

11.4 # 5 note! The series has positive terms

by LCT

Known Series $\sum \frac{1}{\sqrt[3]{n^2}} = \sum \frac{1}{n^{2/3}}$

p-series

$$p = 2/3$$

diverge

$$\lim_{n \rightarrow \infty} \frac{\frac{1}{\sqrt[3]{n^2-3}}}{\frac{1}{\sqrt[3]{n^2}}} = \lim_{n \rightarrow \infty} \frac{\sqrt[3]{n^2}}{\sqrt[3]{n^2-3}} = \lim_{n \rightarrow \infty} \sqrt[3]{\frac{n^2}{n^2-3}} = \sqrt[3]{1} = 1$$

by LCT the series $\sum \frac{1}{\sqrt[3]{n^2-3}}$ will diverge.

By comparison test:

$$n^2 - 3 < n^2$$
$$\sqrt[3]{n^2-3} < \sqrt[3]{n^2}$$

$$\frac{1}{\sqrt[3]{n^2-3}} > \frac{1}{\sqrt[3]{n^2}}$$

$$\sum \frac{1}{\sqrt[3]{n^2}}$$

diverges since
it is a p-series
 $p = 2/3$.

By comparison test

$$\sum \frac{1}{\sqrt[3]{n^2-3}} \text{ will diverge}$$