatrix}$$

compute the expected value for each of these strategies.

$$P_1 = [0.5 \quad 0.5], E = P_1 A Q = -0.1$$

$$P_2 = [0.6 \quad 0.4], E = P_2 A Q = -0.18$$

$$P_3 = [0.35 \quad 0.75], E = P_3 A Q = 0.05$$

The best for John is P_3 since this expected value is the largest.

(b) $0.05 * 1,000 = 50$

5. (a) nothing can be eliminated.

(b)
$$\begin{bmatrix} 8 & -1 \\ -3 & 0 \end{bmatrix}$$

(c)
$$\begin{bmatrix} -5 \\ 0 \end{bmatrix}$$

6. (a)
$$P = \begin{bmatrix} \frac{3}{16} & \frac{13}{16} \end{bmatrix} \quad Q = \begin{bmatrix} \frac{14}{16} \\ \frac{2}{16} \\ \frac{16}{16} \end{bmatrix}$$

value = $\frac{54}{16}$

(b) reduce to
$$\begin{bmatrix} 5 & 2 \\ -2 & 7 \end{bmatrix}$$

$$P = \begin{bmatrix} \frac{3}{4} & 0 & \frac{1}{4} \end{bmatrix}$$

$$Q = \begin{bmatrix} \frac{5}{12} \\ \frac{7}{12} \\ \frac{12}{12} \end{bmatrix}$$

value = $\frac{39}{12}$

- (c) saddle point in row 1 column 1.

$$P = [1 \quad 0 \quad 0] \quad Q = \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

value = 1

(d) reduce to
$$\begin{bmatrix} -2 & 4 \\ 1 & -3 \end{bmatrix}$$

$$P = [0 \quad 0.4 \quad 0.6]$$

$$Q = \begin{bmatrix} 0 \\ 0.7 \\ 0.3 \\ 0 \end{bmatrix}$$

value = -0.2