

Math 166 - Week in Review #7**Section 7.2 - Definition of Probability**

- The probability of an event is a number between 0 and 1 inclusive that indicates the likelihood of that event occurring. The closer the probability is to 1, the more likely the event is to occur.
- **Probability Distribution** - a table that lists all of the simple events of an experiment and their corresponding probabilities.

NOTE: The sum of all probabilities in a probability distribution is always 1.

- **Uniform Sample Space** - a sample space in which all outcomes are equally likely.
- If $E = \{s_1, s_2, \dots, s_k\}$ is an event of an experiment with sample space S , then $P(E) = P(s_1) + P(s_2) + \dots + P(s_k)$.

Section 7.3 - Rules of Probability

Let S be a sample space of an experiment and suppose E and F are events of the experiment. Then

1. $0 \leq P(E) \leq 1$ for any E .
2. $P(S) = 1$
3. If E and F are mutually exclusive, then $P(E \cup F) = P(E) + P(F)$.
4. If E and F are any two events of an experiment, then $P(E \cup F) = P(E) + P(F) - P(E \cap F)$.
5. $P(E^c) = 1 - P(E)$ (Rule of Complements)

NOTE: When calculating probabilities, Venn Diagrams can sometimes be useful. De Morgan's Laws may also come in handy from time to time: $(E \cap F)^c = E^c \cup F^c$ and $(E \cup F)^c = E^c \cap F^c$.

Section 7.4 - Use of Counting Techniques in Probability

- **Computing the Probability of an Event in a Uniform Sample Space** - Let S be a uniform sample space and let E be any event. Then

$$P(E) = \frac{\text{number of favorable outcomes in } E}{\text{number of possible outcomes in } S} = \frac{n(E)}{n(S)}$$

1. Two fair four-sided dice are cast and the numbers that land up on the first and second dice are recorded.
 - (a) What is the sample space of this experiment?

 - (b) Is this a uniform sample space? Why or why not?

 - (c) Write the event that the sum of the dice is 6.

 - (d) What is the probability that the first die is a 2 and the second die is even?

 - (e) What is the probability that the sum of the numbers shown on the dice is less than 4 or at least one die shows a 1?

2. Two fair four-sided dice are cast and the sum of the numbers landing up is recorded.
 - (a) What is the sample space of this experiment?

 - (b) Find the probability distribution for this experiment.

 - (c) Is this a uniform sample space? Why or why not?

 - (d) Write the event that the sum of the dice is 6.

3. Let $S = \{s_1, s_2, s_3, s_4, s_5, s_6\}$ be the sample space of an experiment with the following probability distribution:

Outcome	s_1	s_2	s_3	s_4	s_5	s_6
Probability	$\frac{3}{40}$	$\frac{4}{40}$	$\frac{7}{40}$	$\frac{14}{40}$		

Let $A = \{s_1, s_3, s_5\}$, $B = \{s_3, s_4, s_6\}$, and $C = \{s_2, s_4\}$ be events of the experiment and suppose $P(B) = \frac{24}{40}$.

(a) Fill in the missing probabilities in the probability distribution above.

(b) Is this a uniform sample space? Why or why not?

(c) Find each of the following:

i. $P(A)$

ii. $P(C)$

iii. $P(B^c)$

iv. $P(A \cap B)$

v. $P(A \cup B)$

(d) Are the events A and C mutually exclusive? Why or why not?

4. Let E and F be two events that are mutually exclusive and suppose $P(E) = 0.35$ and $P(F) = 0.4$. Find
- (a) $P(E \cap F)$

 - (b) $P(E \cup F)$

 - (c) $P(E^c \cup F^c)$

 - (d) $P(E \cap F^c)$
5. Acme, Inc. advertised its products in two magazines: Magazine A and Magazine B. A survey of 400 customers revealed that 120 learned of its products from Magazine A, 95 learned of its products from Magazine B, and 70 learned of its products from both magazines. What is the probability that a person selected at random from this group saw Acme, Inc.'s advertisement in
- (a) exactly one of these magazines?

 - (b) at least one of these magazines?

 - (c) in Magazine A but not Magazine B?

Information about a Standard Deck of 52 Cards

- There are 4 suits: hearts, diamonds, clubs, and spades.
 - Hearts and diamonds are red; clubs and spades are black.
 - There are 13 cards in each suit: Ace, 2, 3, 4, 5, 6, 7, 8, 9, 10, Jack, Queen, and King.
 - Jacks, Queens, and Kings are called face cards, so there are 12 face cards in a standard deck of 52 cards.
6. One card is drawn at random from a standard deck of 52 playing cards. What is the probability that the card is
- (a) a club?
 - (b) a face card?
 - (c) a club or a face card?
 - (d) neither a club nor a face card?
7. A box contains 2 red marbles, 8 yellow marbles, 6 red gumballs, 5 yellow gumballs, and 3 blue jawbreakers. If a sample of 5 objects is randomly chosen from the box (without replacement), what is the probability that
- (a) exactly 3 yellow marbles are chosen?
 - (b) exactly 3 red gumballs and exactly 2 yellow objects are chosen?
 - (c) exactly 4 yellow marbles or exactly 1 blue jawbreaker is chosen?
 - (d) at least 1 yellow marble is chosen?

8. Acme, Inc. ships lightbulbs in lots of 50. Before each lot is shipped, a sample of 8 lightbulbs is selected from the lot for testing. If any of the bulbs is defective, the entire lot is rejected. What is the probability that a lot containing 3 defective lightbulbs will still get shipped?
9. License plates in a certain state are made with 6 symbols using letters and digits. If a person is given a new license plate, what is the probability that the license plate
- (a) has 3 letters followed by 3 digits?
 - (b) starts with the letter A or B and ends in an odd digit?
 - (c) has no letter or digit repeated?
10. Harry, Sally, and 5 of their friends go to the movies and randomly sit in seven adjacent chairs. What is the probability that
- (a) Harry and Sally sit on opposite ends from each other?
 - (b) Sally sits in the middle chair?

