

Name \_\_\_\_\_

MATH 251      Exam 3 Version B      Fall 2017

Sections 515      P. Yasskin

Multiple Choice: (6 points each. No part credit.)

1-10	/60	15	/15
14	/15	16	/15
		Total	/105

1. Compute  $\int_0^2 \int_{x^2}^{2x} 2y \, dy \, dx$ .

a.  $-\frac{56}{15}$

b.  $-\frac{32}{15}$

c.  $\frac{32}{15}$

d.  $\frac{64}{15}$

e.  $\frac{128}{15}$

2. Find the average value of the function  $f(x,y) = x^2 \sin y$  on the rectangle  $[0,3] \times [0,\pi]$ .

a.  $\frac{18}{\pi}$

b.  $\frac{6}{\pi}$

c.  $3\pi$

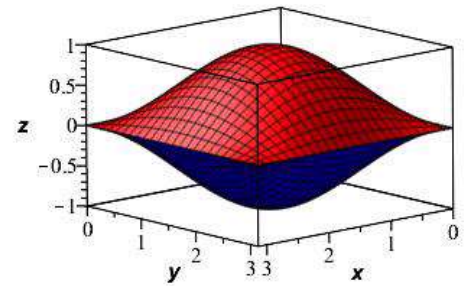
d. 18

e.  $54\pi$

3. Find the volume of the ravioli bounded by

$$-\sin x \sin y \leq z \leq \sin x \sin y$$

for  $0 \leq x \leq \pi$  and  $0 \leq y \leq \pi$ .



- a. 2
- b. 4
- c. 8
- d.  $\pi^2$
- e.  $4\pi^2$

4. Find the mass of a triangular plate with vertices  $(0,0)$ ,  $(2,4)$  and  $(2,-4)$  whose surface mass density is  $\delta = x$ .

- a.  $\frac{32}{3}$
- b.  $\frac{32}{5}$
- c.  $\frac{16}{3}$
- d.  $\frac{16}{5}$
- e.  $\frac{8}{3}$

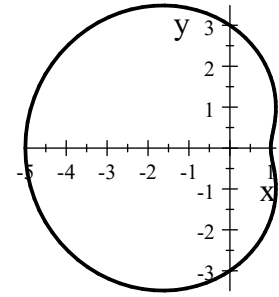
5. Find the center of mass of a triangular plate with vertices  $(0,0)$ ,  $(2,4)$  and  $(2,-4)$  whose surface mass density is  $\delta = x$ .

- a.  $(\frac{2}{3}, 0)$
- b.  $(0, \frac{2}{3})$
- c.  $(\frac{3}{2}, 0)$
- d.  $(0, \frac{3}{2})$
- e.  $(16, 0)$

6. Find the area inside the limaçon

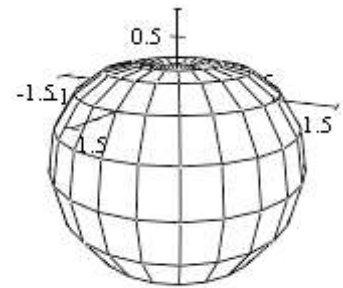
$$r = 3 - 2 \cos \theta.$$

- a.  $\pi$
- b.  $3\pi$
- c.  $7\pi$
- d.  $9\pi$
- e.  $11\pi$



7. Find the volume of the apple whose surface is given in spherical coordinates by  $\rho = 1 - \cos \varphi$ .

- a.  $2\pi$
- b.  $4\pi$
- c.  $\frac{2\pi}{3}$
- d.  $\frac{8\pi}{3}$
- e.  $\frac{16\pi}{3}$



8. Find the normal to the parametric surface  $\vec{R}(u, v) = (u + v, u - v, uv)$

- a.  $(u + v, v - u, -2)$
- b.  $(u + v, u - v, -2)$
- c.  $(u + v, v - u, 2)$
- d.  $(u + v, u - v, 2)$
- e.  $(2, 0, u + v)$

9. Find the mass of the half cylinder **surface**  $x^2 + y^2 = 4$  for  $y \geq 0$  and  $0 \leq z \leq 3$ , with surface mass density  $\delta = y$ . Parametrize the surface as

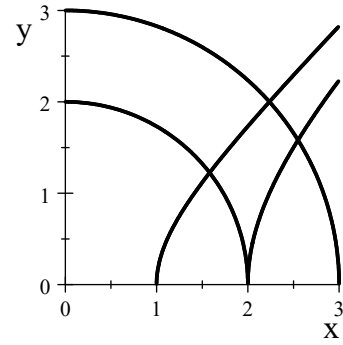
$$\vec{R}(\theta, z) = (2 \cos \theta, 2 \sin \theta, z)$$

- a. 0
  - b. 24
  - c. 48
  - d. 72
  - e. 96
10. Compute the flux  $\iint \vec{F} \cdot d\vec{S}$  of the vector field  $\vec{F} = (xy, y^2, yz)$  through the half cylinder  $x^2 + y^2 = 4$  for  $y \geq 0$  and  $0 \leq z \leq 3$  oriented toward the positive  $y$ -axis.

- a. 0
- b. 24
- c. 48
- d. 72
- e. 96

Work Out: (15 points each. Part credit possible. Show all work.)

11. (15 points) Compute the integral  $\iint xy dA$  over the diamond shaped region in the 1<sup>st</sup> quadrant bounded by  $x^2 + y^2 = 4$ ,  $x^2 + y^2 = 9$ ,  $x^2 - y^2 = 1$ , and  $x^2 - y^2 = 4$ .



12. (15 points) Find the mass of the ice cream cone below the paraboloid  $z = 8 - x^2 - y^2$  above the cone  $z = 2\sqrt{x^2 + y^2}$  if the density is  $\delta = \sqrt{x^2 + y^2}$ .



13. (15 points) Find the centroid of the hemisphere  $0 \leq z \leq \sqrt{9 - x^2 - y^2}$ .

